RNA packaging motor: From structure to quantum mechanical modelling and sequential-stochastic mechanism

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The bacteriophages of the \textit{Cystoviridae} family package their single stranded RNA genomic precursors into empty capsid (procapsids) using a hexameric packaging ATPase motor (P4). This molecular motor shares sequence and structural similarity with RecA-like hexameric helicases. A concerted structural, mutational and kinetic analysis helped to define the mechanical reaction coordinate, \textit{i.e.} the conformational changes associated with RNA translocation. The results also allowed us to propose a scheme of coupling between ATP hydrolysis and translocation which requires the cooperative action of three consecutive subunits. Here, we first test this model by preparing hexamers with defined proportions of wild type and mutant subunits and measuring their activity. Then, we develop a stochastic kinetic model which accounts for the catalytic cooperativity of the P4 hexamer. Finally, we use the available structural information to construct a quantum-chemical model of the chemical reaction coordinate and obtain a detailed description of the electron density changes during ATP hydrolysis. The model explains the results of the mutational analyses and yields new insights into the role of several conserved residues within the ATP binding pocket. These hypotheses will guide future experimental work.

\textbf{Keywords:} virus; assembly; molecular motor; density functional; mutagenesis; ATPase

\section*{Introduction}

During the life cycle of every virus, its genome needs to be condensed and enclosed within the confines of its capsid. Many RNA viruses utilize a mechanism in which the coat protein subunits and the genomic RNA co-assemble into the viral particle. A classical example is the tobacco mosaic virus in which protein subunits co-assemble with the ssRNA genome into a helical rod \cite{12,13}. However, dsDNA viruses typically package their genomes into preformed empty capsid precursors. A well studied example is that of bacteriophage \textit{\phi}29 in which the packaging is performed by a large molecular motor composed of capsid-bound dodecameric connector, several small RNA subunits and transiently associated ATPase subunits \cite{28,59,62}.

dsRNA bacteriophages of the \textit{Cystoviridae} family (phages \textit{\phi}6–\textit{\phi}14) utilize the latter mechanism and package ssRNA precursors into preformed procapsids (also called polymerase complexes, Figure 1(A)) \cite{26}. Cystoviruses possess three genomic segments (small, medium...
and large) which are packaged sequentially by the viral packaging motor P4 [52,55] (Figure 1(B)). P4 hexamers [33] reside at each of the five-fold vertices of the procapsid (Figure 1(A)) [27]. After successful packaging, the three ssRNAs are converted into dsRNA inside the viral procapsid by a virus-associated RNA-dependent RNA polymerase (protein P2) [11,25]. For each segment, the packaging process may be divided into three steps (Figure 1(D)): (i) recognition of the RNA pac site (a packaging signal) by a specific binding site on the surface of the viral capsid (i.e. major structural protein P1) [23,50], (ii) loading of the ssRNA into the packaging motor (most likely by a ring-opening mechanism) [43], (iii) unidirectional, 5′−3′ translocation of the captured ssRNA into the procapsid at the expense of ATP hydrolysis [24,38]. This mechanism is somewhat similar to those of dsDNA viruses, albeit the packaging machinery of the latter is more complex. While the architecture of cystoviruses is related to that of viruses of the Reoviridae family, packaging in the latter may differ considerably and involves several non-structural proteins [65]. For example, rotavirus protein NSP2, which is involved in packaging and exhibits helicase activity, is an octameric ATPase belonging to the HIT family and is not related to P4 [29].

The dome-shaped P4 hexamer has an overall structure and subunit fold similar to those of hexameric helicases (Figure 1(B)–(C)) [46,48]. The subunit structure has three domains: N-terminal apical dome, middle RecA-like ATPase core and C-terminal platform. Interestingly, the same basic fold was also found for a packaging ATPase domain from dsDNA bacteriophage T4 [64]. Thus, based on structure alone one may be tempted to speculate that all these motor proteins may share certain mechanistic features. In recent years, the P4 protein has become one
Figure 2. (A–B) Loop L2 movement in the central channel (C) Mechanism of sequential hydrolysis of ATP (yellow) and RNA (light green) translocation for three subunits viewed from within the central
of the best characterized hexameric helicases and, given the wealth of structural and biophysical information available, it constitutes a good model system for studying the mechano-chemistry of nucleic acid translocation. In this contribution, we first review the available structural and biochemical data together with the proposed model of the mechano-chemical coupling. Then, we present recent experimental and theoretical results and discuss their implications for the model.

P4s from bacteriophages φ6, 8, 12 and 13 have been characterized biochemically, crystallized [45,47] and high resolution structures were obtained for some (φ6, 12 and 13) (Figure 1(B)–(C)) [46,49]. These proteins can be expressed and purified in hexameric form and possess RNA-stimulated ATPase activity [36,38]. Isolated φ8 and φ13 P4 hexamers also exhibit helicase (duplex unwinding) activity in vitro [38]. The structurally conserved Rec-A like core encompasses five sequence motifs (H1, H1a, H2, H3 and H4) that are common to all superfamily 4 (SF4) helicases [39,46,48,60] (Figure 1(C)). The structural homology of P4 proteins extends to SF3 (human papilloma virus HPV E1, Simian virus 40 SV40 Large T antigen and LTag) and SF5 (Rho terminator) helicases, and to other proteins of the AAA⁺ family [37].

