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(MINOS Collaboration)

1Argonne National Laboratory, Argonne, Illinois 60439, USA
2Department of Physics, University of Athens, GR-15771 Athens, Greece
3Physics Department, Benedictine University, Lisle, Illinois 60526, USA
4Brookhaven National Laboratory, Upton, New York 11973, USA
5Lauritsen Lab, California Institute of Technology, Pasadena, California 91125, USA
6Department of Physics, Cavendish Laboratory, University of Cambridge, Madingley Road, Cambridge CB3 0HE, United Kingdom
7Universidade Estadual de Campinas, IF-UNICAMP, CP 6165, 13083-970, Campinas, SP, Brazil
8Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100039, China
9APC–Collège de France, 11 Place Marcelin Berthelot, F-75231 Paris Cedex 05, France
10Physics Department, Columbia University, New York, New York 10027, USA
11Fermi National Accelerator Laboratory, Batavia, Illinois 60510, USA
12High Energy Physics Lab, Cambridge University, Cambridge, Massachusetts 02138, USA
13Physics Division, Illinois Institute of Technology, Chicago, Illinois 60616, USA
14Physics Department, Indiana University, Bloomington, Indiana 47405, USA
15Institute for High Energy Physics, Protvino, Moscow Region RU-140284, Russia

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The complete 5.4 kton MINOS far detector has been taking data since the beginning of August 2003 at a depth of 2070 meters water-equivalent in the Soudan mine, Minnesota. This paper presents the first MINOS observations of $\nu_\mu$ and $\bar{\nu}_\mu$ charged-current atmospheric neutrino interactions based on an exposure of 418 days. The ratio of upward- to downward-going events in the data is compared to the Monte Carlo expectation in the absence of neutrino oscillations, giving $R_{\text{data}}^{\text{up}/\text{down}}/R_{\text{MC}}^{\text{up}/\text{down}} = 0.62^{+0.19}_{-0.14} \text{(stat.)} \pm 0.02 \text{(sys.)}$. An extended maximum likelihood analysis of the observed $L/E$ distributions excludes the null hypothesis of no neutrino oscillations at the 98% confidence level. Using the curvature of the observed muons in the 1.3 T MINOS magnetic field $\nu_\mu$ and $\bar{\nu}_\mu$ interactions are separated. The ratio of $\pi_\mu$ to $\nu_\mu$ events in the data is compared to the Monte Carlo expectation assuming neutrinos and antineutrinos oscillate in the same manner, giving $R_{\pi_\mu/\nu_\mu}^{\text{data}}/R_{\pi_\mu/\nu_\mu}^{\text{MC}} = 0.96^{+0.38}_{-0.25} \text{(stat.)} \pm 0.15 \text{(sys.)}$, where the errors are the statistical and systematic uncertainties. Although the statistics are limited, this is the first direct observation of atmospheric neutrino interactions separately for $\nu_\mu$ and $\bar{\nu}_\mu$.

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I. INTRODUCTION

Over the course of the past ten years the deficit of muon neutrinos from cosmic-ray showers in the atmosphere has been firmly established by the Super-Kamiokande experiment [1–6] and confirmed by the MACRO [7] and Soudan 2 [8] experiments. The favored interpretation of the data is $\nu_\mu \leftrightarrow \nu_\tau$ neutrino oscillations. Recent results from the Super-Kamiokande experiment [9] provide direct

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aNow at Department of Physics, National Technical University of Athens, GR-15780 Athens, Greece.
bNow at GE Healthcare, Florence SC 29501, USA.
cNow at Division of High Energy Physics, U.S. Department of Energy, Germantown, MD 20874, USA.
dNow at APC–Collège de France, 11 Place Marcelin Berthelot, F-75231 Paris Cedex 05, France.
eNow at Math, Science and Technology Department, University of Minnesota–Crookston, Crookston, MN 56716, USA.
fNow at Physics Department, Royal Holloway, University of London, Egham, Surrey, TW20 0EX, United Kingdom.
gNow at Holy Cross College, Notre Dame, IN 46556, USA.
hNow at Department of Radiation Oncology, Beth Israel Medical Center, NY, NY 10003, USA.
iNow at Fermi National Accelerator Laboratory, Batavia, IL 60510, USA.
jNow at Lincoln Laboratory, Massachusetts Institute of Technology, Lexington, MA 02420, USA.
kNow at Physics Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA.
lDeceased.
mNow at Department of Physics, Pennsylvania State University, University Park, PA 16802, USA.
nNow at Nuclear Nonproliferation Division, Threat Reduction Directorate, Los Alamos National Laboratory, Los Alamos, NM 87545, USA.
oNow at Stanford Linear Accelerator Center, Stanford, CA 94309, USA.
evidence for atmospheric neutrino oscillations and yield
best fit oscillation parameters of \((\Delta m^2_{23}, \sin^22\theta_{23}) = (0.0024 \text{ eV}^2, 1.0)\), where \(\Delta m^2_{23} = |m^2_3 - m^2_2|\). Results from the K2K experiment [10] provide further confirmation of the \(\nu_{\mu} \leftrightarrow \nu_{\tau}\) oscillation hypothesis.

