ADAPT: a price-stabilizing compliance policy for renewable energy certificates: the case of SREC markets


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ADAPT: A PRICE-STABILIZING COMPLIANCE POLICY FOR RENEWABLE ENERGY CERTIFICATES: THE CASE OF SREC MARKETS

Javad Khazaei
Address: ORFE Department
Princeton University
Princeton NJ 08544, USA
Email: jkhazaei@princeton.edu

Michael Coulon (corresponding author)
Address: Department of Business and Management
University of Sussex
Brighton BN1 9SL, UK
Email: m.coulon@sussex.ac.uk

Warren B. Powell
Address: ORFE Department
Princeton University
Princeton NJ 08544, USA
Email: powell@princeton.edu
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ABSTRACT. Currently most Renewable Energy Certificate (REC) markets are defined based on targets which create an artificial step demand function resembling a cliff. This target policy produces volatile prices which can make investing in renewables a risky proposition. In this paper, we propose an alternative policy called Adjustable Dynamic Assignment of Penalties and Targets (ADAPT) which uses a sloped compliance penalty and a self-regulating requirement schedule, both designed to stabilize REC prices, helping to alleviate a common weakness of environmental markets. To capture market behavior, we model the market as a stochastic dynamic programming problem to understand how the market might balance the decision to use a REC now versus holding it for future periods (in the face of uncertain new supply). Then, we present and prove some of the properties of this market, and finally we show that this mechanism reduces the volatility of REC prices which should stabilize the market and encourage long-term investment in renewables.

Keywords: Compliance Policy, Renewable Energy Certificates, Stochastic Dynamic Programming, Price Volatility, Mechanism Design

1. INTRODUCTION

To promote the use of renewable sources of energy such as wind, solar, geothermal and biomass, Renewable Portfolio Standards (RPSs) have been implemented in a number of states in the US and in other countries. These are sets of regulations requiring increased generation from renewable energy sources usually by obligating Load Serving Entities (LSEs) to obtain a percentage of their generation from renewable sources. A Renewable Energy Certificate (REC) market is one tool used by many states to implement these policies. According to a set of regulations, certified renewable generators are credited with RECs for each unit of electricity generated. All LSEs are required to comply with their regulatory obligations by submitting enough RECs each Energy Year (EY), or otherwise they are charged a penalty called the Alternative Compliance Payment (ACP) for each REC they are short. These market-based tools are expected to provide a more efficient, competitive and innovative environment for increasing renewable energy supply and decreasing the cost of generation in comparison with other regulatory tools such as feed-in tariffs ([6, 22]).

This particular market design, however, as we discuss more extensively in the next section, can result in undesirably volatile prices. Although REC markets incentivize investing in renewables, excess volatility can affect the amount of investment negatively, and is thus a frequent concern of policymakers (see e.g. [2]). Indeed, authors who advocate fixed-price environmental policy tools
like carbon taxes often cite this weakness of market-based mechanisms (see e.g. [17]), and the European Union’s Emissions Trading Scheme (ETS) faced heavy criticism in its early years as prices fell rapidly towards zero. Price volatility in both REC and carbon markets is mostly attributed to the artificial vertical demand curve imposed by regulations. A number of papers (such as [11, 3, 18, 21]) discuss extensively the problems arising from a vertical demand curve (or a cliff policy) such as an uncompetitive market, volatile prices, higher cost of investment (due to higher risk), and difficult policy evaluation. Various investigations have also been made into ways of reducing price volatility, such as through banking ([20]), or by trading in financial options if available ([29]). We aim to add to this literature with a new design for environmental markets (and for RECs in particular), accompanied by a rigorous mathematical analysis of its implications.

In this paper, we propose an Adjustable Dynamic Assignment of Penalties and Targets (ADAPT) policy by introducing and assessing both a sloped penalty function and an adaptive mechanism for requirements which can adjust to supply and demand imbalances. Under this sloped penalty proposal, the effective ACP is a function of the total submitted RECs in each energy year. While the requirement is normally not directly a function of the submitted or generated RECs, it can also be chosen to be a function of last year’s surplus (or shortage), a type of self-regulation implemented in the Massachusetts SREC market already, with additional complexities linked to SREC auction results. The slope of the penalty function and the sensitivity to last year’s surplus are both then tunable regulatory parameters. We show in this paper that this mechanism can be used by policy makers to dampen the volatility of market prices which should encourage long-term investment in renewable generation. We conduct our case study of the ADAPT policy using the same solar generation model as [8]. However, by incorporating a sloped penalty function along with banking between years, optimal compliance decisions each period are non-trivial, requiring substantially more analysis. Moreover, instead of modeling each vintage year separately as in [8], we adapt the dynamic program to solve for prices simultaneously across all vintage years, over a long time horizon. This paper makes the following key contributions:

(1) We propose an innovative and flexible regulatory policy (that we call ADAPT), which can be used to encourage markets to achieve specific goals (e.g. energy from renewables, limiting emissions, ethanol targets, recyclable garbage, or water usage), without the instability often witnessed in classical “cliff” designs for pre-determined quantity targets. The ADAPT policy is easily integrated into current markets, and represents a generalizable concept for hitting quantitative targets. Through a set of simulated and theoretical results, we show that ADAPT produces dramatically more stable prices than those under a cliff policy.

(2) We derive an optimal policy for submitting RECs to the market (while banking others), which captures the collective market behavior. We describe a series of structural results to accelerate calculations, and then prove several properties of the optimal policy, including:
(a) We demonstrate how the optimal submission under ADAPT is chosen by market participants to balance prices through time.
(b) We show that the prices of RECs of different vintages (RECs generated in different years) are the same under typical market conditions.
(c) We prove a property of the optimal solution that reduces the decision variable’s dimensionality across vintages to a scalar. Dimensionality of the state variable is also shown to reduce to a scalar under certain typical conditions.

(d) We prove that the total penalty payments under the sloped policy is bounded from below by the total payments of the cliff policy for a given submission level.

(3) We conduct extensive numerical experiments and simulations which confirm and further illustrate the important properties of the model derived in previous sections.

While we focus on REC markets here (and specifically solar RECs, or SRECs), techniques developed here are arguably transferable to other environmental markets and even to other commodity markets, assuming appropriate modifications or extensions. Firstly, cap-and-trade markets for carbon emissions are a natural link, due to their related market designs and compliance features. An ADAPT-like framework could certainly be envisioned for such markets, and indeed the regulators of carbon markets have recently experimented with various tools to stabilize markets, including price floor mechanisms (e.g. California, the UK) and the new EU ETS Market Stability Reserve (starting 2018), designed to offset long-term imbalances via automatically triggered supply adjustments. To our knowledge, the idea of a sloped alternative to a vertical demand curve has not been trialed in REC or carbon markets. However, a similar idea was implemented in the capacity markets of NYISO and New England ISO (see [9, 14, 26] for discussion).

While only very limited literature on stochastic modeling of SREC markets exists (see [1, 8, 16]), carbon emissions markets have attracted much more attention (see [7, 13]), including recent studies of the Market Stability Reserve’s likely impact on prices ([15, 19]). However, various key differences between carbon and REC markets require careful consideration, including the opposite roles for supply and demand, the typical ‘withdrawal’ rule reducing incentives for banking, the possibility of unlimited banking, and the wide range of factors affecting carbon emissions abatement, notably volatile fuel prices and power demand. We argue that SREC markets provide an excellent case study for such modeling techniques, with simpler underlying factors (e.g., solar generation), relative separation from other energy markets (at least for current low levels of renewables penetration) and more transparent data facilitating empirical studies and model calibration, as performed in [8] and [16].

Moving slightly further afield, a large literature on the ‘theory of storage’ exists for storable physical commodities, such as agricultural, metals or energy commodities (see e.g. [25, 10]). Such approaches, called ‘structural models’ by [24], are based on the idea of a storage decision at each time period (often by a representative agent or social planner), and solved via dynamic programming techniques. Our approach under the APADT framework here is closely linked to this class of models, with the commodity’s consumption and storage decisions analogous to our REC submission and banking decisions, albeit with different seasonal patterns and frequencies. Different harvests of perishable commodities are similar to different REC vintages, and the same fundamental intertemporal tradeoffs apply, namely that storing more means consuming less now, producing higher prices now, but lower prices in the future (and less risk of future shortages). However, for
storable physical commodities, such models rely crucially on specifying an unobservable inverse demand curve, again giving the REC case study a significant advantage since the SACP function is set artificially by a regulator.

This paper is organized as follows. In Section 2, we introduce and discuss the market design, regulations, and performance of the New Jersey (NJ) SREC market, including the problems resulting from the current market design. In Section 3, we introduce the ADAPT policy and describe how it can be implemented. In Section 4, we formulate the collective behaviour of market participants using a stochastic dynamic programming model. In Section 5, we characterize and prove some of the properties of the REC markets. In Section 6, we detail our methodology for solving this stochastic dynamic program. In Section 7, we use parameters estimated from New Jersey to perform experiments on different aspects of the ADAPT policy in comparison to the current cliff mechanisms. In Section 8, we provide our concluding remarks.

2. Case Application: The New Jersey SREC Market

In the US, nearly 30 states have established RPSs and some of these use multipliers (e.g. 2 or 3 credits per MWh) to specifically promote investment in solar energy. To further promote the use of solar energy, 14 states have established separate solar set-asides and tradeable SRECs, and have been successful in increasing investment in solar generation ([27, 28, 5, 4, 12]). The New Jersey (NJ) SREC market is the biggest in the US, has recorded prices near $700 per SREC, and has the most ambitious target of over 4% of electricity from solar by 2028. SREC generation has grown very rapidly from around 30,000 SRECs in EY2007 to more than 1,000,000 in EY2013. Each energy year represents the twelve month period ending on May 31st of the named year. Table 1 shows the requirement (currently set in terms of percentage of overall supply, with projected absolute numbers) and Solar ACP (SACP) levels following the 2012 rule change ([5, 23]).