A molecular motor converts chemical energy into mechanical work which is manifested by directional motion. How such conversion is achieved by molecular motors is a matter of considerable interest and debate. In essence, the question is how the progress of the chemical reaction (e.g. ATP binding or hydrolysis in the active site of the ATPase) drives or is coupled to the motion along the mechanical coordinate (e.g. RNA translocation through the hexamer). Two possible scenarios can be envisioned: (i) progress of the chemical reaction leads to small structural changes and charge redistributions (on ~0.1 nm scale) in the active site that are directly amplified into larger, nanometre scale and movements, (ii) mechanical motion is stochastic and triggers the chemical reaction which in turn biases the movement in one direction. The former scheme is called a power stroke [66] while the latter constitutes a Brownian motor mechanism, of which the Brownian ratchet is a special case [7]. As we argue below, the proposed mechanism for P4 exhibits features of both the power stroke and the Brownian ratchet.

In order to understand the mechanism of a molecular motor the chemical and mechanical reaction coordinates must be defined and the rules governing coordinated progress and energy exchange between the two coordinates (i.e. mechano-chemical coupling) must be delineated. The first steps towards these goals have been accomplished for φ12 P4. X-ray crystallography revealed that movement of a molecular lever was associated with subtle changes in the nucleotide binding pocket during ATP hydrolysis [46] (Figure 2(A)). The lever consists of two connected elements, an α-helix 6 and a loop named L2. The end of the helix inserts into the ATP binding site of a neighbouring subunit, while the loop L2 protrudes into the central channel of the hexamer and returns back to the active site on the same subunit. The L2 loop contains at its centre a lysine (Lys241 in φ12 P4, Figure 2) which is conserved among most cystoviral P4s [39]. We have recently shown by site-directed mutagenesis that this positively charged side chain interacts with RNA [37]. The position of the L2 loop-α-helix 6 lever inside the central channel depends on the occupancy of the ATP binding site. In the presence of AMPcPP, an ATP analogue the lever is in an ‘up’ position while in the ADP-bound state it is in a ‘down’ position (Figure 2(A)). The position of the lever (‘up’ or ‘down’) correlates with the conformation of the P-loop (H1 motif also known as Walker A), which is seen either retracted from or inserted in the active site (Figure 2(B)). Finally, it was observed that in the ‘down’ position the side chain
of Arg279 (structurally equivalent to ‘arginine finger’ in GAPs and F1-ATPase) is inserted into the neighbouring active site, while it is retracted in the ‘up position’ (Figure 2(E)). In the apo hexamer (i.e. in the absence of bound nucleotide tri- and di-phosphates), the lever can assume both ‘up’ and ‘down’ positions suggesting that the nucleotide occupancy controls this movement. The lever movement was also shown to be essential for ATP hydrolysis [37]. Thus, the lever motion could be considered a good approximation for the mechanical reaction coordinate and is tightly coupled to ATP hydrolysis.

By a combination of site-directed mutagenesis and detailed structural analysis we have recently found that the lever motion is directed by the concerted interaction of two sensor residues, Asn234 and Ser252, with the γ-phosphate (γP) [37]. These sensors belong to helicase motifs H3 (Asn234) and H4 (Ser252), respectively, and are positioned at each end of the lever. They interact with ATP in two neighbouring ATP binding sites. Structural counterparts of these two residues in other helicases have been found to play an important role in the coupling between ATP hydrolysis and DNA binding [14,51,63,68].

The crystal structure of the S252A mutant in complex with ATP and Mg^{2+} revealed a transient state on the chemical reaction coordinate in which the arginine finger Arg279 is inserted into the catalytic pocket and interacts with the γP of the bound ATP (Figure 2(E)). Comparing this structure with that of R279A:ATP complex (Figure 2(E)) demonstrated that the arginine finger is not needed for the precise positioning of the γP inside the binding pocket and likely plays a role later during catalysis, i.e. in formation of the transition state (TS). The S252A structure also revealed that the hydroxyl group of Ser252 is essential for coordinating the catalytic water molecule as in this structure the catalytic water moves away from its usual position next to the γP (Figure 2(E), left). This observation could also explain why the S252A mutation renders P4 ATPase completely inactive [37].

