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Measurements of the top quark branching ratios into channels with leptons and quarks with the ATLAS detector

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Measurements of the branching ratios of top quark decays into leptons and jets using events with $t\bar{t}$ (top antitop) pairs are reported. Events were recorded with the ATLAS detector at the LHC in $pp$ collisions at a center-of-mass energy of 7 TeV. The collected data sample corresponds to an integrated luminosity of 4.6 fb$^{-1}$. The measured top quark branching ratios agree with the Standard Model predictions within the measurement uncertainties of a few percent.

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I. INTRODUCTION

In the Standard Model (SM), 100% of the top quark decays contain a $W$ boson and a down-type quark. Measurements of the ratio of top branching fractions $B(t \rightarrow W + b$-quark)/$B(t \rightarrow W +$ down-type quark) [1] and of single top production [2–4] have shown that more than 95% of the decays are to a $W$ boson and a $b$-quark. In the SM the branching ratio to the different leptons is the same since the decay proceeds via a $W$ boson, but in models of new physics, e.g. supersymmetry (SUSY), final states with $τ$ leptons can be enhanced or suppressed [5]; thus measuring the inclusive cross section using final states with $τ$ leptons can be a good probe for new physics. The measured values of the top quark branching ratios will deviate with respect to the SM predictions if the data sample selected to extract $t\bar{t}$ events contains final states without two $W$ bosons. Examples of processes that would cause deviations include events with a top quark decaying to charged Higgs boson or with SUSY particles decaying to the supersymmetric partner of the $τ$ lepton ($\tilde{τ}$). Limits on the top quark branching ratio to a charged Higgs boson and a $b$-quark have been published by the CDF [6], D0 [7,8], ATLAS [9,10] and CMS [11] collaborations. Another example of a final state that can change the observed branching ratios is the pair production of supersymmetric partners of the top quark ($\tilde{t}$) decaying into $b\nu_τ \tilde{τ}$ followed by the $\tilde{τ}$ decay into a $τ$ lepton and the gravitino, predicted by gauge-mediated SUSY breaking models [12].

This article presents the first direct measurement of the top quark semileptonic and all-hadronic branching ratios. The branching ratios can be more sensitive probes of deviations from SM expectations than measuring cross sections in different channels, because of cancellation of systematic uncertainties. The large number of $t\bar{t}$ pairs produced at the LHC provides an opportunity to measure top quark branching ratios with high precision. These top quark branching ratios are expected to be determined by the $W$ boson branching ratios, which have been measured at LEP [13] to be in good agreement with the SM expectations [14]. Observing any deviation would be an indication of non-SM processes contributing to final states dominated by $t\bar{t}$ production. This article also presents a measurement of the inclusive $t\bar{t}$ cross section using events with an isolated charged lepton ($μ$ or $e$) and a $τ$ lepton decaying hadronically ($τ_{\text{had}}$). Previous measurements of the cross section at $\sqrt{s} = 7$ TeV in this channel have been published by the ATLAS and CMS collaborations [15,16].

The analysis uses the full data sample, 4.6 fb$^{-1}$, collected by the ATLAS experiment at the LHC from $pp$ collisions at $\sqrt{s} = 7$ TeV between March and November 2011. Kinematic selection criteria are applied that require one or both of the top and antitop quarks to decay into a final state with one isolated lepton and a jet. At least one jet in the event must be tagged as originating from a $b$-quark ($b$-tag). Seven mutually exclusive final states are used in this analysis: $e +$ jets, $μ +$ jets, $ee +$ jets, $μμ +$ jets, $eμ +$ jets, $eτ_{\text{had}} +$ jets and $μτ_{\text{had}} +$ jets. Branching ratios for semileptonic and purely hadronic top quark decays are obtained by combining these seven final states assuming that only SM processes contribute to the background and the top branching ratios to leptons and jets add up to one.

II. ANALYSIS OVERVIEW

Data samples enriched with $t\bar{t}$ events are selected by means of criteria that are designed to accept two $W$ bosons and at least one $b$-quark. In every event, either an electron or a muon is required, with the aim to select $W \rightarrow ℓν$, where $ℓ$ stands for either $e$ or $μ$. The $ℓ$ may be produced directly in $W \rightarrow ℓν$ boson decays or indirectly in $W \rightarrow τν$...
decays. Separate event channels are classified depending on the decay of a second W boson: \( W \rightarrow \ell + \text{jets}, W \rightarrow \ell\nu \) for \( \ell\ell' + \text{jets}, \) or \( W \rightarrow \ell_\text{had}\nu \) for \( \ell_\text{had} + \text{jets}. \) Since the analysis does not distinguish electrons or muons that originate from a \( t \) lepton decay from those that come from direct \( W \rightarrow e\nu \) and \( W \rightarrow \mu\nu \) decays, both are included in the \( W \rightarrow \ell\nu \) decays. The branching ratios are measured by taking ratios of the number of \( \tau \) events extracted from the three channels; thus an important aspect of the event selection is to use similar criteria for the object selection in the three channels; thus an important aspect of the event in the \( \tau \) selection is to use similar criteria for the object selection in all final states, so as to allow the cancellation of systematic uncertainties in the ratios. Another important criterion is to ensure that no event contributes to more than one channel. The channel with the largest background and smallest number of signal events is that containing \( \ell_\text{had} + \text{jets}; \) thus the event selection and analysis were optimized to reduce the uncertainty in that channel (see Sec. V).

The number of \( \tau \) events in a given channel is extracted by fitting background and signal templates to data distributions. The template shapes are fixed while their normalizations are allowed to vary. The signal templates are derived from \( \tau \) Monte Carlo (MC) simulation, which assumes that the top quark decays to a \( W \) boson and a \( b \)-quark with a 100\% branching ratio. This assumption affects the shape of the signal templates, and if it is not valid for the selected data, the measured branching ratios will deviate from the SM prediction. The amount of background varies significantly in each channel. It is almost negligible in the \( e\mu + \text{jets} \) channel and larger than the signal in the \( \ell_\text{had} + \text{jets} \) channel. In the \( \ell + \text{jets} \) channels, three invariant masses from two- and three-jet systems and a transverse mass distribution are fitted, as described in detail in Sec. VI, while in the \( \ell\ell' + \text{jets} \) channels the dilepton effective mass distributions from two different missing transverse momentum (\( E_T^{\text{miss}} \)) regions are used (see Sec. VII). Because of the much larger background, which originates from jets misidentified as \( \tau \) leptons, a very different approach is taken in the \( \ell_\text{had} + \text{jets} \) channel. Instead of fitting a kinematic distribution, the quantity fitted is a boosted decision tree (BDT) output [17], a multivariate discriminant that separates jets from \( \tau \) leptons decaying to hadrons (see Sec. VIII).

The details of how the inclusive production cross section and branching ratios are derived from the number of \( \tau \) events obtained from each channel are discussed in Sec. IX. The systematic uncertainties of the measurements are estimated by varying each source of systematic uncertainty by \( \pm 1\sigma \) in templates derived from MC simulation and fitting all the distributions with the new templates (see Sec. X). The final results are given in Sec. XI.

### III. ATLAS DETECTOR

The ATLAS detector [18] at the LHC covers nearly the entire solid angle around the collision point.\(^1\) It consists of an inner tracking detector surrounded by a thin superconducting solenoid, electromagnetic (EM) and hadronic calorimeters, and an external muon spectrometer incorporating three large superconducting toroid magnet assemblies. The inner tracking detector provides tracking information in a pseudorapidity range \(|\eta| < 2.5\). The liquid-argon (LAr) EM sampling calorimeters cover a range of \(|\eta| < 3.2\) with fine granularity. An iron/scintillator tile calorimeter provides hadronic energy measurements in the central rapidity range \(|\eta| < 1.7\). The endcap and forward regions are instrumented with LAr calorimeters for both the EM and hadronic energy measurements covering \(|\eta| < 4.9\). The muon spectrometer provides precise tracking information in a range of \(|\eta| < 2.7\).

In 2011, ATLAS used a three-level trigger system to select events. The level-1 trigger is implemented in hardware using a subset of detector information to reduce the event rate to less than 75 kHz. This is followed by two software-based trigger levels, namely level-2 and the event filter, which together reduce the event rate to about 300 Hz recorded for analysis.