The rules of the current SREC market in New Jersey can be summarized as follows:

- For each MWh of solar electricity generated, one SREC is issued to the owner of the plant.
- For several years ahead, the government sets targets for solar power consumption.
- All LSEs, primarily utilities, must meet their requirement by submitting sufficient SRECs each year. Otherwise, they need to pay a fixed penalty (or SACP) for each MWh they fall below the target. They are free to generate SRECs themselves or to buy from other SREC generators.
- Finally, SRECs can be banked and used for a few years in the future. In the current NJ SREC market, SRECs can be used for four more years in addition to their production year.

<table>
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<tbody>
<tr>
<td>Target (% supply)</td>
<td>2.05%</td>
<td>2.45%</td>
<td>2.75%</td>
<td>3.00%</td>
<td>3.20%</td>
<td>3.29%</td>
<td>3.38%</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Target (1000s MWh)</td>
<td>442</td>
<td>596</td>
<td>1,708</td>
<td>2,072</td>
<td>2,360</td>
<td>2,614</td>
<td>2,830</td>
<td>2,953</td>
<td>3,079</td>
</tr>
<tr>
<td>SACP</td>
<td>$658</td>
<td>$641</td>
<td>$339</td>
<td>$331</td>
<td>$323</td>
<td>$315</td>
<td>$308</td>
<td>$300</td>
<td>$293</td>
</tr>
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Table 1. The current requirement and penalty levels (last changed in 2012)
Figure 1a shows historical SREC prices in NJ between 2007 and 2016, while Figure 1b shows generation levels, and total banked supply relative to annual targets. Shortly after its introduction, the NJ SREC market sustained very high prices close to its SACP level, as the market failed to meet the targets. More recently, the market was characterised by oversupply in 2012-13, leading to low prices, less new solar generation and a rule change to increase the requirement, before finally swinging back towards undersupply very recently. Ohio and Pennsylvania SREC markets have both also witnessed price drops from above $300 to under $50 within 18 month periods. Many argue that a market with such volatile prices is a risky environment for investors, thus decreasing competition and increasing cost of generation (e.g. [11]).

To reduce the volatility of SREC prices and thereby reduce the risk of solar investments, several rule changes have been introduced in the NJ SREC market. For example, higher SACP levels and the possibility of banking (for two years) were introduced in 2008. In 2012, the banking horizon was extended to four years, along with increases to the targets. Frequent changes in the market mechanism suggest that these policy adjustments have not been a long-term solution and that market design has some room for improvement. Various possible remedies are discussed by [11], including price floors, long-term contracts and increased banking years. These authors were also the first to suggest the use of a downward sloping demand curve in this context. However they do not provide details of their proposal’s implementation or any substantial analysis. Moreover their approach differs from ours in using an exponential SACP curve that never reaches zero, thus removing any possibility of full compliance.

3. ADAPT: A Price-stabilizing Compliance Policy

In this section, we introduce a new class of regulatory policies for computing alternative compliance penalties that allows regulators to moderate or avoid excess price volatility. We provide a description and rigorous analysis of the ADAPT market design in the context of SREC markets,
Figure 2. Price formation for two submission scenarios $x_1$ and $x_2$ under ADAPT and the cliff policy. The hashed areas represent total penalty payment in each case.

but its application could be extended to other environmental markets, such as cap-and-trade markets for emissions.

The standard compliance policy used in New Jersey and elsewhere looks like a cliff (dashed line in Figure 2), where the full SACP is imposed per MWh if usage is less than the target, dropping to zero if usage meets or exceeds the target. The first distinguishing feature of ADAPT is to replace the cliff with a downward sloping function (solid line in Figure 2), thus diminishing the large uncertainty in penalty payments that naturally arises with a cliff-style target policy.

In Figure 2, $x_1$ and $x_2$ represent two scenarios of SREC submissions, one on each side of the requirement. Resulting penalty levels $p_1$ and $p_2$ are vastly different, illustrating how small changes in generation can produce high price volatility. On the other hand, with the sloped SACP function, the same submissions $x_1$ and $x_2$ result in penalties $p'_1$ and $p'_2$ that are much closer together, providing some initial intuition as to why ADAPT produces more stable prices. Furthermore, when transitioning to a new energy year, the probability of meeting a target may drop sharply from high to low due to the chosen requirement schedule. The sloped SACP function can mitigate the price impact of this problem by avoiding the binary nature of the cliff policy. Nonetheless, long-term imbalances between supply and demand may still develop, and therefore an additional tunable policy feature may also be incorporated to automatically redefine next year’s requirement level, as we shall elaborate below.

The hashed gray area in Figure 2 represents total penalty payment in the current mechanism for $x_1$, while total penalty payment for $x_2$ is zero. Note that the full SREC requirement under the sloped mechanism (i.e., the right end of the sloped section) is more than the requirement of the current mechanism and so the penalty is paid for a higher number of SRECs (but a smaller penalty value for each unit). The hashed red and blue areas show the total penalty payment under the
sloped mechanism for $x_1$ and $x_2$ respectively. The intuition behind this alternative penalty regime is that in the sloped region each SREC short of the full requirement should be penalized gradually more and more until ADAPT finally starts to penalize each one at the full SACP. This construction allows us to interpret the SACP function as a marginal demand curve, for which a total penalty equal to the area under the curve must be paid.

The rules of the proposed ADAPT market can be summarized as follows.

- As usual, one SREC is issued per MWh to solar power generators.
- The regulator sets SREC requirement levels for several years in the future. However, the requirement levels can be automatically adapted to generation levels according to the market performance in the last year. For example, in case of a surplus (shortage) in the last year, requirements may be increased (decreased) according to a predefined formula.
- All Load Serving Entities (LSEs) must meet their requirement by submitting sufficient SRECs each year, or else pay a penalty for each MWh they fall short. Penalties, however, are calculated based on a sloped SACP function as in Figure 2; the more SRECs submitted, the lower the penalty value per SREC (assuming being in the sloped region of the function).
- A generator or LSE can bank SRECs to the following year, effectively increasing their penalty now and thus raising the value of the SRECs being submitted. This allows SREC holders to more precisely balance the value of SRECs in the future against the price they receive now, but only within a specified range (due to the limited lifetime of each SREC).

**Example 1.** Assume that the sloped SACP function is defined as represented in Figure 3 (the left plot) and $\lambda = 0.1$. Let $t = 14$ and 15 represent the compliance times of EY2014 and EY2015 respectively. According to the values given in Table 1, the full requirement of the sloped mechanism
(the right end of the sloped area) for EY2014 will be equal to
\[(1 + \lambda)R_{14} = 1,878,724.\]

Also the maximum (but not the effective) penalty \(P_{14}\) and \(P_{15}\) is equal to the current SACP levels \$339 and \$331 respectively. Now assume that a total of \(b_{14} = 2,000,000\) banked SRECs are available before the compliance time of EY2014 \(t = 14\). Assume that all market participants collectively submit \(x_t = 1,800,000\) SRECs to the regulators, and the remaining SRECs are banked for the future. According to the sloped SACP function, for this aggregate amount of submission, the SACP is equal to \$78. This means market participants are obliged to pay a total amount of \(0.5 \times 78 \times 78,724\) dollars. The remaining SRECs are banked because their expected future price is higher than or equal to the penalty of \$78. Note that in practice SACPs paid would be linked to individual agents’ decisions and indeed each LSE faces its own individual requirement, but the existence of the market to allow trading of SRECs up until compliance time should ensure that all parties ultimately choose to pay the same penalty.

Here, total available SRECs at \(t = 14\) exceeds the target \(R_{14} = 1,707,931\). Let \(s_t\) represent this surplus (or shortage if negative) from the last compliance time. In this case,
\[s_t = b_{14} - R_{14} = 292,069, \quad t \in (14, 15].\]
In an adaptive requirement scheme, we increase the requirement of the following year by a portion of \(s_t\) (as shown in the right plot of Figure 3). For example, for \(\alpha = 0.5\), we obtain:
\[R_{15} = \tilde{R}_{15} + \alpha s_{15} = 2,071,803 + 0.5 \times 292,069 = 2,217,838,\]
where \(\tilde{R}_{15}\) is equal to the already announced requirement for EY2015 (from table 1). Note that in the previous period we used \(R_{14} = \tilde{R}_{14}\), effectively assuming that \(s_{14} = 0\).

4. Mathematical Model

We now develop a mathematical model of this mechanism to investigate the effects of the sloped SACP function and adaptive requirements as well as other policy variations (and their combinations), such as number of banking years. We use the following notation.

Indices \((t, y)\): We index time by \(t\), and energy or vintage year by \(y\). In our implementation of the model, the smallest time step is assumed to be a period of one month (i.e. \(\Delta t = \frac{1}{12}\)), matching the observation frequency of NJ generation data. Each energy year \(y \in \mathbb{N}\) is associated with the time interval \((y - 1, y]\), while \(t = y\) determines the compliance time of energy year \(y\). For example, time \(t = 6\) corresponds to the end of energy year 2006 (May 31 2006). We use notation \((p_{t,y})_y\), \((b_{t,y})_y\) and \((x_{t,y})_y\) to represent vectors containing different SREC vintages.