Biochemical analysis revealed that the ATPase activity and cooperativity in P4 are increased in the presence of RNA. The cooperativity is catalytic rather than being due to cooperative binding of ATP and is mediated by sequential coordination of hydrolysis between three consecutive subunits (Figure 2(C)) [44]. All structural and biochemical results lead us to put forward a model in which L2 loops of three consecutive subunits bind to the RNA backbone in a staircase configuration similar to that recently revealed for the hexameric helicase E1 of HPV [19]. The three subunits cooperate in sequential hydrolysis (Figure 2(C)) [37]. At the beginning of the cycle (panel I), two subunits (i, i + 1) are in ATP ‘pre-hydrolysis or up’ state while the third (i − 1) is in the ADP ‘product or down’ state resulting from the previous hydrolysis cycle. The L2 loop of (i − 1) is bound to RNA in the ‘down’ position. In the ‘down’ position, the arginine finger Arg279 of the (i − 1) is inserted into the (i) active site and triggers or stimulates hydrolysis [37]. The arginine finger insertion constitutes the structural basis for sequential hydrolysis. After hydrolysis at subunit i, the Pi (inorganic phosphate, HPO_4^{2−}) is released from the active site and the absence of γP/Pi further stabilizes the ‘down’ position of the preceding (i − 1) lever through the loss of Ser252 side chain interaction with the γP. In this way, the lever motion is being rectified by hydrolysis in the neighbouring active site, i.e. this part of the mechanism is akin to the Brownian ratchet. Pi release from active site of (i) also changes the energy landscape for the lever at subunit i due to the loss of interaction between Asn234 side chain and the γP (Figure 2(B)–(D)). Hence the lever moves to the new, energy favourable ‘down’ position and propels the bound RNA down the central channel (panel II). This, in turn, may be considered a power stroke albeit the down motion remains fairly stochastic in nature. At the end of the cycle, the (i − 1) subunit detaches from RNA, ADP is released and exchanged for ATP to enter another round.

The central idea in this model, the cooperation of three consecutive subunits, has been established and supported through kinetic measurements. While it is in general agreement with the
structural and mutation analyses, a direct verification is still lacking. One way to probe this model is to generate hexamers harbouring increasing number of mutant (inactive) subunits and measure their specific activity. The current model predicts that the activity would be negligible after reaching the level of three inactive subunits per hexamer. Here, we describe the preparation and activity of such mixed \( \Phi 12 \) P4 hexamers harbouring subunits with a mutated arginine finger (R279A).

Modelling the overall kinetics of hexameric helicases is complicated by their high cooperativity and by the number of possible states. Purely kinetic models have now been designed and solved for two hexameric helicases [1,41] however their correspondence with the available structural information is hard to fathom. A structure based approach, i.e. molecular dynamics (MD), offers, in principle, a complete description of the motion [20] but the computational costs for a hexameric system become prohibitive when simulating events on a time scale relevant to enzyme kinetics (i.e. ms). Simplified models based on Brownian dynamics may be used in lieu of full MD description when the trajectory of the mechanical reaction coordinate can be extracted or extrapolated from the structural data [10,66]. Here, we use a version of this approach, the discrete event stochastic algorithm [21,22], to simulate the kinetic cooperativity of P4.

Another drawback of MD and related techniques is that they cannot adequately describe the breaking or the forming of covalent bonds, i.e. the phosphodiester bond in ATP [67]. As the latter involves electron density redistributions, it must be described at the quantum mechanical (QM) level. Although QM methods are severely restricted in terms of the size of the system (number of atoms) they can handle, recent developments of density functional theory (DFT) brought within reach the computation of ATPase reaction mechanisms [15,16]. Here, we demonstrate that by judicious use of structural information it is possible to select all important residues in the vicinity of the triphosphate and to obtain a self-consistent model of the active site. This model is then used to map the course of phosphodiester hydrolysis, i.e. the chemical reaction coordinate including the structure and energy of the TS. The roles of the conserved residues in the reaction are examined at the QM level and compared with the results of site-directed mutagenesis.

The results presented here can be viewed as examples of our current efforts and do not necessarily provide a conclusive picture. Furthermore, greater integration of the theoretical approaches with experimental results is required before we can take full advantage of the models and employ them to test and propose hypotheses.

**Experimental**

We prepared hexamers with varying number of mutant subunits by *in vitro* re-assembly. This approach required several steps: (1) wild type (wt) and mutant hexamer dissociation into subunits, (2) re-assembly and (3) separation of species with a defined number of wt subunits.

In order to aid step 3, a hexa-histidine tag was added to the C-terminus of the wt protein P4 from bacteriophage \( \Phi 12 \). The wt gene was PCR-amplified from pPG-27 [47] (pET-32a) with primers containing Nde1 site upstream and Hind3 site downstream and sub-cloned into the Nde1-Hind3 sites of plasmid pET-22b which has T7 promoter and 6 X His Tag 15 base-pairs downstream of the Hind3 site. The stop codon TGA of P4 was removed and following primers were used: forward GCCTAA-CATATG-ATCCATCTGTACGACGCA (Nde1); reverse TAATAA-AAGCTT-GTTGGAGGTGAGACGACG (Hind3). The resulting plasmid pHB1 was sequenced and introduced into *Escherichia coli* expression strain BL21 (DE3) [70]. The C-terminally tagged protein (P4His) was expressed at 17°C in a similar fashion to wt [47]. P4His was purified following a procedure previously described for his-tagged \( \Phi 8 \) P4 protein [6]. The molecular weight of purified protein and presence of his-tag was verified by mass spectrometry.
Hexamer dissociation was accomplished by diluting P4 protein (2 mg/ml final concentration) into a high salt buffer in the absence of divalent cations and nucleotide phosphates (TNE buffer: 20 mM Tris–HCl, pH 8.0, 0.5 M NaCl, 5 mM EDTA) [34]. The high ionic strength was important for stabilization of the subunits throughout the slow dissociation (48 h at 25°C) [70]. Re-association was done by mixing the wt P4His with an untagged arginine finger mutant R279A in the desired proportion. The association products were further enriched in the amount of the desired species by affinity chromatography on Ni-NTA agarose column (HisTrap, GE Healthcare, Freiburg, Germany). Structural integrity of re-assembled hexamers was checked by size-exclusion chromatography coupled with dynamic light scattering [35]. The proportion of wt subunits was estimated from staining of the R279A and wt P4his bands on SDS-PAGE gel using densitometry (Figure 3(A), note that the addition of 6xHis caused P4His to migrate significantly slower). Activity of the purified, mixed hexamers was measured by the EnzChek phosphate release assay as previously described [42].