### IV. DATA AND MONTE CARLO SAMPLES

The present measurements use collision data with a center-of-mass energy of \( \sqrt{s} = 7 \text{ TeV} \) taken in 2011 and selected with a single-electron or a single-muon trigger. Taking into account selection criteria for good data quality, the total integrated luminosity for the analyzed data sample is \( 4.6 \text{ fb}^{-1} \).

The \( \tau \) signal is modeled using the POWHEG [19,20] event generator, interfaced to PYTHIA6 (v6.421) [21] with the Perugia 2011C tune [22] for showering and hadronization, setting the top quark mass to 172.5 GeV and using the next-to-leading-order (NLO) parton distribution function (PDF) set CTEQ66 [23]. The \( \tau \) production cross section used in the simulation is normalized to 177 pb as obtained from next-to-next-to-leading-order (NNLO) plus next-to-next-to-leading-logarithm (NNLL) calculations [24].

The calculation of the backgrounds uses MC simulations of \( W/Z \) production with multiple jets (matrix elements for the jets production include light quarks, \( c, \bar{c}, \bar{c} \), \( b\bar{b} \)), single-top-quark, and diboson (\( WW, WZ, ZZ \)) events. Single-top-quark events were generated using MC@NLO (v4.01) [25] interfaced with HERWIG (v6.520) [26] and JIMMY (v4.31) [27] to model parton showering.

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\(^1\)ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point in the center of the detector and the \( z \) axis along the beam pipe. The \( x \) axis points to the center of the LHC ring, and the \( y \) axis points upwards. The azimuthal angle \( \phi \) is measured around the beam axis and the polar angle \( \theta \) is the angle from the beam axis. The pseudorapidity is defined as \( \eta = -\ln[\tan(\theta/2)] \). The distance \( \Delta R \) in \( \eta-\phi \) space is defined as \( \Delta R = \sqrt{\Delta\phi^2 + (\Delta\eta)^2} \). The transverse momentum and energy are defined as \( p_T = p \sin \theta \) and \( E_T = E \sin \theta \), respectively.
hadronization, and the underlying-event using PDF set CT10 [28]. W + jets events with up to five partons and $Z + \text{jets}$ events generated with $m(\ell^+\ell^-) > 40 \text{ GeV}$ and up to five partons were generated using ALPGEN (v2.13) [29] interfaced to HERWIG plus JIMMY and the CTEQ6L1 [30] PDF set. The MLM matching scheme [31] of the ALPGEN generator is used to remove overlaps between matrix-element and parton-shower products. Diboson events were generated using HERWIG plus JIMMY and the MRST Mcal PDF set [32]. Scale factors are applied to each process to match next-to-leading-order predictions. The $\tau$ decays are handled by TAUOLA [33].

All samples of simulated events include the effect of multiple $pp$ interactions in the same and neighboring bunch crossings (pile-up). On average, nine minimum-bias events are overlaid on all simulated events to match the pile-up conditions in data. The average number of $pp$ collisions in a bunch crossing ($(\mu)$) depends on the instantaneous luminosity, which increased over time; $(\mu)$ varied from 5 at the beginning of the run period to approximately 18 at the end. The events are reweighted in order to make the distribution of the average number of interactions per bunch crossing match the one observed in data. All MC events are simulated with a detailed GEANT4-based detector simulation [34,35] and are reconstructed with the same algorithms as used in data.

V. EVENT SELECTION

Events are selected using a single-muon trigger with a $p_T$ threshold of 18 GeV or a single-electron trigger with an $E_T$ threshold of 20 GeV, rising to 22 GeV during periods of high instantaneous luminosity. The $p_T$ and $E_T$ criteria used in the further analysis guarantee a high and constant trigger efficiency. The same triggers and reconstructed object definitions are applied to all channels.

Muon candidates are selected using tracks from the inner detector matched with tracks in the muon spectrometer [36]. They are required to have $p_T > 20 \text{ GeV}$ and $|\eta| < 2.5$ and to satisfy criteria designed to reduce the muon misidentification probability. The muon must have a longitudinal impact parameter ($z_0$) with respect to the primary vertex of less than 2 mm. In addition, to suppress muons from heavy-quark decays, muons must pass the isolation cuts: the calorimeter energy in a cone of size $\Delta R = 0.2$ around the muon track must be less than 4 GeV, and the scalar sum of the $p_T$ of the tracks reconstructed in the inner tracker in a cone of $\Delta R = 0.3$ around the muon track must be less than 2.5 GeV. If a muon overlaps within a cone of $\Delta R = 0.4$ with an electron candidate or with a jet, as defined below, it is not considered to be isolated.

Electron candidates are required to satisfy cuts on calorimeter and tracking variables to separate isolated electrons from jets [37]. Electrons must fall into the region $|\eta_{\text{cluster}}| < 2.47$, where $|\eta_{\text{cluster}}|$ is the pseudorapidity of the calorimeter energy cluster associated with the electron, excluding the transition region between the barrel and endcap calorimeters at $1.37 < |\eta_{\text{cluster}}| < 1.52$, and have $E_T > 25 \text{ GeV}$. The electrons must also pass an $E_T$ isolation cut within a cone of $\Delta R = 0.2$ derived for 90% efficiency along with a $p_T$ isolation cut within a cone of $\Delta R = 0.3$ derived for 90% efficiency for prompt electrons from $Z \rightarrow e^+ e^-$ events. The electron must have $z_0$ with respect to the primary vertex of less than 2 mm. Finally, if the electron lies within a cone of $\Delta R = 0.4$ around the muon or between $0.2 < \Delta R \leq 0.4$ around a jet as defined below, the object is considered to be a muon or a jet, respectively.

Jets are reconstructed from clustered energy deposits in the calorimeters using the anti-$k_t$ [38] algorithm with a radius parameter $R = 0.4$. Jets are required to have a transverse momentum $p_T > 25 \text{ GeV}$ and to be in the pseudorapidity range $|\eta| < 2.5$. The summed scalar $p_T$ of tracks associated with the jet and associated with the primary vertex is required to be at least 75% of the summed $p_T$ of all tracks associated with the jet [39]. Any jet close to a good electron, as defined above, is considered to be an electron if it lies within a cone of $\Delta R = 0.2$ around the electron. Missing transverse momentum ($E_T^{\text{miss}}$) is the magnitude of the vector sum of the $x$ and $y$ components of the cluster energy in the calorimeters. Each cluster is calibrated according to which type of high-$p_T$ object it is matched to, either electrons, jets, muons or photons.

Jets containing $b$-hadrons ($b$-jets) are identified ($b$-tagged) with a multivariate discriminant that exploits the long lifetimes, high masses and high decay multiplicities of $b$-hadrons. It makes use of track impact parameters and reconstructed secondary vertices. An operating point corresponding to an average efficiency of 70% and an average mistag rate for light-quark jets of 0.8% is used [40].

$\tau$ candidates are reconstructed using calorimeter jets as seeds. These seed jets are calibrated with the local calibration (LC) scheme [41,42]. The $\tau$ candidate must have $E_T > 20 \text{ GeV}$, $|\eta_T| < 2.3$, and only one track with $p_T > 4 \text{ GeV}$ associated with the $\tau$ candidate (77% of hadronic $\tau$ decays have only one track). The charge of the $\tau$ candidate is given by the charge of the associated track. Candidates with higher track multiplicity are not used as they do not improve the precision of the measurement because of much larger associated systematic uncertainties. The analysis makes use of a BDT for $\tau$ identification, a cut-based multivariate algorithm that optimizes signal and background separation [17].

The $\tau$ candidates that overlap within $\Delta R < 0.4$ of a $b$-tagged jet, a loose muon, or an electron, are rejected and kept as jets or electrons. To remove the remaining

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Loose muons are selected with all requirements described in Sec. V for good muons, except $p_T > 4 \text{ GeV}$ and no isolation requirements are applied.