Prices \((p_{t,y})_y\): The market price at time \(t\) of an SREC of vintage year \(y\), which is endogenously determined via our dynamic programming approach, and is a function of the state variable.
Parameters \((T, \tau, \lambda, \alpha, \tilde{R}_y, P_y, r)\):

- \(T\): The planning horizon or scheduled length of market existence (could also be \(\infty\)).
- \(\tau\): The maximum number of years (compliance times) that an SREC can be banked.
- \(\lambda\) \((0 \leq \lambda \leq 1)\): The parameter determining the shape and slope of the SACP function (see figure 3).
  If \(\lambda = 0\), we obtain the current cliff policy.
- \(\alpha\) \((0 \leq \alpha \leq 1)\): The parameter representing the portion of last year’s surplus (shortage) to be added to (deducted from) the base requirement. If \(\alpha = 0\), this mechanism disappears.
- \(\tilde{R}_y\): Number of SRECs required for energy year \(y\), determined by regulators in advance. This, however, is not the effective requirement \(R_y\), updated according to market performance.
- \(P_y\): Maximum penalty per MWh for energy year \(y\), set by regulators in advance.
- \(r\): Interest rate.

State variables: The state variable \(S_t = ((b_{t,y})_y, \hat{g}_t, s_t)\) is defined as follows.

- \((b_{t,y})_y\): Total accumulated or banked SRECs from different vintages at time \(t\). The total banked SRECs available from all vintages is represented by \(\tilde{b}_t = \sum_{y=\max\{1, t-\tau\}}^{\infty} b_{t,y}\).
- \(\hat{g}_t\): The installed capacity of SREC generation at time \(t\).
- \(s_t\): The surplus (or shortage) of SRECs from the last compliance time \((s_t = \tilde{b}_{t-1} - \tilde{R}_{t-1})\). Note that \(s_t\) cannot always be obtained from \((b_{t,y})_y\), e.g., in the case of a shortage \((s_t \leq 0)\).

Decision variables \((x_{t,y})_y\): The number of SRECs to be submitted at compliance time \(t\) from different vintages. We denote the total submitted SRECs at time \(t\) by \(\bar{x}_t = \sum_{y=\max\{1, t-\tau\}}^{\infty} x_{t,y}\). Decisions will be made by a policy \(\pi\) using a function \(X^\pi_t(S_t)\) to be determined later.

Exogenous information processes \((\varepsilon_t)\): The random variable indicative of noise in generation. Let \(\omega \in \Omega\) be a sample path for \((\varepsilon_1, \ldots, \varepsilon_T)\). Let \(\mathcal{F}_t = \sigma(\varepsilon_1, \ldots, \varepsilon_T)\) be the sigma-algebra on \(\Omega\), equipped with the filtration \(\{\mathcal{F}_t\}_{t \geq 1}\), and let \(Q\) be the risk-neutral probability measure on \((\Omega, \mathcal{F})\), giving us a filtered probability space \((\Omega, \mathcal{F}, \{\mathcal{F}_t\}_{t \geq 1}, Q)\). We assume throughout that any variable indexed by \(t\) is \(\mathcal{F}_t\)-measurable, and that all risk premiums are zero.

Other functions \((R_t(s_t), f^\text{SACP}_t(\bar{x}_t))\):

- \(R_t(s_t)\): The number of SRECs required by the regulation at time \(t \in \mathbb{N}\), defined as
  \[
  R_t(s_t) = \tilde{R}_t + \alpha s_t
  \]
- \(f^\text{SACP}_t(\bar{x}_t)\): The SACP function, determining the marginal penalty price for any value of total SREC submission \(\bar{x}_t\) at time \(t\). This is the (artificial) inverse demand function of \(SACP_t\) from \(x_t\), updated according to market performance and at any compliance time \(t \in \mathbb{N}\) it can be represented by \((\lambda > 0)\):
  \[
  f^\text{SACP}_t(\bar{x}_t) = \max\left(0, \min\left[P_t, P_t - \frac{P_t}{2\lambda R_t}(\bar{x}_t - (1 - \lambda)R_t)\right]\right)
  \]
  For other time periods \(t \notin \mathbb{N}\), we define \(f^\text{SACP}_t(\bar{x}_t) = 0\) and \(R_t(s_t) = 0\), to provide a more general model without the need to discriminate between compliance and non-compliance times.
Transition function \((S^M)\): We represent this generically using \(S_{t+\Delta t} = S^M(S_t, (x_{t,y})_y, W_{t+\Delta t})\). Variables \(\hat{g}_{t+\Delta t}\) and \(b_{t+\Delta t}\) both depend on the SREC generation model, for which we follow the approach of [8], supported by empirical evidence from New Jersey. The model consists of annual and semi-annual seasonality, noise, and a price-dependent expected generation growth rate to capture feedback onto new supply from current SREC prices. (More generally, [8] allow for dependence on lagged SREC prices or historical average prices to reflect solar construction time, but for simplicity and dimension reduction we use only current newest vintage prices.) The instantaneous generation rate \(g_t\) at each \(t\) is given by

\[
(1) \quad g_t(p, \varepsilon_t) = \hat{g}_t \exp \left( a_1 \sin(4\pi t) + a_2 \cos(4\pi t) + a_3 \sin(2\pi t) + a_4 \cos(2\pi t) + \varepsilon_t \right).
\]

while the related installed generation \(\hat{g}_t\) evolves according to

\[
(2) \quad \hat{g}_{t+\Delta t} = \hat{g}_t \exp(a_5 \Delta t + a_6 p_t, \lceil t \rceil \Delta t).
\]

The number of banked SRECs \(b_{t+\Delta t,y}\) can be obtained from

\[
\begin{align*}
0 & \quad y < [t + \Delta t] - \tau, \\
|b_{t,y} - x_{t,y}| [t + \Delta t] - \tau & \quad y < [t + \Delta t], \\
b_{t,y} + g_t \Delta t - x_{t,y} & \quad y = [t + \Delta t], \\
0 & \quad y > [t + \Delta t].
\end{align*}
\]

The four cases above correspond respectively to (i) vintages fully expired; (ii) older vintages still trading; (iii) the most recent vintage; and (iv) vintages yet to exist. Between compliance dates \(b_{t,y}\) only changes for the current vintage as new SRECs are generated, while at compliance dates total submissions for all existing vintages must be accounted for. Based on the definition of the SACP function, no SRECs are submitted at non-compliance times \((x_{t,y} = 0 \text{ if } t \notin N)\).

Finally, surplus can be updated from

\[
|s_{t+\Delta t} = \begin{cases} 
\bar{b}_t - \bar{R}_t & t \in \mathbb{N}, \\
\bar{s}_t & t \notin \mathbb{N}.
\end{cases}
\]

This is only a surplus (or shortage) relative to the base requirement schedule \(\bar{R}_t\), set in advance. Hence it is possible that \(s_t > 0\) but the market is short of the adjusted target. i.e. \(\bar{R}_t < \bar{b}_t < R_t\).

Objective function: At each time step, the collective behaviour of a competitive market maximizes social welfare or equivalently here, minimizes total cost of compliance. Since the definition of social welfare relies on integrating under an artificial demand function, we favour the compliance cost minimization as the more natural approach, linking clearly to the individual banking decisions of LSEs. Letting \(C(S_t, x_t)\) denote the compliance cost function at time \(t\), then we have

\[
C(S_t, \bar{x}_t) = \int_{\bar{x}_t(S_t)}^{\infty} f^{\text{SACP}}_t(u) du.
\]

In order to obtain cleaner equations, we use \(F_t(\bar{x}_t)\) to represent \(\int_{\bar{x}_t}^{\infty} f^{\text{SACP}}_t(u) du\). Let \(\Pi\) be the set of all policies \(\pi\) i.e. functions that match each state \(S_t\) to a decision \(X^\pi_t(S_t)\). The total cost of
future compliance $V_t$, under the best policy $\pi \in \Pi$, therefore satisfies

$$V_t(S_t) = \min_{\pi \in \Pi} \mathbb{E}_t \sum_{t'=t}^T e^{-r(t'-t)} F_{t'}(X_{t'}^\pi(S_{t'})),$$

where $e^{-r(t'-t)}$ is the discount factor, and $\mathbb{E}_t$ is a time $t$ conditional expectation under $Q$. We will use the notation $\bar{x}_t^*$ for optimal total submission strategy (sum across vintages).

Note that we are assuming that the competitive equilibrium can be modelled directly via the optimal decision of a single representative agent minimizing total costs. Much theory exists relating such a decision to that of individual agents able to trade with each other in the market, for example in the carbon market setting of [7] or [13], so we choose to avoid adding an additional lengthy technical justification of this link here. Furthermore, we comment that an extension of the model to incorporate other costs and decisions is possible. While the marginal cost of SREC generation from existing solar installations is essentially zero, the upfront cost of installing new solar could of course be modelled, effectively adding an additional decision variable (and greater computational burden) to the problem. Instead, we choose to focus solely on the submission (or banking) decision, and assume the construction of new solar follows (2), a simple price-feedback relationship justified by empirical evidence in [8]. Furthermore, one might argue that some measure of risk-aversion is important for both the banking and new investment decisions (given our premise that excess volatility discourages investment), but we choose to focus solely on the dynamic programming approach and to gain insight into the key implications of the ADAPT policy proposal.

5. Model Properties

Through a series of theorems and propositions, we now derive several properties of the model introduced in the previous section that help us in analysing the collective market behaviour and solving the associated dynamic programming problem. We assume throughout that future penalties $P_y$ are non-increasing in time, as has been the case (and typically decreasing) in all SREC markets to our knowledge and through all regulation changes in the NJ SREC market. (Note that the jump upwards in 2008 in NJ was instead a sudden rule change and shift in the entire penalty schedule.) We also assume $\lambda > 0$, since the optimal policy under the classical market design is trivial (with non-increasing penalties), namely $\bar{x}_t^* = \min(\bar{b}_t, R_t)$, submit all you can up to the ‘cliff’ and bank everything beyond.

The first helpful lemma reduces the dimensionality of the decision variable, by mapping the optimal total submission $\bar{x}_t^*$ onto the submission decision for individual vintages, $x_{t,y}^*$:

**Lemma 1.** If the optimal number of submitted SRECs at time $t$, $\bar{x}_t^*$, is known, the optimal number submitted from the different existing non-expired vintages at time $t$ is given by

$$x_{t,y}^* = \min\{b_{t,y}, \bar{x}_t^* - \sum_{u=[t]-\tau}^{y-1} x_{t,u}^*\}$$
for any \( y \) such that \( \lceil t \rceil - \tau \leq y \leq \lceil t \rceil \), and zero otherwise.