Theory

Kinetic model of catalytic cooperativity

A simplified kinetic model contained six equivalent ATP binding sites flanked by their corresponding levers (a6 helix-L2 loop) (Figure 4(A) left). ATP and ADP binding and dissociation rate constants were unaffected by the state of neighbouring subunits and lever position (i.e. purely kinetic cooperativity). Since inorganic phosphate (Pi) does not seem to inhibit the rate of hydrolysis, we assumed that Pi release is fast [44]. Hence we only considered three states for each active site (Figure 4(A) right): empty (E), ATP-bound enzyme substrate (ES), ADP-bound enzyme product (EP). The only reliable set of nucleotide binding and dissociation rate constants was measured for the fluorescently labelled 2'-MANT-3'-dATP and MANT-ADP analogues. These analogues exhibit higher affinity and thus the apparent Michaelis constant of 2'-MANT-3'-dATP is lower than that of ATP [42,44]. Under the steady-state conditions, ADP does not accumulate and hence we set the ADP re-binding constant to zero (k6 = 0).

Very little is known about the magnitudes of intrinsic rate constants for the chemical reaction (k3 and k4). From results obtained for related hexameric helicases, this step is likely to be faster than other steps, including the phosphate release step [32]. In the absence of RNA, the overall turnover of P4 is relatively slow (0.8 s⁻¹ for ATP and 0.07 s⁻¹ for 2'-MANT-3'-dATP [44]) and hence there must be a rate-limiting step prior to the chemical reaction. Given the results of structural and mutational analysis, we think it is fair to assume that the insertion of the arginine finger is the rate-limiting step and a prerequisite for hydrolysis. Hence the intrinsic rate constant, when this step has been fulfilled (i.e. when the lever position in the preceding subunit reached the intermediate state, see below), was set k3 = 5000 s⁻¹. This means that we consider this step to be almost instantaneous compared with other steps when the prerequisite slower mechanical motion has been achieved. Conversely, in the absence of Arg279 insertion we set k3 = 0. For simplicity, we set k4 = 0, since under the steady-state conditions Pi release was assumed to be fast, making the reaction virtually irreversible.

In an ideal case, the mechanical part of the cycle, i.e. the lever position, should be modelled as stochastic motion on energy landscapes similar to those shown in Figure 2(D). The exact shape and parameters of these landscapes are not known at the present. Hence, we simplified the trajectory by three points (states) for which there is a structural evidence (Figure 4(A) right): the initial ‘up’ position, as seen in the P4:AMPcPP:Mg²⁺ crystal structure (up), an intermediate position (in) which is concomitant with the insertion of the arginine finger and triggers hydrolysis in the neighbour (e.g. configuration similar to that in the S252A:ATP:Mg²⁺ structure.
Figure 3. Incorporation of increasing number of arginine finger mutant (R279A) subunits into hexamers. 
(A) Separation of hexamers by Ni-affinity chromatography. Note the slower migration of wt P4His due to 
the addition of the 6xHis and the intervening linker residues. (B) Dependence of the Michaelis constant on 
the number of wt subunits (from initial mixing ratio). (C) Dependence of the turnover number on the
Figure 4. (A) Schematics of the ATP binding sites interconnecting mechanical levers (L2) and the key residues that control the lever position depending on γP presence (left). In the right panel, the overall scheme of reaction is given for the levers (up, in and down states) and ATP binding sites belonging to three consecutive subunits (S, ATP; ES, substrate complex; EP, product complex; P, product). The stimulating effect on hydrolysis in the next neighbour is shown as green arrows while slowing down the lever motion is depicted as red arrows. RNA binding to the neighbouring subunits causes synchronization of motion of their levers. This is modelled as an increase of the lever motion rate constant depending on the neighbouring lever position (magenta arrow). (B) Simulated relative activity as a function of MANT-ATP concentration (left) and occupancy of states during the simulation (right) in the absence of RNA. Apparent $K_m = 0.41$ and $k_{\text{max}} = 163$. (C) As in panel B but in the presence of RNA, $K_m = 0.27$ and $k_{\text{max}} = 249$. In each left panel, the dashed magenta curve represents a simple hyperbolic fit (Michaelis–Menten non-cooperative kinetics) while the black curve is fit to Hill equation $V = k_{\text{max}}*[\text{ATP}]^n/(\text{[ATP]}^n + K_m^n)$.