These electrons are selected with all requirements described in Sec. V for good electrons, but electrons with $E_T > 20 \text{ GeV}$ are considered.
electrons misidentified as τ candidates a medium BDT (BDT$_{\tau}$) electron veto is applied. BDT$_{\tau}$ is a BDT trained to distinguish electrons and τ leptons using a $Z \rightarrow \tau\tau$ MC sample as signal and a $Z \rightarrow \ell\ell$ MC sample as background. The BDT$_{\tau}$ uses four variables; the two most powerful being the ratio of high-threshold to low-threshold track hits in the transition radiator and the ratio of energy deposited in the EM calorimeter to the total energy deposited in the calorimeter. The medium working point corresponds to 85% efficiency for $Z \rightarrow \tau\tau$, Ref. [43]. The additional rejection factor for electrons after removing isolated electrons that overlap with τ candidates is 60. In addition, a muon veto that compares the track momentum in τ candidates with the energy deposited in the electromagnetic calorimeter is required to further reduce the muon background. It is tuned to 96% efficiency on signal (62% on background after overlap removal). A BDT to reject hadronic jets faking τ leptons, BDT$_{\tau}$, is trained with τ leptons from a $Z \rightarrow \tau\tau$ MC sample as signal and jets from data, selected from events with at least two jets, as background. The BDT$_{\tau}$ uses eight variables, the most sensitive is the fraction of energy deposited in the region $\Delta R < 0.1$ with respect to all energy deposited in the region $\Delta R < 0.2$ around the τ candidate. Details of the BDT$_{\tau}$ and BDT$_{\tau}$ input variables and performance are given in Ref. [43].

The event selection requirements common to all channels are a primary vertex with at least five associated tracks with $p_T > 400$ MeV, at least one isolated high-$p_T$ muon ($p_T > 20$ GeV) and/or isolated high-$p_T$ electron ($p_T > 25$ GeV), at least two jets with $p_T > 25$ GeV, and at least one of them tagged as a b-jet. In addition, there are requirements specific to each channel. For the $\ell +$ jets channels the isolated-muon $p_T$ threshold is raised from 20 GeV to 25 GeV to reduce the multijet background and exactly one isolated $\ell$ is required. The minimum number of jets with $p_T > 25$ GeV is raised to four. Events with τ candidates are removed. Removing events with τ candidates from the $\ell +$ jets channel results in an efficiency loss of 8.5%. For the $\ell\ell +$ jets channels, events are required to have exactly two isolated $\ell$ with opposite-sign charges and $E_T^{\text{miss}} > 30$ GeV. For the $\ell_{\text{had}} +$ jets channels, exactly one isolated $\ell$, $E_T^{\text{miss}} > 30$ GeV, and at least one τ candidate are required. In addition the $\ell$ and the τ candidate must have opposite charge. The τ candidates that do not satisfy these requirements are kept as jets. The thresholds for lepton $p_T$, jet $p_T$ and $E_T^{\text{miss}}$ were optimized for the $\ell_{\text{had}} +$ jets channel for maximum signal significance by means of a search in parameter space.

VI. SINGLE-LEPTON + JETS CHANNEL

Three different classes of events contribute as a background to the $t\bar{t} \rightarrow \ell +$ jets channel:

1. events with one isolated $\ell$ originating from processes with one true lepton ($W$ boson decay);
2. events with one jet misidentified as an isolated lepton and no other isolated lepton reconstructed;
3. events with one isolated lepton originating from processes with multiple true leptons but only one isolated lepton reconstructed.

The number of $t\bar{t} \rightarrow \ell +$ jets events is extracted by fitting distributions of four invariant mass variables with templates for signal and backgrounds. The following variables provide good discrimination between signal and background:

1. $m_{jj}$: invariant mass of the two highest-$p_T$ jets not designated as b-jets;
2. $m_{b\ell jj}$: invariant mass of the leading b-jet and the jets used to calculate $m_{jj}$;
3. $m_{b\ell jj}$: invariant mass of the subleading b-jet and the jets used to calculate $m_{jj}$;
4. $m_T$: transverse mass of $\ell$ and the $E_T^{\text{miss}}, m_T(\ell, E_T^{\text{miss}}) = \sqrt{(E_T^\ell + E_T^{\text{miss}})^2 - (p_T^\ell + E_T^{\text{miss}})^2 - (p_T^\ell + E_T^{\text{miss}})^2}$.

If an event has only one jet tagged as a b-jet, the highest-$p_T$ jet that is not tagged is assumed to be a second b-jet. A few observations motivate the choice of mass distributions for the fit. The presence of a $W$ boson decaying to a pair of quarks leads to an $m_{jj}$ distribution that peaks at the $W$ boson mass. The presence of a top quark decaying to $\ell + \nu$ manifests itself as a Jacobian peak in the $m_T$ distribution when there are no additional high-$p_T$ neutrinos in the event.

A. Background templates

The main backgrounds in the $\ell +$ jets channel are from $W(\rightarrow \ell\nu) +$ jets and other $t\bar{t}$ final states. There are also smaller contributions from single top, $Z(\rightarrow \ell\ell) +$ jets (with one lepton not identified) and multijet processes with one jet misidentified as a lepton. Background templates are derived from the MC simulations in all cases except multijet processes. The multijet background is very difficult to simulate due to the need for a very large sample and the fact that MC models do not reproduce that background well. Instead it is derived from a control data sample with nonisolated electrons and muons, keeping all other selection criteria the same. The distributions of a small expected contribution from $t\bar{t}$ is subtracted from the multijet control sample.

Figure 1 shows the $m_{jj}$, $m_{b\ell jj}$, and $m_T$ distributions predicted by MC simulation and normalized to unity for $W +$ jets, $Z +$ jets, and $t\bar{t} \rightarrow \ell +$ jets events. It also shows these distributions for multijet events derived from the control data sample. The distributions from other $t\bar{t}$ channels are not shown as that background is normalized following the MC prediction of the ratio to the number of $t\bar{t} \rightarrow \ell +$ jets events. The figure demonstrates that the shape of all the invariant mass distributions from jets are
jets. On the other hand, the those with little intrinsic only significant background in the control data sample is and the same jet selections as for the quarks decaying to $\tau$. They do show a clear separation between $l\tau$ channels but cannot discriminate between them. They show a clear separation between final states with one $W$ boson decaying leptonically and those with little intrinsic $E_{\text{T}}^\text{miss}$ ($Z + \text{jets}$ and multijets).

The background templates for $Z + \text{jets}$ events from MC simulation are checked with $Z + \text{jets}$ events from data by selecting events with two identified leptons and requiring the dilepton mass to be near the $Z$ mass. Events are required to have two oppositely charged leptons ($p_T^\ell > 25$ GeV and $p_T^\ell > 20$ GeV), $70 \text{GeV} < m_{\ell\ell} < 110 \text{GeV}$, $E_{\text{T}}^\text{miss} > 30$ GeV, and the same jet selections as for the $\ell + \text{jets}$ signal. The only significant background in the control data sample is from the $t\bar{t} \rightarrow \ell\ell' + \text{jets}$ channel. Figure 2 shows the $m_{jj}$, $m_{b1j}$, and $m_{b2j}$ distributions after merging $ee$ and $\mu\mu$ events for ALPGEN $Z + \text{jets}$ MC simulation and the data after applying scale factors (SF) based on comparing data and simulation as a function of the $Z$ boson $p_T$ and the jet multiplicity. The small expected $t\bar{t}$ contribution is subtracted from the data distributions. The Kolmogorov-Smirnov goodness-of-fit test (KS) value in each plot indicates how well the shape of the data distribution is described by the ALPGEN MC simulation. Since there is no noticeable difference between the shapes of the $W + \text{jets}$ and $Z + \text{jets}$ templates, as shown in Fig. 1, one can conclude that both MC templates can reproduce reasonably well the distributions expected in the data. The number of selected $Z + \text{jets}$ events is also predicted well by the simulation.

\textsuperscript{4}KS is calculated with the function supplied by ROOT for comparing the compatibility of two histograms [44].
B. Fits to mass distributions

As shown in Sec. VI A the three invariant masses constructed from jets do not discriminate between the various backgrounds, while the signal from $t\bar{t}$ is quite distinct. The only distribution that is different for each background is the transverse mass. In particular, the transverse mass clearly distinguishes final states with intrinsic $E_T^{\text{miss}}$, i.e. those with a W boson decaying to a lepton and neutrino, from those where $E_T^{\text{miss}}$ is due to mismeasurements. The dominant processes without sizeable intrinsic $E_T^{\text{miss}}$ are multijet and $Z +jets$. The transverse mass distributions for those two processes are different. However, they contribute little in mass distributions for those two processes are different.

However, they contribute little in mass distributions for those two processes are different. The fractional contributions for the various $t\bar{t}$ channels are obtained using MC events. To ensure that events are not used more than once, two sets of data are fitted: $E_T^{\text{miss}} < 30$ GeV (set 1) and $E_T^{\text{miss}} > 30$ GeV (set 2). Set 1 is used to fit the $m_T$ distributions and helps determine the multijet background. Set 2 is used to fit the three jet mass distributions. Both sets are fit simultaneously with three parameters: the total number of multijet events, the total number of $W +$ jets events and the total number of $t\bar{t}$ events.