Proof. On one hand, all (non-expired) SREC vintages have the same impact on reducing the cost function \( F_t(x_t) \) at each time. On the other hand, the newer SRECs can be used further in the future to minimize \( \mathbb{E}_t \sum_{a} e^{-r (a-t)} F_a(\bar{x}^a_t) \). Therefore, for any \( y \), if \( x^*_{t,y} < b_{t,y} \), \( x^*_{t,y+1} = 0 \) (i.e. the older SRECs must be submitted first). This means that the oldest SRECs must all be submitted \((x^*_{t,[t]-\tau} = b_{t,[t]-\tau})\) unless \( b_{t,[t]-\tau} > \bar{x}^*_{t} \). Therefore, \( x^*_{t,[t]-\tau} = \min \{ b_{t,[t]-\tau}, \bar{x}^*_{t} \} \). Similarly, the second oldest SRECs must all be submitted if this does not exceed the total remaining SRECs from the optimal submission \( \bar{x}^*_{t} \), or \( x^*_{t,[t]-\tau+1} = \min \{ b_{t,[t]-\tau+1}, \bar{x}^*_{t} - x^*_{t,[t]-\tau} \} \). Extending this to other vintages \( \lceil t \rceil - \tau \leq y \leq \lceil t \rceil \), we obtain \( x^*_{t,y} = \min \{ b_{t,y}, \bar{x}^*_{t} - \sum_{u=\lceil t \rceil - \tau}^{y-1} x^*_{t,u} \} \). Expired or not yet produced SRECs of course cannot be submitted.

The simple and intuitive result above can be described as a ‘first in first out’ (FIFO) warehousing rule, as would apply to any perishable commodity. While it crucially allows us to reduce the decision variable to a scalar \( \bar{x}_t \), the objective function (total discounted expected future costs), is still a function of the full vector \((b_{t,y})_y\) contained in \( S_t \), which can lead to cases where different vintage SRECs have different values. Despite this warehousing concept, an SREC is a financial certificate, and does not have any storage or delivery costs or other constraints related to physical commodities. As such, standard no arbitrage arguments from finance theory apply, and SRECs must satisfy the martingale condition under the risk-neutral measure (at all times including compliance dates, as long as some are banked). At a compliance date non-expired SRECs must be worth at least as much as the current penalty rate paid per SREC, and at optimality would be banked if discounted expected future prices are higher. Expired SRECs have no value. Thus, the price of SRECs of vintage \( y \) at time \( t \) satisfies

\[
(4) \quad p_{t,y} = \max \{ f^\text{SACP}_t(\bar{x}^*_{t}), e^{-r \Delta t} \mathbb{E}_t \{ p_{t+\Delta t,y} \} \}, \quad \text{for } t \leq y + \tau,
\]

and \( p_{t,y} = 0 \) for \( t > y + \tau \). Recall that \( f^\text{SACP}_t(x_t) = 0 \) for non-compliance times (\( t \notin \mathbb{N} \)).

We note that the pricing equation closely resembles that of an American (or Bermudan) option, which is very natural since SRECs are used (‘exercised’) at predetermined compliance dates, or else expire. SREC prices in a competitive equilibrium can also be understood as the marginal benefit of having an additional unit of that vintage (or the marginal cost of having one less). Unlike for the discontinuous cliff policy, in the ADAPT policy (with \( \lambda > 0 \)) we can equivalently use the derivative of the total cost function, as described by the proposition below.

**Proposition 1.** The price of SRECs of vintage \( y \) at time \( t \) can be written as

\[
(5) \quad p_{t,y} = \begin{cases} 
-\partial V_t(S_t), & t \leq y + \tau, \\
0, & t > y + \tau.
\end{cases}
\]

Proof. Writing the objective function in (3) as

\[
V_t(S_t) = \min_{\pi \in \Pi} \left\{ F_t(X^\pi_t(S_t)) + e^{-r \Delta t} \mathbb{E}_t \sum_{t'=t+\Delta t}^{T} e^{-r(t'-(t+\Delta t))} F_{t'}(X^\pi_{t'}(S_{t'})) \right\},
\]
we can see that an additional SREC will either be used to reduce the first term or the second (depending on which is optimal). Therefore, differentiating with respect to \( b_{t,y} \) (and noting that vintage \( y \) is worthless after \( y + \tau \)) returns precisely the price definition equation in (4). \( \square \)

Next, to understand the optimal policy for \( \bar{x}^*_t \), we first need to prove the following lemmas. We assume \( \tau > 0 \) throughout, since otherwise there is no banking decision to make. The first lemma describes the required price for any SREC vintages used for compliance.

**Lemma 2.** Let \( \bar{x}^*_t = X^*_t(S_t) \) represent the optimal policy at any compliance time \( t \in \mathbb{N} \). For any vintage \( y \) such that \( x^*_{t,y} > 0 \), we must have \( p_{t,y} = f^{SACP}(\bar{x}^*_t) \).

**Proof.** From (4), we know that \( p_{t,y} \geq f^{SACP}(\bar{x}^*_t) \). Suppose that \( p_{t,y} > f^{SACP}(\bar{x}^*_t) \). Since we have \( p_{t,y} = -\frac{\partial V(S_t)}{\partial b_{t,y}} \) by Proposition 1, we know an additional SREC (of vintage \( y \)) can reduce our objective function by \( \partial b_{t,y} \). Therefore it cannot be optimal to have submitted an SREC at SACP level \( f^{SACP}(\bar{x}^*_t) \), hence contradicting \( x^*_{t,y} > 0 \). (Intuitively, if the market price is higher than the SACP, it’s better to sell the SREC in the market and pay a slightly higher penalty than to submit it for compliance. This is not always true for the discontinuous cliff policy.) \( \square \)

The next lemma applies between compliance dates and for SREC vintages not submitted.

**Lemma 3.** For any vintage \( y \) such that \( x^*_{t,y} = 0 \), we must have \( p_{t,y} = e^{-r\Delta t}E_t[p_{t+\Delta t,y}] \).

**Proof.** The total future compliance cost function can be written

\[
V_t(S_t) = \min_{\pi \in \Pi} \left\{ F_t(X_t^*(S_t)) + e^{-r\Delta t}E_t \sum_{t' = t+\Delta t}^T e^{-r(t'-t)} F_{t'}(X_{t'}^*(S_{t'})) \right\}
\]

Since \( x^*_{t,y} = 0 \), we know that \( F_t(X_t^*(S_t)) \) is not a function of \( b_{t,y} \), and hence

\[
\frac{\partial V_t(S_t)}{\partial b_{t,y}} = e^{-r\Delta t} \frac{\partial}{\partial b_{t,y}} \min_{\pi \in \Pi} E_t \sum_{t' = t+\Delta t}^T e^{-r(t'-t)} F_{t'}(X_{t'}^*(S_{t'})) = e^{-r\Delta t}E_t \left[ \frac{\partial V_{t+\Delta t}(S_{t+\Delta t})}{\partial b_{t,y}} \right]
\]

Thus, by Proposition 1, \( p_{t,y} = e^{-r\Delta t}E_t [p_{t+\Delta t,y}] \). \( \square \)

Finally, consider the case of an SREC vintage reaching the end of its usable life.

**Lemma 4.** At vintage \( y \)’s expiry (at \( t = y + \tau \)), if \( b_{t,y} > 0 \), then \( x^*_{t,y} = b_{t,y} \) and \( p_{t,y} = f^{SACP}(\bar{x}^*_t) \).

**Proof.** By definition, \( p_{t+\Delta t,y} = 0 \) at \( t = y + \tau \), so any remaining SRECs will expire worthless if not used at \( t \). Since \( F \) is strictly non-increasing in \( \bar{x} \), submitting additional SRECs can only reduce one’s costs, so \( x^*_{t,y} = b_{t,y} \) must be optimal (noting however that any submission beyond \((1 + \lambda)R_t \) would no longer have any impact on the objective function). \( \square \)

The result above clearly implies that at any \( t \in \mathbb{N} \), the optimal submission decision lies in the range \( \bar{x}^*_t \in [b_{t,t-\tau}, \bar{b}_t] \). We can now prove the main theorem describing how price dynamics are linked to submission and banking decisions, starting directly from the optimization problem.

**Theorem 1.** Let \( \bar{x}^*_t = X^*_t(S_t) \) represent the optimal policy at any compliance time \( t \in \mathbb{N} \). Then

\[
f^{\text{SACP}}(\bar{x}^*_t) = \max \left( f^{\text{SACP}}(\bar{b}_t), \min \left( f^{\text{SACP}}(b_{t,t-\tau}), e^{-r\Delta t}E_t[p_{t+\Delta t,y}] \right) \right),
\]

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where $\tilde{y} = \max\{y : x_{t,y}^* > 0\}$.