Number of wt subunits. The expected turnover numbers for the three-in-row and four-in-row models are shown as solid and dashed curves, respectively. Error bars (SD) were estimated from several independent determinations. (D) Enumeration of different microstates for the six macrostates (from Ref. [44]). Active microstates for the three-in-row model are highlighted.
Figure 5. Structural snapshots along the reaction coordinate obtained by QM modeling. QM optimized model of ES state with all atoms shown (A) and with omitted methyl groups and unimportant water molecules (B). Structure close to the TS state (C) and in product state EP with Pi still bound (D). Energy along the reaction coordinate for the wt (solid line and filled symbols) and R279A mutant (dotted line, empty symbols). The ES and EP states were fully optimized without any constraints while the bond length
in Figure 2(E) but closer to the TS structure, see next section on QM modelling for details), and
the ‘down’ position, as seen in the P4:ADP:Mg\(^{2+}\) structure (down). The inter-conversion rates for
the lever at subunit \(i\) were modulated by the nucleotide binding state at this (through interaction
of Asn234 with the \(\gamma\)P) and the following subunit (\(i + 1\), via Ser252 interaction with the \(\gamma\)P).
The presence of these interactions slowed the ‘down’ motion ten-fold while their absence slowed
the ‘up’ motion (Figure 4(A) right). In the absence of nucleotides, we assumed fast inter-
conversion rates since reasonable results were obtained with \(k7–10 \sim 50–100\) s\(^{-1}\). Obviously,
lever motion is the least determined feature of the model and needs further improvements,
e.g. by extracting energy landscapes from molecular mechanics simulations or estimating the
lever mobility constants from experiment such as NMR spectroscopy.

RNA binds to Lys241 at the tip of the moving lever [37] and was modelled as a link between
two consecutive levers (Figure 2(D)). Motion of one lever facilitates, via the RNA link, the
neighbouring lever to adopt the same position, \textit{i.e.} accelerates the lever motion in one direction
ten-fold. Once again this is a somewhat arbitrary number since there is no information on the
kinetics of RNA binding and correlation of lever positions. RNA unbinding from one subunit
was followed by its binding to a neighbour (Figure 2(D)).

The overall scheme of coupled reactions is summarized in Figure 4(A). Obviously, such a
coupled system would be difficult to solve exactly and hence we employed the stochastic
discrete step simulation, as originally devised by Gillespie [21]. This scheme employs variable
time steps and is implemented in a Matlab shell which allows for easy modifications and
improvements. Further acceleration of simulation was accomplished by implementing the core
algorithm in C as a subroutine. Steady-state kinetics rates were obtained from linear fits of
product concentrations versus time for 1000 simulation steps at each of the 30 different ATP
concentrations, without and with RNA present. Using the stochastic simulation approach, we
can in the future extend the scheme to include Brownian motion of the lever in a measured or
computed potential.

\textit{QM modelling of the chemical reaction}

\textit{Model of the enzyme–substrate complex}

The model was constructed by combining the available crystallographic structures of the P4
active site [37,46]. The missing hydrogen atoms, which are not visible in the X-ray structure at
2 Å resolution, were subsequently added by applying the correct stereochemistry. The resulting
system was truncated to a computationally tractable model by a careful selection of the
important residues while including as a large part of the reaction centre as possible. For
comparison, much smaller regions are usually treated quantum mechanically in the QM/MM
calculations [15,17].

In more detail, the model of the active site was constructed by combining two crystal
structures of bacteriophage \(\phi\)12 motor protein P4. Structure 1W49 (PDB id. 1W49) (Protein
Data Bank: [9]) presents P4 protein in complex with an ATP-analogue, AMPcPP and Mg\(^{2+}\) [46].
The 2VHQ (PDB id. 2VHQ) structure is a mutant P4 in which Ser252 was replaced with alanine,
and complexed with ATP and Mg\(^{2+}\) [37]. This combination was devised to obtain ATP in an
approximation of its native, hydrolysable form, since in the wt complex the bound AMPcPP

along the reaction coordinate was held constant during the TS state optimization. Molden, version 4.5 beta
[57], gOpenMol, version 3.00 [8,40] and Maestro (Copyright 1999–2007 Schrödinger, LLC) packages
were employed for visualization of the results. Available in colour online.
is in an inactive configuration (see comparison in Figure 2(E)). Figure 5(A) illustrates the merged structure in which the ATP–enzyme complex is ready for hydrolysis. The arginine finger (Arg279), which was also taken from 2VHQ, is in the hydrolysis stimulating, inserted position, i.e. close to the γP. Ser252 and the catalytically important water molecule were taken from 1W49 structure since they were missing from the mutant [37]. The P-loop amino acids (Lys136 and Thr137) were poorly resolved in the 2VHQ structure, and hence taken from the 1W49 wt structure. All other amino acids were taken from 2VHQ structure to get the model as close as possible to the situation just before ATP hydrolysis (Figure 5(A)).