The variables $m_{b1jj}$ and $m_{b2jj}$ are strongly correlated with $m_{jj}$. To exploit the fact that the correlations are very different in $t\bar{t}$ and the background, the fits are done simultaneously in $6 \times 6$ bins of $m_{jj}$, $m_{b1jj}$ and $m_{b2jj}$ for a total of 216 bins. Of those, 30 bins have zero events since they are kinematically not possible. The ranges and bin sizes are chosen so that all bins used for fitting are populated by more than 10 events. That limits the range of $m_T$ to $m_T < 120$ GeV, $m_{jj}$ to $m_{jj} < 250$ GeV, $m_{b1jj}$ to $m_{b1jj} < 450$ GeV, and $m_{b2jj}$ to $m_{b2jj} < 450$ GeV.

The $m_T$ distributions for events with $E_T^{\text{miss}} < 30$ GeV, used in the fits, are shown in Fig. 3. Table I shows the predicted contributions from each channel, combining events with $E_T^{\text{miss}} < 30$ GeV and $E_T^{\text{miss}} > 30$ GeV. Figure 4 shows that the fits describe well the full $e +$ jets and $\mu +$ jets event distributions of $m_{jj}$, $m_{b1jj}$ and $m_{b2jj}$ after requiring $E_T^{\text{miss}} > 30$ GeV. Figure 5 shows the $m_T$ distribution for events with $E_T^{\text{miss}} > 30$ GeV compared with the predicted contributions, which agree well with the data.

Noticeable features from these fits are as follows:

(i) The largest backgrounds originate in $W +$ jets (15%) and other $t\bar{t}$ channels (8.5%); the rest add up to 12% (multijets 5.3%, $Z +$ jets 3.9%, and single top 3.0%).

(ii) The numbers of $t\bar{t}$ and $W +$ jets events obtained by fitting are in good agreement with those predicted by the SM.

![Graphs of mass distributions for different processes](image-url)
VII. DILEPTON + JETS CHANNEL

The number of \( t\bar{t} \rightarrow \ell\ell' + \text{jets} \) events in the data is extracted by fitting two dilepton invariant mass distributions: one with \( 30 < E_{T\text{miss}} < 60 \text{ GeV} \) and the other with \( E_{T\text{miss}} > 60 \text{ GeV} \). The most significant background to the \( \ell\ell' + \text{jets} \) channels after requiring \( E_{T\text{miss}} > 30 \text{ GeV} \) and at least one \( b \)-tagged jet comes from the \( Z(\rightarrow \ell\ell') + \text{jets} \), with a smaller contribution from single top production (4%). Since the \( E_{T\text{miss}} \) distribution falls more rapidly for the \( Z + \text{jets} \) background than for the \( t\bar{t} \) signal process separating it into two \( E_{T\text{miss}} \) bins improves the sensitivity of the fit for separating the two processes. Backgrounds from dibosons and jets misidentified as isolated leptons (mainly from \( W + \text{jets} \) with leptons from heavy-quark semileptonic decays or an isolated charged hadron misidentified as a lepton, together denoted as nonprompt leptons) amount to 1.0% of the events. The background from nonprompt isolated leptons is estimated from the number of data events with lepton pairs with the same charge after subtracting a very small expected contribution from diboson processes. The invariant mass distributions are fitted with three templates: one derived from a \( t\bar{t} \) MC sample, one from a \( Z + \text{jets} \) MC sample, and one summed over all other contributions. Only the amounts contributed by \( t\bar{t} \) and \( Z + \text{jets} \) are allowed to vary. The \( Z \) boson background in the \( e\mu + \text{jets} \) channel from the \( Z(\rightarrow \tau\tau \rightarrow e\mu) + X \) channel is too small to be extracted by a fit, so \( m_{e\mu} \) is fitted only for the number of \( t\bar{t} \) events in the data while the background is fixed. The fits in the \( \ell\ell' \) channel are performed over a mass range from 40 GeV to 250 GeV and in the \( e\mu \) channel over a mass range from 10 GeV to 250 GeV. Figures 6 and 7 show that the \( m_{e\mu} \) and \( E_{T\text{miss}} \) distributions are well described in all dilepton channels. Results of the fits are given in Table II.

VIII. LEPTON + \( \tau_{\text{had}} \) + JETS CHANNEL

Unlike the single-lepton + jets and dilepton channels the background in the \( \ell\tau_{\text{had}} + \text{jets} \) channel is not small and is dominated by contributions from other \( t\bar{t} \) channels. Thus, invariant masses and other kinematic variables are not

---

**TABLE I.** Results from fitting \( e + \text{jets} \) and \( \mu + \text{jets} \) mass distributions from \( \ell + \text{jets} \) events requiring exactly one isolated lepton \( (e \text{ or } \mu) \), at least four jets, and at least one \( b \)-tag. The uncertainties quoted here are from the fits and do not include systematic uncertainties. The \( Z + \text{jets} \) contribution is normalized to the MC expectation. In addition to MC statistical uncertainty, it includes the uncertainty from the scale factors applied to the simulation in order to match the jet multiplicity and the \( Z \) boson \( p_T \) dependence to that observed in the data. The single top and diboson contributions are normalized to MC predictions, include only MC statistical uncertainty and the SM cross section uncertainty. The (MC) rows give the numbers expected from MC simulation. The \( \chi^2/\text{ndf} \) row gives the \( \chi^2 \) and degrees of freedom of the fits.

<table>
<thead>
<tr>
<th>Channel</th>
<th>( e + \text{jets} )</th>
<th>( \mu + \text{jets} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t\bar{t} \rightarrow \ell\ell' + \text{jets} ) (MC)</td>
<td>(18966 ± 31)</td>
<td>(24233 ± 34)</td>
</tr>
<tr>
<td>( t\bar{t} ) (MC)</td>
<td>(2674 ± 30)</td>
<td>(3393 ± 30)</td>
</tr>
<tr>
<td>( W + \text{jets} ) (MC)</td>
<td>(2577 ± 11)</td>
<td>(3277 ± 16)</td>
</tr>
<tr>
<td>( Z + \text{jets} ) (MC)</td>
<td>(4140 ± 70)</td>
<td>(5850 ± 90)</td>
</tr>
<tr>
<td>Total background</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Signal + background</td>
<td>(25090 ± 310)</td>
<td>(24233 ± 340)</td>
</tr>
<tr>
<td>Data</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \chi^2/\text{ndf} )</td>
<td>11333 ± 700</td>
<td>13700 ± 600</td>
</tr>
<tr>
<td></td>
<td></td>
<td>31000 ± 800</td>
</tr>
<tr>
<td></td>
<td></td>
<td>30733</td>
</tr>
<tr>
<td></td>
<td></td>
<td>188/207</td>
</tr>
</tbody>
</table>
sufficiently sensitive to separate signal and background. In this case a BDT multivariate discriminant, named BDT$_T$, is used to separate $\tau$ leptons from jets identified as $\tau$ candidates (see Sec. V). Compared to the previous ATLAS measurement with this channel [15], the present analysis uses only one-prong $\tau$ decays and is based on a larger data sample with a different background model to reduce the statistical uncertainty on the background prediction.

A. Tau background templates

In order to separate the contribution of processes with $\tau$ leptons (signal) from those with jets misidentified as $\tau$ (fake $\tau$) the BDT$_T$ distributions of selected events are fitted with templates for fake $\tau$ distributions derived from data and true $\tau$ lepton distributions derived from MC simulation. Control data samples to obtain templates of jets misidentified as $\tau$ candidates are selected with the following requirements:

(i) exactly one isolated electron with $p_T > 25$ GeV and no identified muons for the $e + \tau$ channel;
(ii) or exactly one isolated muon with $p_T > 20$ GeV and no identified electrons for the $\mu + \tau$ channel;
(iii) and no additional muons with $p_T > 4$ GeV;
(iv) and $40$ GeV < $m_T(\ell, E_T^{miss})$ < 100 GeV;
(v) and exactly one $\tau$ candidate and at most one additional jet.