**Proof.** Throughout this proof we use the notation $b_t$, $x_t$ and $g_t$ to denote the vectors containing all vintages (noting that for $g_t$ only the current vintage is non-zero).

\begin{equation}
V_t(b_t, \cdot) = \min_{x \in \Pi} \mathbb{E}_t \sum_{t' = t + \Delta t}^T e^{-r(t' - (t + \Delta t))} F_t'(X_t^*(S_{t'}))
\end{equation}

\begin{equation}
= \min_{\bar{x}_t \in [b_{t,t-\tau}, b_t]} \left( F_t(\bar{x}_t) + e^{-r\Delta t} \mathbb{E}_t [V_{t+\Delta t}(b_t - x_t + g_t \Delta t, \cdot)] \right).
\end{equation}

Now we look at the Karush-Kuhn-Tucker (KKT) conditions of this constrained maximization (with two constraints, so we introduce KKT multipliers $\mu_1$ and $\mu_2$). Since $\frac{\partial f(\bar{x}_t)}{\partial x_t} = -f_{SACP}(\bar{x}_t)$, the stationarity condition (with optimal solution denoted by $\bar{x}_t^*$) gives:

$$-f_{SACP}(\bar{x}_t^*) + e^{-r\Delta t} \frac{\partial}{\partial \bar{x}_t} \mathbb{E}_t [V_{t+\Delta t}(b_t - x_t + g_t \Delta t, \cdot)]|_{\bar{x}_t = \bar{x}_t^*} = \mu_1 - \mu_2$$

while the complementary slackness conditions give

$$\mu_1 (\bar{x}_t^* - \bar{b}_t) = 0 \quad \text{and} \quad \mu_2 (b_{t,t-\tau} - \bar{x}_t^*) = 0.$$

Also, $b_{t,t-\tau} \leq \bar{x}_t^* \leq \bar{b}_t$ and $\mu_1, \mu_2 \geq 0$. Thus if $b_{t,t-\tau} < \bar{x}_t^* < \bar{b}_t$, then $\mu_1 = \mu_2 = 0$, so

$$-f_{SACP}(\bar{x}_t^*) + e^{-r\Delta t} \frac{\partial}{\partial \bar{x}_t} \mathbb{E}_t [V_{t+\Delta t}(b_t - x_t + g_t \Delta t, \cdot)]|_{\bar{x}_t = \bar{x}_t^*} = 0$$

or equivalently, since Lemma 1 tells us that derivatives with respect to $\bar{x}_t$ correspond to derivatives with respect to the most recent vintage used for submission,

$$f_{SACP}(\bar{x}_t^*) = -e^{-r\Delta t} \mathbb{E}_t \left[ \frac{\partial}{\partial \bar{x}_t} V_{t+\Delta t}(b_t - x_t + g_t \Delta t, \cdot) \right]$$

where $\tilde{y} = \max\{y : x_{t,y}^* > 0\}$. Thus, if $b_{t,t-\tau} < \bar{x}_t^* < \bar{b}_t$, then using Proposition 1 and Lemma 2 for any submitted vintage $y$ (i.e. such that $x_{t,y}^* > 0$),

$$p_{t,y} = e^{-r\Delta t} \mathbb{E}_t [p_{t+\Delta t, \tilde{y}}].$$

Overall, for any $t \in \mathbb{N}$, we must have

$$(\bar{x}_t^* - \bar{b}_t)(\bar{x}_t^* - b_{t,t-\tau})(p_{t,y} - e^{-r\Delta t} \mathbb{E}_t [p_{t+\Delta t, \tilde{y}}]) = 0$$

and since $f_{SACP}(\cdot)$ is a strictly non-increasing function, we can conclude that

$$f_{SACP}(\bar{x}_t^*) = \max \left( f_{SACP}(\bar{b}_t), \min \left( f_{SACP}(b_{t,t-\tau}), e^{-r\Delta t} \mathbb{E}_t \left[ f_{SACP}(\bar{x}_{t+1}) \right] \right) \right).$$

\[ \square \]

We can also link the optimal policy $\bar{x}_t^*$ with that of the following compliance date, $\bar{x}_{t+1}^*$:

**Corollary 1.** Let $\bar{x}_t^* = X_t^*(S_t)$ represent the optimal policy at any $t \in \mathbb{N}$. Then,

$$f_{SACP}(\bar{x}_t^*) = \max \left( f_{SACP}(\bar{b}_t), \min \left( f_{SACP}(b_{t,t-\tau}), e^{-r\Delta t} \mathbb{E}_t \left[ f_{SACP}(\bar{x}_{t+1}) \right] \right) \right).$$

**Proof.** To extend the theorem above to the corolla, we need to show that

$$e^{-r\Delta t} \mathbb{E}_t [p_{t+\Delta t, \tilde{y}}] = e^{-r\Delta t} \mathbb{E}_t \left[ f_{SACP}(\bar{x}_{t+1}) \right],$$
where \( \tilde{y} = \max\{y : x_{t,y}^* > 0\} \). First note that \( e^{-\gamma\Delta t}E_t[p_{t+\Delta t,y}] = e^{-\gamma E_t[p_{t+1,y}]} \) by Lemma 3 since \( \bar{x}_t^* = 0 \) for \( t \notin \mathbb{N} \) (i.e. the martingale condition). Now there are two cases to consider:

(i) \( x_{t,\tilde{y}}^* < b_t \tilde{y} \): Since \( R_{t+1} > 0 \) and \( P_{t+1} \geq P_u \forall u > t + 1 \) by assumption, we can deduce that \( x_{t+1,\bar{y}} > 0 \) (i.e. at least some of the remaining SRECs of vintage \( \bar{y} \) will be used for compliance), as we know the first of these will reduce the total cost function by \( P_{t+1} \), a larger number than possible in any future year. Thus, by Lemma 1, \( p_{t+1,\bar{y}} = f^{SACP}(x_{t+1}^*) \).

(ii) \( x_{t,\tilde{y}}^* = b_t \tilde{y} \): As no SRECs of vintage \( \tilde{y} \) remain beyond time \( t \), \( p_{t+1,\tilde{y}} \) is a hypothetical price in the event of suboptimal banking. Nonetheless, we can still claim that \( p_{t+1,\bar{y}} = f^{SACP}(x_{t+1}^*) \) must hold by Lemma 1 in such a case. \( \square \)

The theorem and corollary above describe the three possible cases at a submission time \( t \in \mathbb{N} \): undersupply, (severe) oversupply, and normal conditions. In the first case, \( \bar{x}_t^* = \tilde{b}_t \) (since \( f^{SACP}(\bar{x}_t^*) = f^{SACP}(\tilde{b}_t) \)), so all available SRECs are submitted in order to reduce penalties as much as possible. In the second case, only the oldest vintage is submitted \( (x_{t,y}^* = b_t y) \) in order to avoid SRECs expiring worthless. Given \( \tau = 4 \) as in New Jersey, this oversupply case is particularly extreme and unlikely, as it would imply that all five vintages still exist in the market, and moreover that \( b_{t,t-4} \) is a large enough number that it would not be optimal to use any of \( b_{t,t-3} \). Finally, the most typical case of \( b_{t,t-\tau} < \bar{x}^* < \tilde{b}_t \) is between these extremes, with some SRECs submitted and others saved in order to balance with their expected future value.

In all three cases, Lemma 2 tells us that \( p_{t,y} = f^{SACP}(\bar{x}_t^*) \) for all vintages \( y \) with \( x_{t,y}^* > 0 \). In the undersupply case \( (p_{t,y} = f^{SACP}(\tilde{b}_t) \) for all vintages), all existing SRECs are submitted, so \( E_t[p_{t+\Delta t,y}] \) arguably does not exist, since none of the current vintages will trade next period. However, if (suboptimally) any SRECs remained in the market, their future price would drop. In the extreme oversupply case \( (p_{t,t-\tau} = f^{SACP}(b_{t,t-\tau}) \) for the only submitted vintage), other vintages may have higher prices given by their continuation value, as in Corollary 1. Finally, in the common case, all vintages \( y \geq \tilde{y} \) will typically have prices equal to \( e^{-\gamma\Delta t}E_t[p_{t+\Delta t,y}] \), the continuation value of the newest vintage submitted, but it is theoretically possible that other vintages \( y > \tilde{y} \) can exist with higher prices. We now derive another representation of the price \( p_{t,y} \) that can help provide further intuition, showing that an SREC’s value is the maximum over its compliance cost impact at all future exercise opportunities for which \( x_{t,y}^* > 0 \) optimally:

**Proposition 2.** Let \( \bar{x}_t^* = X_t^*(S_t) \) represent the optimal policy at any compliance time \( t \in \mathbb{N} \). The price of SRECs of vintage \( y \) at time \( t \) can be written

\[
p_{t,y} = \max_{u \in \{t\},[t]+1,\ldots,[t]+\tau} E_t\left[e^{-\gamma(u-t)}f^{SACP}(\bar{x}_u^*)1_{\{x_{u,y}^* > 0\}}\right].
\]

**Proof.** For \( t \in (y+\tau-1, y+\tau] \), we have no further banking decisions remaining for vintage \( y \), and from Lemmas 3 and 4, we must have

\[
p_{t,y} = e^{-\gamma(y+\tau-t)}E_t\left[f^{SACP}(\bar{x}_{y+\tau}^*)\right].
\]
At $t = y + \tau - 1$, using Corollary 1 and Lemmas 2 and 3, we then have:

$$p_{t,y} = \begin{cases} f^{SACP}(\bar{x}_{t}^{*}), & \text{if } x_{t,y}^{*} > 0 \\ e^{-r\tau}E_{t} \left[ f^{SACP}(\bar{x}_{y+\tau}^{*}) \right] \geq f^{SACP}(\bar{x}_{t}^{*}), & \text{if } x_{t,y}^{*} = 0. \end{cases}$$

By repeating this argument iteratively back in time we obtain the result. \qed

The possibility of different prices for different vintages introduces a high dimensional state variable. However, investigations of realistic scenarios reveal that it is very likely for all vintages to have the same price, allowing us to approximate the problem by a much lower dimensional one with $\bar{b}_{t}$ as state variable. Using Proposition 2, we can show that for any neighbouring vintages $y$ and $y + 1$, $p_{t,y} < p_{t,y+1}$ is possible if and only if there exists some positive probability that we have an excess of vintage $y$ SRECs to dispose of at their expiry.