The most conserved water molecules in the active site were found with the help of UCSF Chimera modelling environment [53]. The active sites of the three subunits in the asymmetric unit were aligned with each other in both crystal structures and water molecules present in at least two subunits were included in the model. In total, eight water molecules were found within the active centre (Figure 5(A)). Hydrogen atoms were added using an automatic procedure implemented in Maestro (v.8.0) and further checked manually in order to assure proper ionization forms of the amino acids, assuming the local pH in the active site to be between 7 and 8, as in the experiments or in vivo conditions.

To obtain a computationally feasible system, several amino acids were truncated at a location unlikely to directly influence the reaction: The backbone regions and hydrocarbon (aliphatic) portions of all amino acids, except the P-loop (Lys136 and Thr137), were replaced with methyl groups. The resulting truncated system (Figure 5(B)) was then used in all calculations.

**DFT and computational details**

In the DFT, the electron cloud is described by one electron density function, which includes all electrons of the system, rather than one wave function for each individual electron [31]. Thus, a 3N-dimensional N-electron problem is reduced to a three dimensional problem and makes DFT calculations fast and scaleable. The price to pay for this advantage is that the exact form of the density functional is not known and various approximations are necessary.

The quantum-chemical calculations were done with Turbomole software package [3], versions 5.8. The RI-J (resolution of the identity) and MARI-J (multipole accelerated resolution of the identity) DFT schemes were employed to accelerate the calculations [58]. Split-valence polarization (def-SVP) basis sets were used for all atoms [56], except magnesium, for which the more appropriate triple-zeta valence polarization set was used [69]. Corresponding auxiliary basis sets for RI approximation were used [18]. Most calculations were done with Perdew–Burke–Ernzerhof (PBE) functional and confirmed with the hybrid B3LYP (Becke 3-parameter exchange functional with Lee–Yang–Parr correlation) functional. Default code parameters were used except for the finer numerical integration accuracy in DFT (gridsize m4). Relaxed convergence criteria were used for obtaining the complete reaction coordinate with reasonable numerical accuracy.

**Results and discussion**

**A minimum of three subunits in a row cooperate in hydrolysis**

Mutation of the arginine finger Arg279 to alanine (R279A) causes severe reduction of the P4 ATPase activity (>1000-fold) [37]. We have incorporated increasing numbers of R279A subunits into the hexamer by mixing it with wt his-tagged subunits (P4His). Separation of the hexamers according to the increasing number of P4His subunits is demonstrated in Figure 3(A). Nickel affinity purification and gel staining also demonstrated that the proportion of the wt
subunits in the peak fraction follows the initial mixing ratio (not shown). Hence, we subsequently prepared hexamers by simply mixing different proportions of dissociated subunits followed by size-exclusion chromatography to remove unassembled subunits or residual aggregates. The ratio of wt and mutant subunits was verified by SDS-PAGE as described above.

The steady-state kinetic parameters (apparent Michaelis constant, $K_m$, and the turnover number $k_{\text{cat}}$ in the presence of 1 mM poly(rC)) for hexamers at different mixing ratios are shown in Figure 3(B)–C. With the increasing number of mutated, inactive subunits both $k_{\text{cat}}$ and $K_m$ were affected. Although the R279A mutation does not affect the ATP affinity [37] $K_m$ increased roughly linearly with the number of inactive subunits incorporated (Figure 3(B)). This is clear manifestation of catalytic (kinetic) cooperativity.

As expected from the proposed cooperativity model (i.e. three consecutive subunits cooperate, three-in-row model), $k_{\text{cat}}$ decreased to almost background noise levels when the number of incorporated mutated subunits was more than three. The observed residual activity is due to binomial distribution of the number of inactive subunits in mixed hexamers (hexameric macrostates 0–6 in Figure 3(D)) at each mixing ratio (probabilities related to the initial mixing ratio $p = [\text{wt}]/(\text{wt} + [\text{R275A}]), q = 1 - p$). Assuming that the mutation does not affect hexamer assembly (the structure of R279A mutant is essentially wt [37]), each macrostate is composed of equally populated microstates which are the configurations of inactive subunits within the hexamer (Figure 3(D)). For a given mechanism, certain microstates are active while others are not [44]. For example, the active configurations for the three-in-row mechanism are highlighted in Figure 3(D). By counting the number of active configurations for each macrostate and weighting them by the binomial distribution of macrostates, we obtained the expected activity as a function of number of wt subunits (see [44] for details). Two models, corresponding to the three-in-row and the four-in-row model, respectively, are compared with experimental data in Figure 3(C). At low numbers of mutant subunits, the experimental points follow the four-in-row model while at higher numbers they are closer to the three-in-row model. This suggests that during fast hydrolysis and processive translocation (i.e. at ATP saturation levels) up to four subunits in row may cooperate. The hexamer can however still work with a minimum of three subunits in a row, as suggested previously [37,44]. More sophisticated models are needed to fully account for the experimental data.