There are two mutually exclusive control samples:

The $W + 1$-jet sample contains a lepton, one jet misidentified as a $\tau$ candidate and no additional jets. The $W + 2$-jets sample contains a lepton and exactly two jets with the lower $p_T$ jet misidentified as a $\tau$ candidate.
The control samples are divided into two subsamples, one with $\tau$ and $\ell'$ having the opposite-sign charges (OS), and the other with $\tau$ and $\ell'$ having the same-sign charges (SS). The $W + 1$-jet sample is rich in jets originating from quark hadronization (quark jets) while the $W + 2$-jets sample has a high percentage of jets originating from gluon hadronization (gluon jets) as determined from MC studies. One can extract the distributions of gluon jets misidentified as $\tau$ candidates since the number of gluon jets in OS and SS samples must be the same because they are not correlated with the charge of the lepton. Fake $\tau$ template shapes depend on the jet type. Those from light-quark jets peak at higher BDT$_j$ values than those from gluon jets. The signal contributes only to OS events. Therefore, the BDT$_j$ distributions of OS events are fitted with a pair of background templates, whose linear combination equals the sum of the OS light-quark and gluon jets identified as $\tau$ candidates, and a signal $\tau$ template. MC studies show that requiring $\tau$ candidates that have only one associated charged particle strongly suppresses jets originating from heavy quarks ($c$-jets, $b$-jets). The $b$-jets are further suppressed by excluding $\tau$ candidates that are tagged as $b$-jets. The BDT$_j$ template from remaining $c$-jets identified as $\tau$ candidates is similar to the light-quark template. The signal template is constructed by summing the expected contribution of any channel that has a real $\tau$ lepton or a lepton misidentified as a $\tau$ lepton.

In the $W + 2$-jets sample the lower-$p_T$ jet has a high probability of coming from final- or initial-state radiation and thus a high probability of being a gluon jet. In the following, OS1 (SS1) stands for the $\tau$ fake BDT$_j$ distribution obtained from OS (SS) $W + 1$-jet data sets and OS2 (SS2) represent the equivalent distribution for $W + 2$-jets. Figures 8(a) and 8(b) show the OS and OS-SS distributions normalized to compare the shapes. It can be seen that there are significant differences between OS1 and OS2, but if one subtracts the SS distribution from the OS distribution (OS-SS) the shapes are in good agreement. The distributions are a sum of light-quark jets and gluon jets, and can be described by the following equations:

$$\text{OS1} = a_1 \cdot \text{OS}_q + b_1 \cdot G,$$

$$\text{SS1} = c_1 \cdot \text{SS}_q + b_1 \cdot G,$$

$$\text{OS2} = a_2 \cdot \text{OS}_q + b_2 \cdot G,$$

$$\text{SS2} = c_2 \cdot \text{SS}_q + b_2 \cdot G,$$

where $\text{OS}_q$ ($\text{SS}_q$) is a function describing the shape of the distribution of light-quark jets contributing to OS (SS) and $G$ is the corresponding function for gluon jets. The observation that the OS1–SS1 and OS2–SS2 distributions have the same shape leads to the conclusion that $a_1/c_1 = a_2/c_2$ for any $E_T$ as the $E_T$ of $\tau$ candidates from $W + 2$-jets are significantly lower than those from $W + 1$-jet. Using the above equations, one can extract the $G$ function from the OS and SS distributions separately, i.e.

$$K \cdot G = (R \cdot \text{OS1} - \text{OS1}),$$

$$K \cdot G = (R \cdot \text{SS2} - \text{SS1}).$$
where \( R \) is the ratio of the total number of OS1–SS1 events to OS2–SS2 events and \( K = R \cdot b_2 - b_1 \) is an unknown constant that must be the same whether SS or OS is used to extract \( G \). Figure 8(c) shows the extracted \( K \cdot G \) distributions for \( \tau \) candidates. It is seen that the OS and SS distributions are fully consistent with each other and can be summed to reduce the statistical uncertainties.

In principle any background BDT \( j \) distribution can be described by a linear combination of \( G \) and OS1 distributions. Furthermore, the BDT \( j \) distributions depend on \( E_T \) of the \( \tau \) candidates, which differs from sample to sample. The \( E_T \) dependence of the BDT \( j \) is taken into account by fitting separate \( E_T \) regions with templates derived for those regions weighted to reproduce the \( E_T \) distributions of the expected background. The OS1 sample has a small (2\%) number of \( \tau \) leptons from dibosons and \( Z \to \tau^+ \tau^- \) final states that have no impact on the fits to \( \ell^+ \ell^- + \text{jets} \) BDT \( j \) data distributions whether or not they are subtracted from the OS1 template.

**B. Signal extraction by fitting to BDT \( j \) shape**

The final background normalization and signal measurement are established through fitting templates to the data. There are various classes of background:

- Data
- Template
- Other
(1) from processes with an isolated $\ell$ where a jet is misidentified as a $\tau$ candidate;
(2) from processes other than $t\bar{t}$ that have $\tau$ leptons and an isolated $\ell$;
(3) from processes with two isolated $\ell$ where one $\ell$ is misidentified as a $\tau$ candidate;
(4) from multijet processes where both $\ell$ and $\tau$ are from one jet misidentified as an isolated $\ell$ and another as a $\tau$ candidate.

The dominant background to the $t\bar{t} \rightarrow \ell \tau_{\text{had}} + \text{jets}$ channel comes from the $t\bar{t} \rightarrow \ell + \text{jets}$ channel with one jet misidentified as a $\tau$ candidate (class 1). The only powerful suppression technique for that background is $\tau$ identification, thus the best variable is the BDT$_{\tau}$ score, described with the $\tau$ candidate selection in Sec. V. Background of classes 1 and 4 is taken into account using templates consisting of light-quark jet $\tau$ fakes and gluon jet $\tau$ fakes derived from enriched $W + \text{jets}$ data samples as described in Sec. VIII A.

The signal BDT$_{\tau}$ template is derived from MC $\tau$ candidates that are matched to a $\tau$ lepton or a lepton from MC events that satisfy the event selection (classes 2 and 3). The class 2 processes contributing to the signal template are $t\bar{t} \rightarrow \ell \tau + \text{jets}, Z(\rightarrow \tau^{+}\tau^{-}) + \text{jets}$, and small contributions from single top and diboson events. The main backgrounds of class 3 are $Z \rightarrow e^{+}e^{-}$ and $t\bar{t}$ events. Most electrons are removed by the BDT$_{\tau}$ cut (see Sec. V); the few that remain are indistinguishable from $\tau$ leptons. There is an even smaller number of muons overlapping with $\tau$ candidates that are not removed by the muon veto and are also indistinguishable from $\tau$ leptons. In these cases, the $\tau$ candidates are added to the signal template. The efficiency for electrons and muons misidentified as $\tau$ candidates is determined by studying $Z \rightarrow \ell^{+}\ell^{-}$ events. Based on these studies the estimated contribution from class 3 background to the signal template is 2.8%. The total contribution from class 2 and class 3 backgrounds ($Z + \text{jets}, t\bar{t} \rightarrow \ell \ell + \text{jets}$, single top and dibosons) to the signal template is 15%. Table III shows the detailed composition of the signal templates.