**Theorem 2.** Let $\bar{x}_{t}^{*} = X_{t}^{*}(S_{t})$ be the optimal policy, and $Q_{t}$ the conditional probability at $t$. If

$$Q_{t}\{ \bar{x}_{u}^{*} = b_{u,u-\tau} \} = 0, \quad \forall u \in \{ [t], [t] + 1, \ldots, [t] + \tau \},$$

then all SREC vintages have equal prices at time $t$. (i.e. $p_{t,u} = p_{t,v}, \forall u, v \in \{ [t], [t] + 1, \ldots, [t] + \tau \}$).

**Proof.** Assume $Q_{t}\{ \bar{x}_{u}^{*} = b_{u,u-\tau} > 0 \} = 0, \quad \forall u \in \{ [t], [t] + 1, \ldots, [t] + \tau \}$. Now suppose (for a contradiction) that $p_{t,y} < p_{t,y+1}$ for some $y \in \{ [t] - 1, \ldots, [t] - \tau \}$, noting that $p_{t,y} > p_{t,y+1}$ is precluded by no arbitrage since newer vintages give all the benefits of older ones plus more.

From Proposition 2, we can deduce that there must exist some paths $A \in \Omega$ with $Q_{t}\{ A \} > 0$ such that for some $\tilde{u} \in \{ [t], [t] + 1, \ldots, y + \tau + 1 \}$ we have $x_{\tilde{u},y} = 0, x_{\tilde{u},y+1} > 0$ and $p_{\tilde{u},y} < p_{\tilde{u},y+1}$. However, if $\tilde{u} \leq y + \tau$ (i.e., before vintage $y$ expires), we can show a contradiction: firstly if $b_{\tilde{u},y} > 0$ for $A \in \Omega$, then $x_{\tilde{u},y} = 0, x_{\tilde{u},y+1} > 0$ contradicts Lemma 1; alternatively, if $b_{\tilde{u},y} = 0$, then the ‘hypothetical’ price $p_{\tilde{u},y} = f^{SACP}(\bar{x}_{\tilde{u}}^{*})$ still holds, which equals $p_{\tilde{u},y+1}$, again a contradiction.

This proves that no price difference can stem from the earlier compliance dates and we must have $\tilde{u} = y + \tau + 1$, for which $0 = p_{\tilde{u},y} < p_{\tilde{u},y+1}$ for paths $A \in \Omega$, since vintage $y$ has expired. However this is not necessarily sufficient to lead to $p_{t,y} < p_{t,y+1}$. We know from Lemma 4 that at time $y + \tau$, $\bar{x}_{y+\tau}^{*} \geq b_{y+\tau,y}$. Suppose that $\bar{x}_{y+\tau}^{*} > b_{y+\tau,y}$. Then by Lemma 1, $x_{y+\tau,y+1} > 0$ and $p_{y+\tau,y+1} = p_{y+\tau,y+1}$, again contradicting the assumed price difference between vintages. Therefore the only remaining possibility is that $\bar{x}_{y+\tau}^{*} = b_{y+\tau,y}$ for paths $A \in \Omega$, in which case from Corollary 1, we can have $p_{y+\tau,y} = f^{SACP}(\bar{x}_{y+\tau}^{*}) < e^{-r\tau}E_{y+\tau} \left[ f^{SACP}(\bar{x}_{y+\tau+1}^{*}) \right] = p_{y+\tau,y+1}$. This event was ruled out at the start of our proof, producing a contradiction which completes the proof. The extension of the claim from neighbouring vintages $y$ and $y + 1$ to any non-expired vintages is trivial. \qed

A simpler sufficient (far from necessary) condition for price convergence across vintages is

$$\bar{x}_{t}^{*} > \sum_{y=t-\tau}^{t-1} b_{t,y}, \quad \forall t \in \mathbb{N}$$

as it then guarantees that $x_{t,t}^{*} > 0$ (i.e., at least some of the newest vintage SRECs are submitted). Recalling Figure 1b, we note that at the peak of oversupply in the New Jersey market (2012-13),
banked certificates still remained between 40% and 50% of the following year’s requirement, sug-
gestings that the newest vintage would always be needed for compliance, easily enough to equalize
prices, even with a significantly positive $\lambda$ under ADAPT (since with non-increasing penalties it is
always optimal to submit at least $(1 - \lambda)R_t$ SRECs). Recall that the natural feedback effect in the
market naturally serves to avoid the most extreme imbalances since new generation slows during
oversupply, and accelerates during undersupply.

On the other hand, price differences between vintages are fairly common for the cliff policy (e.g.,
Figure 1a) so it is not immediately intuitive how the sloped policy eliminates such differences in
all but extreme scenarios. We provide an illustrative toy example below:

**Example 2.** Let $r = 0$. Suppose also we have no randomness in the model ($\epsilon_t = 0$), and perfect
foresight on future SREC supply. Set $\tau = 1$ so that (at most) two vintages are available at any
time. Vintage 0 expires in year 1, and vintage 1 in year 2. Requirements are $R_1 = R_2 = 10,000$, and
penalties $P_1 = P_2 = P$. The banked certificates available by the end of year 1 are

$$b_{1,0} = 8,000, \quad b_{1,1} = 6,000$$

and we know that next year we will also have some vintage 2 SRECs available:

$$b_{2,2} = 5,000$$

We consider the optimal submission decisions for year 1 and year 2 to minimize total cost, firstly
under the case of the cliff policy, and secondly for ADAPT’s sloped policy (with $\lambda = 0.1$).

1. **Cliff Policy:** In Year 1, 14,000 SRECs are available, so 10,000 can be used to meet the first
requirement, with 4,000 banked to Year 2. Since no penalty is paid, $p_{1,0} = 0$. Then only
9,000 will be available for Year 2 compliance, so $R_2$ will be missed, and thus $p_{1,1} = P$, the
penalty. The total payments for non-compliance (over the two years) are $1,000P$.

2. **ADAPT Policy ($\lambda = 0.1$):** Suppose we choose to submit $(1 + \lambda)R_1$ in Year 1 to reduce our
penalty to zero. Then we would submit 11,000 in Year 1, leaving only 8,000 for Year 2 and
a total penalty of $2,000P$ (the area $\int_{8000}^{11000} f^{SACP}(x)$). Prices are again $p_{1,0} = 0, p_{1,1} = P$
in this (suboptimal) case. Instead, the optimal policy (ignoring Year 3 and beyond) is to
spread our compliance costs between years, by submitting 9,500 SRECs each of the two
years. The two vintage prices are then equal at $p_{1,0} = p_{1,1} = 0.75P$, and the total penalty
payment each year is $1,500(0.75P)/2$, giving a combined value of $1,125P$.

While the total penalty of $1,125P$ under ADAPT is slightly higher than the $1,000P$ under the cliff
policy, it is significantly lower than the $2,000P$ under the naive policy of lowering the first year’s
penalty to zero at the expense of the second. We clearly see the incentive for market participants
to balance their banking decisions with future price expectations, and the resulting equalization of
vintage prices. Note that in a more complete example, the feedback effect should also be included
such that the future generation of SRECs ($b_{2,2}$, say) should change as current prices (linked to
current decisions) change. Similarly, with $\alpha > 0$ under ADAPT, the future requirement would also
respond to earlier decisions. However, these additional effects would not change the overall features
of the comparison being made above.

Note also that the inventory of SRECs in this simple example has more of the older vintages remaining than newer ones, an unrealistic scenario both because of Lemma 1 and because of the growth of generation in most markets. Even still, prices across vintages are equal. One would have to change the balance to \( b_{t,0} = 9,501, b_{t,1} = 4,499 \) before a price difference would emerge, because it would no longer be optimal to only submit 9,500 in year 1 (and waste one SREC).

In other words, a price difference can only emerge if the optimal submission decision \( x_t \), needed to balance today’s penalty with expected future prices, would fall below the bound \( b_{t,t-\tau} \) either this period or with some probability in a future period. In such a case, it is instead preferable to submit \( b_{t,t-\tau} \) to avoid wasting SRECs, thus bringing down the price of the expiring vintage compared to newer ones. In line with the example above, the following theorem shows that the total penalty payment is always more under the sloped market design.

**Theorem 3.** Total penalty payment of the sloped market design is always greater than or equal to that paid under the original step mechanism.

**Proof.** Let \( \bar{x}_t^* \) denote the total submitted SRECs at time \( t \in \mathbb{N} \) under the optimal policy for the ADAPT regime. Let \( F_t^{ADAPT}(\bar{x}_t) \) and \( F_t^{Cliff}(\bar{x}_t) \) represent total compliance costs at each \( t \) under each regime, for a policy \( \bar{x}_t \). Consider the two possible cases for \( \bar{x}_t^* \), for any \( t \in \mathbb{N} \):

(i) If \( \bar{x}_t^* \geq R_t \), we have

\[
F_t^{Cliff}(\bar{x}_t^*) = \int_{\bar{x}_t^*}^{\infty} f_t^{Cliff}(z)dz = 0 \leq \int_{\bar{x}_t}^{\infty} f_t^{ADAPT}(z)dz = F_t^{ADAPT}(\bar{x}_t^*).
\]

(ii) If \( 0 \leq \bar{x}_t^* \leq R_t \), we have \( \int_0^{\bar{x}_t^*} f_t^{Cliff}(z)dz \geq \int_0^{\infty} f_t^{ADAPT}(z)dz \). Since by construction the total areas under the two penalty functions are equal \( \int_0^{\infty} f_t^{Cliff}(z)dz = \int_0^{\infty} f_t^{ADAPT}(z)dz \), we conclude

\[
F_t^{Cliff}(\bar{x}_t^*) = \int_{\bar{x}_t^*}^{\infty} f_t^{Cliff}(z)dz \leq \int_{\bar{x}_t}^{\infty} f_t^{ADAPT}(z)dz = F_t^{ADAPT}(\bar{x}_t^*).
\]