**Kinetic simulation of stochastic-sequential cooperativity**

One of the hallmarks of P4 cooperativity is the apparently high Michaelis constant ($K_m > K_d$) in the absence of RNA which becomes comparable to the equilibrium dissociation constant ($K_d$) when RNA is bound and translocated. In addition, cooperativity is clearly discernible in the presence of RNA and is accompanied by a modest increase of $k_{\text{cat}}$ (three-fold for ATP and about ten-fold for MANT-ATP). Note that RNA has no effect on ATP or ADP binding kinetics and equilibrium [44]. Standard kinetic models do not account for this behaviour. Here, we present a stochastic-sequential model (Figure 4(A)) which predicts with reasonable accuracy the expected decrease in $K_m$ and increase in $k_{\text{cat}}$ and cooperativity (compare Figure 4(B),(C)). However, the activity enhancement was less than expected for MANT-ATP (note MANT-ATP was used in lieu of ATP for which no binding rate constants are known at the present time). The discrepancy is not surprising given that some of the kinetic constants in the model could only be estimated.

Comparison of lever state distributions throughout the entire course of the simulation provided additional insight (Figure 4(B),(C), right panels). There was a dramatic difference in the pattern of lever motion and therefore hydrolysis rate in absence or presence of RNA. Without RNA only isolated, stochastic ‘islands’ of sequential hydrolysis are apparent and the subunits spend most of the time waiting for the right constellation of binding sites and levers to re-start.
sequential hydrolysis. RNA binding introduces coupling of lever motion between neighbouring subunits and as a consequence hydrolysis becomes sequential and processive. The proposed simulation scheme constitutes a plausible starting model. Since variations in the estimated rate constants and their couplings yield different results we need to obtain further constraints from experiment.

**QM model of the chemical reaction coordinate**

**Structure of ATP-bound state**

While the ‘pre-hydrolysis’ model structure after optimization at the QM level correlates well with the equivalent atomic structure based model, the packing of amino acids in the active site in the former is slightly denser than that in the latter. This may be due to missing protein environment around the active centre. In both the atomic structure based model and the QM optimized model structure, Ser252 coordinates a water molecule which then attacks the γP during the reaction. In the QM optimized model (Figure 5(A)), Lys136 side chain in the P loop was closer to the β-phosphate (βP) than in the atomic structure based model. Similarly, Glu160, which coordinates another important water molecule (the so called assisting water), moved closer to the γP following the rearrangement of water molecules in the vicinity of γP during optimization. Also, Arg279 and Arg272 moved closer to the γP and rotated around their side chain axes. The conformation of ATP remained almost the same as in the 2VHQ structure. All three phosphates form coordination bonds with the magnesium ion, which is also coordinated by one water molecule and the oxygen of Thr137 hydroxyl group.

**Reaction path**

A common mechanism of ATP hydrolysis is a nucleophilic attack of a water molecule on the γP [2,15]. Hence, we initiated the reaction by moving ‘in silico’ the catalytic water molecule (highlighted in Figure 5(A)) towards the γP and optimizing the system at each H2O-Pγ distance. The energy profile along this reaction coordinate exhibited a typical maximum due to formation of a high-energy TS followed by a sharp drop to the lower energy products (Figure 5(E)). The TS energy barrier was 90 kJ/mol, somewhat higher than the experimental value (63 kJ/mol) obtained for the related δ6 [30] and other ATPases. The model yielded also structural information about the TS and the product state with Pi still present within the binding pocket. Both of these states are short-lived and thus hard to study experimentally. Starting from the reactant state in Figure 5(B), the reaction proceeded via a TS in which the γP was in a typical penta-coordinated configuration (Figure 5(C)) [2]. Following the TS, the γP separated abruptly from the βP while still being coordinated to Mg2⁺ (Figure 5(D)). After the γP separation, Lys136 lowered the high negative charge of ADP by donating a proton to the βP (Table 1).

In addition, the computational method offers insights which are not easily obtainable from experimental methods, such as unravelling the detailed path to the TS and the proton relay involved in generation of the nucleophilic agent, the hydroxyl anion, from the attacking water molecule. The nucleophilicity of the water molecule was increased by an assisting water molecule that accepts a proton from the attacking water and becomes a positively charged hydronium ion. The hydronium ion in turn sheds the extra proton to the carboxylate of Glu160 which becomes a neutral carboxylic acid (Figure 5(D) and Table 1). The formation of the hydroxyl anion was concomitant with its approach to the γP. The assisting water molecule remained hydrogen-bonded to the oxygen on the P1 which originated from the attacking water (Figure 5(D)).
Role of arginine fingers in catalysis

An arginine finger is a residue which, at various points along the catalytic cycle, inserts into the active site of many GTPases and ATPases and generally accelerates the hydrolytic reaction. Arginine fingers were first identified in small GTPases (G-proteins) where they are provided in trans by activator proteins (GAPs) [4]. For G-proteins, the catalytic role of arginine fingers has been firmly established [4,5]. Since arginine fingers always coordinate the $\gamma$P of NTP, it has also been proposed that in hexameric rings they act as $\gamma$P sensors which relay the information from one NTP binding site to the adjacent subunit and therefore promote sequential conformational changes [19,61].