### Table II. Results from fitting $\ell\ell'$ invariant mass distributions using two $E_{T}^{miss}$ regions from $\ell\ell' + \text{jets}$ events requiring two isolated leptons ($e$ or $\mu$), $E_{T}^{miss} > 30$ GeV, at least two jets, and at least one $b$-tag. The numbers of events are after summing events from both $E_{T}^{miss}$ regions $E_{T}^{miss} < 60$ GeV and $E_{T}^{miss} > 60$ GeV. The uncertainties are from the fits and do not include systematic uncertainties. The single top and diboson contributions are normalized to the SM predictions and include only the MC statistical uncertainty and the uncertainty on the SM cross section. The (MC) rows give the numbers expected from MC simulation.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$\mu\mu + \text{jets}$</th>
<th>$ee + \text{jets}$</th>
<th>$e\mu + \text{jets}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t\bar{t}$</td>
<td>$2890 \pm 80$</td>
<td>$1000 \pm 40$</td>
<td>$2640 \pm 50$</td>
</tr>
<tr>
<td>(MC)</td>
<td>$(2536 \pm 11)$</td>
<td>$(903 \pm 6)$</td>
<td>$(2420 \pm 11)$</td>
</tr>
<tr>
<td>$Z + \text{jets}$</td>
<td>$1380 \pm 50$</td>
<td>$379 \pm 11$</td>
<td>$13 \pm 4$</td>
</tr>
<tr>
<td>(MC)</td>
<td>$(1267 \pm 8)$</td>
<td>$(385 \pm 11)$</td>
<td>$(13 \pm 4)$</td>
</tr>
<tr>
<td>Single top (MC)</td>
<td>$86 \pm 8$</td>
<td>$36 \pm 7$</td>
<td>$98 \pm 9$</td>
</tr>
<tr>
<td>Diboson (MC)</td>
<td>$22 \pm 1$</td>
<td>$8.1 \pm 0.5$</td>
<td>$33 \pm 0.3$</td>
</tr>
<tr>
<td>Fake leptons</td>
<td>$17 \pm 10$</td>
<td>$17 \pm 8$</td>
<td>$19 \pm 10$</td>
</tr>
<tr>
<td>Total background</td>
<td>$1430 \pm 50$</td>
<td>$442 \pm 15$</td>
<td>$136 \pm 12$</td>
</tr>
<tr>
<td>Signal + background</td>
<td>$4400 \pm 100$</td>
<td>$1440 \pm 40$</td>
<td>$2770 \pm 80$</td>
</tr>
<tr>
<td>Data</td>
<td>$4102$</td>
<td>$1447$</td>
<td>$2848$</td>
</tr>
<tr>
<td>$\chi^{2}$/ndf</td>
<td>$35/34$</td>
<td>$31/34$</td>
<td>$58/49$</td>
</tr>
</tbody>
</table>
FIG. 8 (color online). Normalized distributions of the output of the boosted decision tree used to discriminate $\tau$ leptons from jets misidentified as $\tau$s, $\text{BDT}_j$, for $\tau$ candidates from $W+1$-jet and $W+2$-jets samples for leptons with opposite sign (OS), the distribution of opposite-sign leptons with the same-sign lepton distribution subtracted (OS–SS), and the extracted $\text{BDT}_j$ distributions ($K \cdot G$, see text) for gluon jets misidentified as $\tau$ candidates is shown. (a) OS, (b) OS-SS, (c) gluons jets.

With these background templates and MC signal template ($S$), a $\chi^2$ fit is performed with parameters to set the normalization of each template: $a \cdot OS + b \cdot G + c \cdot S$. The combined $e$ and $\mu$ channel results are obtained by fitting to the sum of the distributions. Comparisons of the template shapes of the $e$ and $\mu$ channel show they are identical within the uncertainties.

Two different $E_T$ regions, $20 \text{ GeV} \leq E_T \leq 35 \text{ GeV}$ and $35 \text{ GeV} \leq E_T \leq 100 \text{ GeV}$, are chosen such that each region has the same number of expected signal events. Three parameters are used to fit both regions simultaneously: the fraction of $\tau$ candidates in each $E_T$ region that are gluon jets and the total fraction of signal. In the fit the sum of signal and background must add up to the number of observed events in each $E_T$ region and the amount of signal in the two regions is constrained by the ratio predicted from MC simulation.

C. Fit results

The three-parameter fit was applied to MC samples to establish whether it can extract the known signal without bias. The MC samples are made with events from $\tilde{t}\tilde{t}$, $W+\text{jets}$, $Z+\text{jets}$, single top and diboson final states satisfying the data selection criteria. The MC samples were split into two, one used as the data to fit and the other to generate the templates for the fit. Figure 9 shows these MC fit results after correcting the background templates derived from $W+\text{jets}$ to account for the different $E_T$ distribution of the $\tau$ candidates in the expected background to $\tilde{t}\tilde{t} \rightarrow \ell\tau_{\text{had}}+\text{jets}$. The model uncertainty shown in Fig. 9 corresponds to the uncertainty of the templates in the fits to the data and used for ensemble tests. The ensemble tests show that no bias is introduced by the fitting procedure. The $\mu$ and $e$ channels are combined by adding together the distributions of both channels. The $\text{BDT}_j$ distributions can have multiple entries for an event as all $\tau$ candidates are considered. This has no impact on the $\tilde{t}\tilde{t} \rightarrow \ell\tau_{\text{had}}+\text{jets}$ signal as there is only one $\tau$ lepton decaying to hadrons in that channel.

The results of fitting the data are summarized in Table IV. $N_S^{\text{Fitted}}$ is the number of signal template events. $N_{\tilde{t}\tilde{t}}^{\text{Fitted}}$ is the number of observed $\tilde{t}\tilde{t} \rightarrow \ell\tau_{\text{had}}+\text{jets}$ events, obtained by subtracting the contributions from class 2 and class 3 backgrounds (see Sec. VIII B) from $N_S^{\text{Fitted}}$. The number of expected ($N_{\tilde{t}\tilde{t}}^{\text{MC}}$) is in good agreement with $N_{\tilde{t}\tilde{t}}^{\text{Fitted}}$. Figure 10 shows the final results using these $\mu$ and $e$ channel combined templates.

<table>
<thead>
<tr>
<th>Channel</th>
<th>Region 1</th>
<th>Region 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\tilde{t}\tilde{t} \rightarrow \ell\tau_{\text{had}}+\text{jets}$</td>
<td>$611.5 \pm 5.4$</td>
<td>$621.4 \pm 5.4$</td>
</tr>
<tr>
<td>$\tilde{t}\tilde{t} \rightarrow \ell\ell+\text{jets}$</td>
<td>$13.0 \pm 0.7$</td>
<td>$13.0 \pm 0.7$</td>
</tr>
<tr>
<td>$Z+\text{jets}$</td>
<td>$54.5 \pm 3.3$</td>
<td>$45.3 \pm 3.0$</td>
</tr>
<tr>
<td>Single top</td>
<td>$23.6 \pm 2.3$</td>
<td>$27.1 \pm 2.4$</td>
</tr>
<tr>
<td>Dibosons</td>
<td>$1.5 \pm 0.2$</td>
<td>$2.2 \pm 0.3$</td>
</tr>
<tr>
<td>Total</td>
<td>$705.2 \pm 6.8$</td>
<td>$709.5 \pm 6.8$</td>
</tr>
</tbody>
</table>

072005-12
distributions. The amount of $Z \rightarrow \tau\tau$ is normalized to the MC prediction. The data are well reproduced in all cases.

**IX. MEASURING CROSS SECTION AND BRANCHING RATIOS**

In the SM 100% of the top quark decays have one $W$ boson and a quark. Therefore the top quark branching ratios into channels with leptons and jets are determined by the $W$ decay branching ratios that have been measured with 0.3% precision (assuming lepton universality) [13] and are predicted by the SM with an uncertainty of order 0.1%. It is possible to derive the branching ratios into all decay modes using the number of $t\bar{t}$ events extracted in the previous sections assuming that the top quark branching ratios to leptons and jets add up to 100%. Any deviation from the $W$ branching ratios would be an indication of some process not predicted by the SM. The following notation is used for the top quark branching ratios:

(i) $B_{\mu}$: top quark branching ratio to $\mu\nu\mu(\nu_{\tau}) + X$,
(ii) $B_{\tau}$: top quark branching ratio to $e\nu_{e}(\tau) + X$,
(iii) $B_{\ell}$: top quark branching ratio to $\ell\nu_{\ell} + X$, with the $\ell$ lepton decaying hadronically,
(iv) $B_{j}$: top quark branching ratio to jets,
(v) $B_{\mu\tau} = B_{\mu} + B_{\tau}$.

The branching ratios $B_{\mu}$ and $B_{e}$ include events with leptonic $\tau$ decays.