Finally, let \( \bar{x}_t^* \), be the optimal policy for the step regime. From (3), for any state \( S_t \),

\[
V_t^{Cliff}(S_t, \bar{x}_t^*) \leq V_t^{Cliff}(S_t, \tilde{x}_t^*),
\]

where \( V_t^{Cliff}(S_t, x_t) \) or \( V_t^{ADAPT}(S_t, x_t) \) represent the total future cost function under a given regime when following strategy \( x_t \) from state \( S_t \) onwards, where \( x_t \) may or may not be optimal. Noting from the two cases above that for any \( t \), \( F_t^{Cliff}(\bar{x}_t^*) \leq F_t^{ADAPT}(\bar{x}_t^*) \), we have as required,

\[
V_t^{Cliff}(S_t, \bar{x}_t^*) \leq V_t^{ADAPT}(S_t, \bar{x}_t^*).
\]

\[ \square \]

6. Algorithm for Solving the Model

The original dynamic programming model is computationally intractable due to the dimensionality of the state variable. However, we can reduce the dimensionality, preserving the structure and behavior of the problem yet producing a model that can be solved exactly.
Specifically, the number of dimensions can be reduced greatly by using the scalar \( \bar{b}_t \), giving the aggregate number of banked SRECs, instead of the vector \((b_{t,y})_y\) which captures the banking by vintage. The vintage-specific values appear in the result:

\[
p_{t,y} = \max \left( f^\text{SACP}_{t}^\text{SACP}(\bar{b}_t), \min \left( f^\text{SACP}_{t}^\text{SACP}(b_{t,t-\tau}), e^{-r\Delta t} E_t[p_{t+\Delta t,y}] \right) \right), \quad \forall y \text{ such that } x^*_t,y > 0,
\]

where \( \tilde{y} = \max \{ y : x^*_t,y > 0 \} \), but are only relevant if the number of older SRECs that are about to expire is very large at some \( t \in \mathbb{N} \). This is quite unlikely to happen in reality (in fact, for \( \tau = 4 \), \( b_{t,t-\tau} = 0 \) is virtually guaranteed), specifically because the oldest SRECs are the first to be submitted at each compliance time (by Lemma 1). Therefore, when generating our price surfaces, we find the function \( V_t \) in terms of the scalar \( \bar{b}_t \), with transition function given by

\[
\bar{b}_{t+\Delta t} = \bar{b}_t + g_t \Delta t - \bar{x}^*_t.
\]

However, as we simulate forwards in numerical experiments later, we retain the full vector \((b_{t,y})_y\), allowing us to continually check if our dimension reduction is valid. Experiments with \( \tau = 4 \) and our chosen parameters (see next section) reveal no contradiction of the assumption.

Assuming \( P(\bar{x}^*_t = b_{t,t-\tau}) = 0 \) (as in Theorem 2), Corollary 1 implies that \( f^\text{SACP}_{t}^\text{SACP}(\bar{x}^*_t) = \max \{ f^\text{SACP}_{t}^\text{SACP}(\bar{b}_t), e^{-r\Delta t} E_t[p_{t+\Delta t,y}] \} \) and Theorem 1 then gives,

\[
f^\text{SACP}_{t}^\text{SACP}(\bar{x}^*_t) = \max \left\{ f^\text{SACP}_{t}^\text{SACP}(b_{t}, e^{-r\Delta t} E_t[p_{t+\Delta t,y}]) \right\},
\]

where \( \tilde{y} = \max \{ y : x^*_t,y > 0 \} \). Given our dimension reduction (collapsing \( b_{t,y} \) and \( x^*_t,y \) to \( \bar{b}_t \) and \( \bar{x}^*_t \)), \( \tilde{y} \) is not observable when solving for the price of some vintage \( y \). However, Theorem 2 allows us to replace \( \tilde{y} \) by \( y \). Thus, the optimal \( \bar{x}^*_t \) can be obtained from

\[
\bar{x}^*_t = \min \{ \bar{b}_t, (f^\text{SACP}_{t})^{-1} e^{-r\Delta t} E_t[p_{t+\Delta t,y}] \}.
\]

Note that because \( P_t \) is non-increasing in time, at any time \( t \in \mathbb{N} \) the expected future price is no larger than the maximum penalty at time \( t \) \( (E_t[p_{t+\Delta t,y}^{\text{max}}] \leq P_t) \). Thus, \( e^{-r\Delta t} E_t[p_{t+\Delta t,y}^{\text{max}}] \leq E_t[p_{t+\Delta t,y}^{\text{max}}] \) is in the sloped area of \( f^\text{SACP}_{t} \) and therefore \( (f^\text{SACP}_{t})^{-1} \) is defined.

This means we can solve our dynamic program via SREC prices (and the martingale property) instead of the original objective function. This simplifies calculations at each time step and directly outputs SREC prices. From the fundamental property of prices in (4), we obtain,

\[
p_{t,y} = \exp(-r\Delta t) E_t[p_{t+\Delta t,y}], \quad t \notin \mathbb{N},
\]

and at the compliance dates \( (t \in \mathbb{N}) \), we have

\[
p_{t,y} = \max \{ f^\text{SACP}_{t}^\text{SACP}(\bar{x}^*_t), \exp(-r\Delta t) E_t[p_{t+\Delta t,y}] \}, \quad t \in \mathbb{N}.
\]

We can use equations (9), (10), and (11) to compute the SREC prices using backward induction on a discretized state space. We solve the dynamic program for each vintage in turn, using different grids and starting with the newest vintage \( y^{\text{max}} \) each year due to its assumed role in driving the price feedback. We compute the price surfaces according to the following algorithm.
Discretize the state variable $S_t = (b_t, \hat{g}_t, s_t)$ on a grid ranging over $[0, \kappa^y R_{y+\tau}], [0, \kappa^g R_{y+\tau}]$, and $[-\kappa^y R_{y+\tau}, \kappa^y R_{y+\tau}]$ respectively for each vintage year $y$, where $\kappa^y, \kappa^g > 1$ (e.g. 1.5), and $\kappa^g > 0$ (e.g. 0.5). Also discretize the distribution of the noise variable $\varepsilon_t$ into $n$ outcomes $\varepsilon_{t,i}$ with probability $pr\{\varepsilon_{t,i}\}$, for $i = 1, \ldots, n$.

Initialize the dynamic program by calculating $p_{T,y}^{\text{SACP}}(b_T)$ for all grid points, where $y_{fin}$ denotes the final SREC vintage in our study, and $T = y_{fin} + \tau$.

Go backward through time and compute prices of all (possibly existing) SREC vintages $(y_{min}^i, \ldots, y_{max}^i)$ from (10) and (11) at each grid point $(\bar{b}_t, \hat{g}_t, s_t)$:

(a) If $t \notin N$, $\bar{x}_t = 0$, otherwise find $\bar{x}_t$ by solving $f_t^{\text{SACP}}(\bar{x}_t) = e^{-r \Delta t} E_t\{p_{t+\Delta t,y_{max}^i} \mid \bar{x}_t\}$:

(i) Set $\bar{x}_t = (1 + \lambda)R_t$; at this point $f_t^{\text{SACP}}(\bar{x}_t) = 0$.

(ii) $x_t = \min\{\bar{x}_t, \bar{b}_t\}$

(iii) $p_{t,y_{max}} = \max\{f_t^{\text{SACP}}(\bar{x}_t), f_t^{\text{SACP}}(\bar{b}_t)\}$.

(iv) From (2) $\hat{g}_{t+\Delta t} = \hat{g}_t \exp(a_5 \Delta t + a_6 p_{t,y_{max}} \Delta t)$.

(v) For each $i = 1, \ldots, n$ from (1)

\[
g_{t+\Delta t, i} = \hat{g}_{t+\Delta t} \exp\left(a_1 \sin(4\pi(t + \Delta t)) + a_2 \cos(4\pi(t + \Delta t)) + a_3 \sin(2\pi(t + \Delta t)) + a_4 \cos(2\pi(t + \Delta t)) + \varepsilon_{t,i}\right)
\]

(vi) $\bar{b}_{t+\Delta t, i} = \bar{b}_t + a_1 \Delta t - x_t$.

(vii) $s_{t+\Delta t} = \bar{b}_t - \bar{R}_t$.

(viii) Using the discretized distribution function

\[
E_t[p_{t+\Delta t,y_{max}^i}] = \sum_{s=1}^{n} pr\{\varepsilon_{t,i}\} p_{t+\Delta t,y_{max}^i}(\bar{b}_{t+\Delta t, i}, \hat{g}_{t+\Delta t}, s_{t+\Delta t})
\]

(ix) If $f_t^{\text{SACP}}(\bar{x}_t) < e^{-r \Delta t} E_t\{p_{t+\Delta t,y_{max}^i} \mid \bar{x}_t\}$, update $\bar{x}_t$ to $\bar{x}_t - k$ with $k > 0$, and go to (ii).

(b) Set $\bar{x}^*_t = \min\{\bar{b}_t, \bar{x}_t\}$, and compute $\bar{b}_{t+\Delta t}, \hat{g}_{t+\Delta t}$, and $s_{t+\Delta t}$ as of (a iii) to (a vi) equations.

(c) For $y : y_{max}^i$ to $y_{min}^i$

(i) Calculate $E_t[p_{t+\Delta t,y}] = \sum_{s=1}^{n} pr\{\varepsilon_{t,i}\} p_{t+\Delta t,y}(\bar{b}_{t+\Delta t}, \hat{g}_{t+\Delta t}, s_{t+\Delta t})$.

(ii) $p_{t,y} = \max\{f_t^{\text{SACP}}(\bar{x}^*_t), e^{-r \Delta t} E_t\{p_{t+\Delta t,y}\}\}$.