P4 has two arginine residues in the active site, Arg272 and Arg279 (Figure 5(A)). Although Arg272 is essential for ATPase activity [37], it does not fulfil the role of a finger since it is not being inserted into the active site during the cycle [46]. It probably does not act as a sensor either. Indeed, the computational model confirmed that it has a catalytic role instead of sensory one. Arg272 is important for the formation of the attacking hydroxyl ion and coordinates the assisting water molecule (Figure 5(C)).

Arg279 side chain is inserted into the active site during the course of the reaction and it interacts with the $\gamma$P. ATP binding kinetic is not affected by the R279A mutation [37] indicating a catalytic rather than sensory role. Indeed, the computational model demonstrated that the Arg279 side chain offers a positive charge to the negatively charged exiting $\text{P}_1$. Further insight was gained by computing the reaction path for the R279A mutant. Compared to wt, the energy barrier almost doubled (Figure 5(E)) and the product state was less stable, i.e. making the intrinsic hydrolysis an unfavourable reaction. These results indicate that Arg279 may play a dual role, the first is in the TS formation and the second in stabilizing the product state before $\text{P}_1$ release. While the stabilization of $\text{P}_1$ may slow down its release, which incidentally is the rate-limiting step for many helicases, it may allow the chemical reaction to proceed within the centre making it slightly energetically favourable. It remains to be seen whether the $\text{P}_1$ release is assisted by further motion of the arginine finger towards the $\alpha\text{P}$ and $\beta\text{P}$ with which it interacts in the crystal structure of the product P4:ADP: Mg$^{2+}$ state.

Conserved serine within helicase motif H4 has dual role in the mechanism

The hydroxyl group of Ser252, which is positioned at the end of the moving helix 6, is coordinating the attacking water molecule at all stages of the hydrolysis reaction (Figure 5).

<table>
<thead>
<tr>
<th>Residues</th>
<th>ES</th>
<th>TS</th>
<th>EP</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ser252</td>
<td>-0.06</td>
<td>-0.01</td>
<td>-0.01</td>
</tr>
<tr>
<td>Glu160</td>
<td>-0.71</td>
<td>-0.69</td>
<td>-0.04</td>
</tr>
<tr>
<td>Arg272</td>
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<td>0.80</td>
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<td>Arg279</td>
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<td>0.79</td>
<td>0.78</td>
</tr>
<tr>
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<td>-0.18</td>
<td>-0.17</td>
</tr>
<tr>
<td>Lys136</td>
<td>0.76</td>
<td>0.83</td>
<td>0.12</td>
</tr>
<tr>
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<td>-0.03</td>
<td>-0.03</td>
<td>-0.06</td>
</tr>
<tr>
<td>Asp189</td>
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<td>-0.71</td>
<td>-0.70</td>
</tr>
<tr>
<td>Mg$^{2+}$</td>
<td>1.73</td>
<td>1.76</td>
<td>1.73</td>
</tr>
<tr>
<td>ATP phosphates</td>
<td>-3.53</td>
<td>-3.73</td>
<td>-3.63</td>
</tr>
<tr>
<td>$\alpha\text{P} + \beta\text{P}$</td>
<td>-1.99</td>
<td>-2.70</td>
<td>-2.08</td>
</tr>
<tr>
<td>$\gamma\text{P}$</td>
<td>-1.54</td>
<td>-1.03</td>
<td>-1.55</td>
</tr>
<tr>
<td>Ribose</td>
<td>0.28</td>
<td>0.29</td>
<td>0.29</td>
</tr>
</tbody>
</table>

ES, enzyme substrate complex; TS, transition state; EP, enzyme product complex.
The hydrolysis reaction and movement of helix 6 are thus connected via Ser252. In the simulation Ser252 hydroxyl group followed the attacking water deeper into the active site and helped to align the catalytic water for nucleophilic attack (Figure 5(C)). After reaching the TS, the serine withdrew from the active site (Figure 5(D)) but remained coordinated to the bound P\textsubscript{i}. Ser252 is likely to retreat to its resting position during or after the release of P\textsubscript{i}. As the backbone of Ser252 follows the side chain motion this could provide a mechanism by which the energy from P\textsubscript{i} release is harnessed to effect mechanical motion, e.g. a small movement and turning of Ser252 could cause the whole helix 6 to pivot like a see-saw. This mechanism may also work in the opposite direction, triggering hydrolysis by a coordinated insertion of Ser252 hydroxyl and Arg279 finger upon helix 6 motion. Taken together, these results suggest both sensory and catalytic role for Ser252 in P4 mechanism. It is tempting to propose that this dual role is conserved among all the helicases with structurally related serine or histidine residues [17].

In conclusion, we have devised a concerted experimental and theoretical approach to investigate the complex mechanisms behind the cooperativity and mechano-chemical coupling of hexameric molecular motors. Whilst some of the theoretical tools are still rather rudimentary, e.g. the stochastic kinetic model, others are more mature and provide insights inaccessible to experiment. Theoretical tools, hand-in-hand with new experimental approaches will play essential role in understanding these fascinating molecular machines.

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**References**