With these definitions the following relations hold:

$$N_{\ell\ell} = 2\sigma_{t\bar{t}} \cdot B_{\ell} \cdot B_{j} \cdot \mathcal{L},$$

$$N_{\ell\tau} = \sigma_{t\bar{t}} \cdot B_{\ell} \cdot B_{\tau} \cdot \mathcal{L},$$

$$N_{\ell\tau} = 2\sigma_{t\bar{t}} \cdot B_{\ell} \cdot B_{\tau} \cdot \mathcal{L},$$

$$B_{j} + B_{\ell} + B_{\tau} = 1,$$

where $\sigma_{t\bar{t}}$ is the cross section for $t\bar{t}$ pair production and $\mathcal{L}$ is the integrated luminosity. These four equations with four unknowns can be solved to obtain:

<table>
<thead>
<tr>
<th>$N_{\ell\ell}^{\text{Fitted}}$</th>
<th>$N_{\ell\tau}^{\text{Fitted}}$</th>
<th>$N_{\ell\tau}^{\text{Fitted}}$</th>
<th>$N_{\ell\tau}^{\text{Fitted}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$20 &lt; E_T^\tau &lt; 35$ GeV</td>
<td>$611 \pm 5$</td>
<td>$76.2 \pm 3.5$</td>
<td>$17.1 \pm 1.1$</td>
</tr>
<tr>
<td>$35 &lt; E_T^\tau &lt; 100$ GeV</td>
<td>$621 \pm 5$</td>
<td>$69.5 \pm 3.3$</td>
<td>$17.6 \pm 1.1$</td>
</tr>
<tr>
<td>Combined $E_T^\tau$ bins</td>
<td>$1232 \pm 8$</td>
<td>$146 \pm 5$</td>
<td>$34.8 \pm 1.5$</td>
</tr>
</tbody>
</table>

**TABLE IV.** Numbers of events expected from MC simulation and fit results to the BDT$_{\ell}$ distribution using background and signal templates as described in Sec. VIII A. $N_{t\bar{t}}^{\text{MC}}$ is the expected number of $t\bar{t}$ events, $N_{\text{non-}}t\bar{t}$ is the number of $t\bar{t}$ expected from sources other than $t\bar{t}$, $N_{\text{lepton}}$ is the expected number of leptons misidentified as $t$ lepton. $N_{\text{Fitted}}$ is the number of events extracted with the signal template ($S$, see text) and $N_{\text{Fitted}}^{\text{Signal}} = N_{\text{Fitted}}^{\text{Signal}} B_{\text{non-t}} B_{\text{lepton}}$.
\[
B_j = N_{\tau j}/(N_{\tau j} + 2N_{\ell\ell} + N_{\ell\tau}),
\]
(11)

\[
B_{\ell} = 2N_{\ell\ell}/(N_{\tau j} + 2N_{\ell\ell} + N_{\ell\tau}),
\]
(12)

\[
B_{\tau} = N_{\ell\tau}/(N_{\tau j} + 2N_{\ell\ell} + N_{\ell\tau}),
\]
(13)

\[
\sigma_{\text{ATL}} \cdot \mathcal{L} = (N_{\ell\ell} + 2N_{\ell\tau} + N_{\ell\tau})^2/4N_{\ell\ell}.
\]
(14)

From the numbers of $t\bar{t}$ events given in Tables I–IV and the acceptances given in Table V the values are obtained for $N_{\ell\tau}$ and given in Table VI. The $N_{\ell\tau}$ are in units of events/pb$^{-1}$.

After solving for $B_{\ell}$ one can solve for $B_j$ and $B_{\mu}$ using ratios in the dilepton and the single-lepton channel:

\[
B_{\mu} = 2N_{\mu\mu}/B_j/N_{\mu}(e,j) \equiv a,
\]
(15)

FIG. 10 (color online). Fitted distributions of the $\tau$-jet discriminant BDT$_j$ in data using corrected background templates for (a) $20 \text{ GeV} \leq E_T \leq 35 \text{ GeV}$ and (b) $35 \text{ GeV} \leq E_T \leq 100 \text{ GeV}$. The model uncertainty is the statistical uncertainty of the templates used in the fits. (a) $E_T = 20 − 35 \text{ GeV}$, (b) $E_T = 35 − 100 \text{ GeV}$.

Events/5 GeV

\begin{center}
\begin{tabular}{|c|c|c|c|}
\hline
\text{Fig. 11 (color online).} & & &
\hline
\text{Transverse mass distributions ($m_T$) of $t\bar{t} \rightarrow \ell\tau$ had + jets events. The black points are data, the solid histograms} & & &
\hline
\text{the prediction based on the fits to the BDT$_j$ distributions. The jet background is the sum of all channels with jets misidentified as $\tau$ candidates } & & &
\hline
\text{normalized to the amount obtained from the fits to BDT$_j$ distributions. The multijet background is the estimated contribution} & & &
\hline
\text{from non-$t\bar{t}$ multijet processes and is included in the jet background. The model uncertainty is the statistical uncertainty of the templates} & & &
\hline
\text{used in the fits. KS is the value of the Kolmogorov-Smirnov goodness-of-fit test. (a) BDT$_j < 0.6$, (b) BDT$_j < 0.7$.} & & &
\hline
\end{tabular}
\end{center}
A rise in the range 4% from test-beam data, LHC collision data and simulations with those determined with simulated events selected with the same object criteria as used for the measurements over the course of data taking. The scale factors are applied to MC samples when calculating acceptances to account for any differences between predicted and observed efficiencies. The scale factors are evaluated by comparing the observed efficiencies with those determined with simulated Z boson events. Systematic uncertainties on these scale factors are evaluated by varying the selection of events used in the efficiency measurements and by checking the stability of the measurements over the course of data taking. The modeling of the lepton momentum scale and resolution is studied with reconstructed invariant mass distributions of $Z \rightarrow \ell^+\ell^-$ candidate events, and these distributions are used to adjust the simulation accordingly [36,37].

The jet energy scale (JES), jet energy resolution (JER), the jet energy scale (JES), jet energy resolution (JER), and their uncertainties are derived by combining information from test-beam data, LHC collision data and simulation. For jets within the acceptance, the JES uncertainty varies in the range 4%–8% as a function of jet $p_T$ and $\eta$ [39]. The $b$-tagging efficiency and its uncertainty is determined using a sample of jets containing muons [40]. The effect of all these variations on the final result is evaluated by varying each source of systematic uncertainty by $\pm 1\sigma$ in the MC-derived templates and fitting all the distributions with the new templates.

The uncertainty in the kinematic distributions of the $\ell\ell$ signal events gives rise to systematic uncertainties in the signal acceptance, with contributions from the choice of generator, the modeling of initial- and final-state radiation (ISR/FSR) and the choice of PDF set. The generator uncertainty is evaluated by comparing the MC@NLO and ALPGEN [29] predictions with those of POWHEG [20] interfaced to either HERWIG or PYTHIA. The PDF uncertainty is evaluated following the PDF4LHC recommendation [45]. An event-by-event weighting is applied to a default MC@NLO sample that uses the central value of CT10 [28], MSTW2008 [46] and NNPDF2.0 [47,48] sets are taken to estimate the systematic uncertainty due to the PDF. The uncertainty due to ISR/FSR is evaluated using the ALPGEN generator interfaced to the PYTHIA shower model, and by varying the parameters controlling ISR and FSR in a range consistent with experimental data [49].

The dominant uncertainty in this category of systematic uncertainties is the modeling of ISR/FSR. In addition there is an uncertainty in the $W + \text{jets}$ MC simulation due to the uncertainty in the heavy-flavor component of the jets. The systematic uncertainty from single top MC simulation has a negligible impact on the overall systematic uncertainty. The $\tau$ identification uncertainty is derived from a template fit to the BDT distribution from an enriched $Z \rightarrow \tau^+\tau^-$ data sample selected with the same $\mu$ and $\tau$ candidate requirements as the sample for this analysis, but with fewer than two jets and $m_T < 20$ GeV to remove $W + \text{jets}$ events. The background templates are the $W + 1$-jet OS and the gluon template used in the fit to the $\ell\ell$ data sample. The signal template is the BDT distribution from $Z \rightarrow \tau^+\tau^-$. The jet energy scale (JES), jet energy resolution (JER), and their uncertainties are derived by combining information from test-beam data, LHC collision data and simulation. For jets within the acceptance, the JES uncertainty varies in the range 4%–8% as a function of jet $p_T$ and $\eta$ [39]. The $b$-tagging efficiency and its uncertainty is determined using a sample of jets containing muons [40]. The effect of all these variations on the final result is evaluated by varying each source of systematic uncertainty by $\pm 1\sigma$ in the MC-derived templates and fitting all the distributions with the new templates.
The calculated systematic uncertainties for the inclusive cross section measured with the $\ell\tau_{\text{had}} + \text{jets}$ channel are given in Table VII. Table VIII gives the systematic uncertainties estimated when combining all channels. The uncertainty on the measured integrated luminosity is estimated to be 1.8% [51]. As expected the systematic uncertainties are substantially larger in the measurement of the cross section based on the $\ell\tau_{\text{had}} + \text{jets}$ channel alone than in the combination of all channels. The largest uncertainty in the combined cross-section measurement and in the branching ratio measurements is due to the JES uncertainty, followed by the MC generator and the uncertainty in the heavy-flavor component of $W + \text{jets}$. The uncertainties on the measured branching ratios are significantly smaller than on the measured inclusive cross section, as expected due to cancellations. $B_{\ell}$ has a larger systematic uncertainty than the other branching ratios due to uncertainties on $\tau$ identification that do not cancel in the ratios.