CPU times for solving over a decade (with an acceptable level of accuracy) with a single fine-grained grid are excessive (on the order of several weeks). As our state variables (e.g. generation) lie on different ranges for early and late years, we can use separate smaller grids for different vintage years (as given in step 1 above) instead of a single large grid. The grid size dynamically changes according to the requirement level. Going forward in time, we need to convert any point from an earlier year grid to the corresponding point in the newer year. This maintains the same level of accuracy, while keeping the problem computationally tractable. Experiments were run for 50 to 100 grid points for each state variable for each vintage year, and this was found to produce an acceptable tradeoff between accuracy and CPU times.
Table 2. Estimated parameters for our linear model

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<td>$1.27 \times 10^{-3}$</td>
<td>$0.186$</td>
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7. Experiments

To gain insight into the effects of different SREC policies, we must first choose some reasonable parameters for the current market design to serve as our benchmark. We use ($\tau = 4$) and values $\bar{R}_t, P_t$ given in Table 1 (based on the latest regulation changes in NJ), along with a sharp cliff and non-adaptive requirements, corresponding to $\lambda = 0, \alpha = 0$. We fix $r = 2\%$, but note that the interest rate has little impact on our results. The parameters for the generation model (for $g_t$) are taken directly from [8] (and shown in Table 2), obtained by fitting a linear model to the log of the historical generation. The noise term satisfies $\epsilon_t \sim \mathcal{N}(0, 0.186)$.

We now report on experiments designed to provide insights into the effect of different market designs. We first assume a steady growth in targets, a strategy that ensures that SREC prices do not rapidly fall towards zero. For this purpose, we set $R_y = \alpha \exp\{\beta (y - 14)\}$, with $\alpha = R_{14}$, the EY2014 requirement level and $\beta > 0$ ($\beta = 0.35$ in the following experiments).

7.1. The slope of the SACP function. There are several critical differences between ADAPT and the current market mechanism. If total banked SRECs are less than the requirement under the step mechanism, they clearly should all be submitted, as $P_t$ is a decreasing sequence, such that the current penalty is more than any possible future price. In contrast, under ADAPT participants can choose the submission value to balance prices before and after submission (to minimize compliance costs). This additional flexibility typically results in equal prices across vintages under ADAPT. Furthermore, even for a small positive $\lambda$ (producing a very steep SACP function), extreme prices near zero or $P_t$ are rare, only happening if the total banked SRECs are either very high or very low.

Figure 4 compares SREC prices (of various vintage years) between a stepped and sloped SACP mechanism, by simulating forwards through time and pulling prices from the appropriate surfaces (interpolating when necessary). The top row shows twenty sample paths, while the bottom averages over 10,000 simulations with 100 grid points for each state variable $\hat{g}_t$ and $\bar{b}_t$ (the price feedback parameter $a_6$ is $7 \times 10^{-4}$). To obtain a meaningful comparison in which price volatility can be easily observed, we need prices that are not too high or too low. Therefore, we do not attempt to match our initial conditions to the market, and instead we use $\hat{g}_{13} = R_{14} \exp(-\beta)$ and $\bar{b}_{13} = 0$, which results in mid to high initial prices.

Figure 4 shows that the cliff policy ($\lambda = 0$) not only produces greater price drops for submitted SRECs (which may then no longer exist), but also far more volatile prices generally. We note that since our initial conditions lead to initial prices fairly near $P_t$ for the cliff policy, a centered tilt
under ADAPT tends to shift initial prices downwards towards mid-range levels. Low initial prices would be likely to rise under ADAPT. The bottom row in Figure 4 also reveals that there was no price difference between SRECs of different vintages when using a sloped SACP ($\lambda > 0$), as expected given results from Section 5. Both of these observations indicate that the sloped mechanism provides a safer and more attractive environment for investment in solar power. These figures show that price volatility decreases substantially as $\lambda$ increases, especially from 0 to 0.1 when a slope is first introduced. Under ADAPT, an equilibrium can typically form between the price of SRECs before and after compliance. This is because if the price after compliance is expected to be higher, a firm would prefer to bank more, accepting a higher penalty today while reducing the price of SRECs in the future, until these tradeoffs balance.

However, price levels do not necessarily follow, and in this example even appear to fall slightly. This is logical for the case of tilting a slope when the market is closer to undersupply than oversupply, as is the case here. Keeping $R$ fixed, increasing $\lambda$ corresponds to imposing a higher total payment on society, as Theorem 3 suggests. However, one could also introduce a slight decrease in $R$ when increasing $\lambda$ (since the effective full requirement is $(1 + \lambda)R$) in order to counteract higher compliance costs, but then also lowering price levels. One might seek a balance between higher payments and less volatility. It seems that the main goal of making solar energy more attractive for investment can be achieved by a market mechanism that produces relatively high and less volatile prices with no price difference between various vintages. Our analysis suggests that an ADAPT mechanism with even a small positive $\lambda$ can provide these significant benefits, without a major impact on the total cost of compliance.
7.2. Adaptive requirements. A challenge faced by policy makers is the design of a fixed target schedule, which appears to require forecasting a highly uncertain rate of market adoption many years in advance, as well as technological changes, economic conditions and other behavioral factors. In line with Massachusetts’ innovative adaptive SREC requirement, or the EU’s upcoming adaptive carbon cap (the MSR), we can circumvent this problem by allowing the requirements to adapt to the current generation level. In our model, we use a combination of fixed and adaptive rules:

\[ R_y = \tilde{R}_y + \alpha (b_{y-1} - \tilde{R}_{y-1}), \quad 0 \leq \alpha \leq 1, y \in \mathbb{N}. \]

As described in Section 3, according to this mechanism, there are two sets of requirements: the base requirement level \( \tilde{R}_y \) fixed in advance, and the adaptive requirement \( R_y \), computed when a portion of last year’s surplus (shortage) is added to (deducted from) the known base \( \tilde{R}_y \). One may expect that such an adaptive mechanism can yield less volatile prices in the long-term by helping to enforce a balanced growth for generation and requirement levels.

Figure 5. 20 price sample paths for an 8 year simulation with \((\lambda, \alpha)\)-tuples \((0,0), (0,0.5), \) and \((0.3,0.5)\).

As discussed earlier in Section 4, modeling a market design with adaptive requirements requires one extra dimension in our dynamic program. Although this extra dimension increases the computational time significantly (from around one hour to around a week with 50 grid points for each dimension), we still are able to solve this problem using an exact dynamic programming approach. Figure 5 investigates the impact of the adaptive mechanism (for \( \alpha = 0.5 \)), both without a slope (\( \lambda = 0 \)) and in conjunction with the slope (\( \lambda = 0.3 \)). According to these results, an adaptive cliff policy also reduces price volatility and avoids the risk of very low SREC prices in comparison with a simple cliff policy (the current mechanism). Adaptive requirements, however, appear to reduce the price volatility less than a simple sloped policy, while also counteracting some of the effect of the slope when used in conjunction (compare with the \( \lambda = 0.3, \alpha = 0 \) case in Figure 4). This final potentially counterintuitive result can be explained by the weakening effect that \( \alpha > 0 \) has on the ability of a banking decision to lower future expected prices, a mechanism central to the price stabilizing impact of the slope.

Figure 6 shows SREC prices for 20 sample paths of another experiment on a sloped policy (\( \lambda = 0.3 \)) with and without adaptive requirements (\( \alpha = 0, \alpha = 0.5, \) and \( \alpha = 1 \)). In this experiment
the original NJ requirement schedule is used, and thus the rate of generation growth is not in line with the rate of requirement growth. The adaptive requirement mechanism ($\alpha = 0.5$) delays the rate of convergence to zero for a couple of years, but it cannot completely stop it. This can be better explained if we refer to the case with $\alpha = 1$. When $\alpha = 1$, any value of positive surplus would be added to the requirement of the next year, and this would fully neutralize the effect of accumulating banked SRECs. However, the long-term rate of capacity growth remains above the requirement growth rate and thus prices fall to zero but slower in comparison with the cases of $\alpha = 0$ and $0.5$. The short-term price variability increases because adaptivity counteracts the smoothing effect of banking, as we discuss in the next section.

All in all, although the adaptive requirements can increase price volatility, they can also, to some extent, correct a lack of long-term foresight by policymakers in predicting the rate of capacity growth. This can reduce (but may not eliminate) the need for regulatory fixes, by providing an additional option in the regulator’s toolkit, but as we have seen, care should be taken in combining such policies strategically.

7.3. More banking years. In addition to requirement changes, another strategy chosen by the regulators during the lifetime of the NJ SREC market has been increasing the number of banking years. This simple strategy firstly ensures higher SREC prices as a result of extra years of validity. Secondly, this can stabilize prices from falling too low, by striking a balance among different energy years.

Figure 7 shows the results of an experiment on the number of banking years. Note that at each time, different SREC vintages may exist. The same colors of lines are used for each vintage, however, the lines with higher prices correspond to newer vintages. According to this figure, the difference between the 10th and the 90th percentile of SREC prices of the newer vintages, which are the majority of SRECs at each time, decreases with a higher number of banking years. For example, with five years of lifetime, prices of the majority of SRECs (zero or one year old SRECs) are much less volatile than those with one or three years of lifetime.
Figure 7. The mean, 10th and 90th percentiles of SREC prices for 10000 simulations with 1, 3, and 5 years of lifetime (from left to right), with $\lambda = 0, \alpha = 0$) and each vintage plotted separately.

8. Conclusion

The current SREC market design produces volatile prices which reduces the attractiveness of this market for investment. This itself creates other problems such as reducing competitiveness of the market and therefore inefficiency in SREC generation. We propose the ADAPT policy which uses a sloped SACP function. We develop a dynamic programming model in order to predict collective market behaviour, and we derive and prove some of the properties of this market such as the collective SREC submission policy. We then use this submission policy and other market properties in a pricing model that enables us to compare the performance of different market designs in terms of price level and volatility. The results of our experiments show that the ADAPT policy (particularly the sloped SACP function) can significantly mitigate the risk of sudden price drops and high volatility, thus ensuring greater market stability and reliability in the long run.

References