### XI. RESULTS

The inclusive $t\bar{t}$ cross section using only the $\ell\tau_{\text{had}} + \text{jets}$ channel is derived from the number of observed $t\bar{t} \rightarrow \ell\tau + \text{jets}$ events given in Table IV (Sec. VIII C):

$$\sigma_{t\bar{t}} = 183 \pm 9 \text{ (stat.)} \pm 23 \text{ (syst.)} \pm 3 \text{ (lumi.) pb}.$$  

This result is consistent with the previous ATLAS measurement, $186 \pm 25$ pb [15]. This measurement differs from the earlier one in that it uses only $\tau$s decaying into one charged hadron and a different background model to reduce the systematic uncertainties in the branching ratios. The results from combining all channels to extract the top quark branching ratios are given in Table IX. The measured cross

<table>
<thead>
<tr>
<th>Absolute uncertainties [pb]</th>
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<tbody>
<tr>
<td>$\mu$ uncertainty</td>
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<tr>
<td>$e$ uncertainty</td>
</tr>
<tr>
<td>Jet energy scale</td>
</tr>
<tr>
<td>Jet energy resolution</td>
</tr>
<tr>
<td>ISR/FSR</td>
</tr>
<tr>
<td>MC generator</td>
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<tr>
<td>PDF</td>
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<tr>
<td>$b$-tag</td>
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<tr>
<td>$\tau$ identification</td>
</tr>
<tr>
<td>$\tau$ background correction</td>
</tr>
<tr>
<td>Total</td>
</tr>
<tr>
<td>Luminosity</td>
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</tbody>
</table>

| TABLE VIII. Relative systematic uncertainties (%) for cross section and branching ratio measurements. The systematic uncertainties for $B_{\ell}$ and $B_{\mu}$ (not shown) are 100% correlated with the $B_{\tau}$ uncertainties and of the same size. The $e$ and $\mu$ uncertainties are the sum in quadrature of trigger, reconstruction and selection efficiency uncertainties. The MC generator uncertainty is the difference between POWHEG interfaced with PYTHIA and ALPGEN interfaced with HERWIG. HF stands for heavy flavor. |
|-------------------------------|-----|-----|-----|-----|
| $\sigma_{t\bar{t}}$          | 0.15| 0.6 | 0.5 |
| $B_{\tau}$                    | 0.15| 0.8 | 0.9 |
| $B_{\mu}$                    | 0.2 | $<0.1$ | 2.5 |
| $B_{\ell}$                    | 1.0 | $<1.0$ | $<0.1$ |
| $b$-tag                      | 0.3 | 1.0 | 1.5 |
| $\tau$ identification        | 0.5 | 0.5 | 0.5 |
| $\tau$ background correction | 0.2 | $<0.1$ | 2.5 |
| $W+\text{jets HF content}$   | $-1.0^{+0.7}_{-0.1}$ | $-1.1^{+2.3}_{-1.3}$ |
| Total                        | $-2.1^{+1.8}_{-0.1}$ | $-3.4^{+4.2}_{-7.1}$ |
| Luminosity                   | 1.8 | $<0.1$ | $<0.1$ |
section of $178 \pm 17$ pb is in good agreement with those obtained by ATLAS for individual channels [52–54]. The selection criteria for this measurement were optimized for the $\tilde{t}\tilde{t} \rightarrow \ell\tau_{\text{had}} + \text{jets}$ channel, which has the largest uncertainty, and then applied uniformly to all channels, ensuring no event overlap between them to exploit cancellation of systematic uncertainties in the ratios. This reduces the systematic uncertainties in the branching ratio measurements but it is not optimal for a cross-section measurement combining all channels. The systematic uncertainty on the inclusive cross section obtained by combining the samples used for this measurement is larger than the best ATLAS inclusive cross-section measurement [54], which achieved much smaller uncertainties because it was designed to minimize the systematic uncertainties related to jets, including the b-tagging efficiency and the jet energy scale. All cross-section measurements are in good agreement with the NNLO + NNLL theoretical prediction $177.3 \pm 9.0^{+4.6}_{-6.0}$ pb (calculated for a top mass of 172.5 GeV [24,55]). The branching ratios into leptons and jets are in good agreement with the SM prediction that the top quark decays 100% to $W + \text{quark}$. The precision of the measurements ranges from 2.3% for $B_j$ to 7.6% for $B_\ell$. The $B_\ell$ and $B_\mu$ include the leptonic decay of $\tau$ leptons while $B_\mu$ includes only the hadronic decays of $\tau$ leptons. There is no evidence for any non-SM top quark decay or for any non-SM process contribution that could affect these measurements. For example, the measured branching ratio $B_\tau$ will vary by more than the observed uncertainty if the branching ratio $\tilde{t} \rightarrow b\nu_\tau\tilde{\tau}$ times the $\tilde{t}\tilde{\tau}$ production cross section ($\sigma_{\tilde{t}\tilde{\tau}}$) is greater than 3% of $\sigma_{\tilde{t}\tilde{t}}$. The predicted $\sigma_{\tilde{t}\tilde{\tau}}$ depends on $\tilde{t}$ mass ($m_\tilde{t}$); it is equal to $\sigma_{\tilde{t}\tilde{t}}$ for $m_\tilde{t} = 120$ GeV and 12% of $\sigma_{\tilde{t}\tilde{t}}$ for $m_\tilde{t} = 180$ GeV [56].

### XII. CONCLUSION

The inclusive cross section for producing $\tilde{t}\tilde{t}$ pairs in $pp$ collisions at a center-of-mass energy of $\sqrt{s} = 7$ TeV at the LHC has been measured with the ATLAS detector and an integrated luminosity of 4.6 fb$^{-1}$ using the $\ell\tau_{\text{had}} + \text{jets}$ channel alone, as $\sigma_{\tilde{t}\tilde{t}} = 183 \pm 23$ pb, and as a single parameter to fit the channels $\ell + \text{jets}$, $\ell\ell' + \text{jets}$ and $\ell\tau_{\text{had}} + \text{jets}$, to be $178 \pm 17$ pb. These are in agreement with all other cross-section measurements obtained by ATLAS and CMS. All cross-section measurements are fully compatible with the NNLO + NNLL theoretical prediction. Top quark branching ratios have also been measured and found to be in good agreement with branching ratios predicted by the SM. The precision ranges from 2.3% for the decays to jets to 7.6% for the decays to $\tau\nu + \text{jet}$. There is no evidence for any non-SM process affecting these branching ratios.

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<table>
<thead>
<tr>
<th>Measured (top quark)</th>
<th>SM</th>
<th>LEP (W)</th>
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<tbody>
<tr>
<td>$\sigma_{\tilde{t}\tilde{t}}$</td>
<td>178 ± 3 (stat.) ± 16 (stat.) ± 3 (lumi.) pb</td>
<td>177.3 ± 9.0$^{+4.6}_{-6.0}$ pb</td>
</tr>
<tr>
<td>$B_j$</td>
<td>66.5 ± 0.4 (stat.) ± 1.3 (syst.)</td>
<td>12.72 ± 0.01</td>
</tr>
<tr>
<td>$B_\ell$</td>
<td>13.3 ± 0.4 (stat.) ± 0.5 (syst.)</td>
<td>12.72 ± 0.01</td>
</tr>
<tr>
<td>$B_\mu$</td>
<td>13.4 ± 0.3 (stat.) ± 0.5 (syst.)</td>
<td>7.0 ± 0.3 (stat.) ± 0.5 (syst.)</td>
</tr>
</tbody>
</table>
Taiwan; TAEK, Turkey; STFC, the Royal Society and Leverhulme Trust, United Kingdom; DOE and NSF, United States of America. The crucial computing support from all WLCG partners is acknowledged gratefully, in particular from CERN and the ATLAS Tier-1 facilities at TRIUMF (Canada), NDGF (Denmark, Norway, Sweden), CC-IN2P3 (France), KIT/GridKA (Germany), INFN-CNAF (Italy), NL-T1 (Netherlands), PIC (Spain), ASGC (Taiwan), RAL (UK) and BNL (USA) and in the Tier-2 facilities worldwide.

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