The 5.4 kiloton (kt) mass of the recently constructed MINOS (Main Injector Neutrino Oscillation Search) far detector [11] is much less than the ~25 kt fiducial mass of the Super-Kamiokande detector. However, it does possess one unique advantage, namely, it is the first large deep underground detector to have a magnetic field. This allows studies of neutrino flavor oscillations for neutrinos and antineutrinos separately by identifying the charge of muons produced in charged-current \(\nu_{\mu}\) and \(\bar{\nu}_{\mu}\) interactions. A separate measurement of \(\nu_{\mu}/\bar{\nu}_{\mu}\) oscillations could provide constraints on CPT violating models [12,13] which have been invoked to accommodate simultaneously the solar, atmospheric and LSND [14] neutrino oscillation data. It should be noted that a number of recent studies have indicated difficulties with the CPT violating models (see for example [15]). Nevertheless, a direct measurement of \(\nu_{\mu}/\bar{\nu}_{\mu}\) oscillations is of interest. In addition, MINOS is unique in its ability to provide an accurate measurement of the neutrino energy and direction for all contained-vertex \(\nu_{\mu}\) charged-current (CC) interactions.

This paper presents first results on atmospheric neutrinos from the MINOS experiment. Here, only results from \(\nu_{\mu}/\bar{\nu}_{\mu}\) CC events with neutrino interaction vertices contained inside the detector volume are considered; results from events where the neutrino interacts in the surrounding rock will be the subject of a separate publication. The data used were recorded between August 2003 and February 2005 and correspond to a live time of 418 days giving an exposure of 6.18 kiloton years (4.54 kiloton years fiducial). The data are compared to the expectation in the absence of neutrino oscillations and the favored hypothesis of \(\nu_{\mu} \leftrightarrow \nu_{\tau}\) oscillations with \(\Delta m^2_{23} = 0.0024 \text{ eV}^2\) and \(\sin^22\theta_{23} = 1.0\). The first direct results showing charge-separated \(\nu_{\mu}\) and \(\bar{\nu}_{\mu}\) atmospheric neutrino interactions are presented.

II. THE MINOS DETECTOR

The MINOS far detector is located at a depth of 2070 meters-water-equivalent (mwe) in the Soudan mine, Northern Minnesota. The far detector is a steel-scintillator sampling calorimeter consisting of two supermodules (SM) separated by a gap of 1.1 m. The detector consists of octagonal planes of 2.54 cm thick steel followed by planes of 1 cm thick extruded polystyrene scintillators and a 2 cm wide air gap. The first and second SMs are comprised of 248 and 236 scintillator planes, respectively. Each SM is magnetized to an average value of 1.3 T by a 15 kA current loop which runs through the coil hole along the detector central axis and returns below the detector. Each scintillator plane is made up of 192 strips of width 4.1 cm and of length between 3.4 m and 8.0 m depending on position in the plane. The strips in alternating planes are oriented at \(\pm 45^\circ\) to the vertical thereby providing two orthogonal coordinates.\(^1\) The scintillation light is collected using wavelength shifting (WLS) fibers embedded within the scintillator strips. The WLS fibers are coupled to clear optical fibers at both ends of a strip and are read out using 16-pixel multi-anode photomultiplier tubes (PMTs). The signals from eight strips, separated by approximately 1 m within the same plane, are optically summed (multiplexed) and read out by a single PMT pixel. The multiplexing pattern is different for the two sides of the detector, which, for a single hit, enables the resulting eightfold ambiguity to be resolved. For all types of events, the ambiguities are efficiently resolved in software using additional information from timing and event topology.

The detector is optimized for detecting beam neutrinos coming from the direction of Fermilab. For the study of atmospheric neutrinos the planar structure presents a particular problem: cosmic-ray muons traveling almost parallel to the scintillator planes can penetrate deep into the detector by traveling in the steel or air between the planes. To reject this source of background a scintillator veto shield surrounds the upper part of the main detector. The veto shield is constructed from the same scintillator modules as used in the main detector but with the orientation of strips aligned along the \(z\) axis. The veto shield comprises a “ceiling” section above the detector, consisting of two scintillator layers, and “wall” sections along each of the two sides of the detector formed from a single scintillator layer.

A. Data acquisition and trigger

The output signals from each PMT pixel are digitized and time-stamped (with a 1.5625 ns precision) by the VME-based front-end electronics. The signals from the pixels are digitized by 14-bit analogue-to-digital converters (ADC) when the dynode signal from the PMT exceeds a programmable threshold, corresponding to approximately one third of a photo-electron (PE). To reduce the data flow, the pedestal corrected signals are only written to the data acquisition output buffers if two out of 36 channels on the same readout board are above threshold. These 36 channels correspond to the readout on one side of the detector from a contiguous group of either 20 or 24 planes. The raw data rate is approximately 8 MB s\(^{-1}\). The raw data are transferred to a personal-computer-based trigger farm where the data are divided into blocks bounded by regions of 100 clock ticks (156 ns) or more where no detector activity has

\(^{1}\)The MINOS right-handed coordinate system has the \(z\) axis defined along the detector axis pointing away from Fermilab and the \(y\) axis vertical. The alternating scintillator planes provide measurements of the \(U\) and \(V\) coordinates which are related to \(x\) and \(y\) by \(U = \frac{1}{\sqrt{2}}(x + y)\) and \(V = \frac{1}{\sqrt{2}}(y - x)\).
been recorded. The primary trigger algorithm, applied to these blocks of data, requires there to be activity in at least four planes out of any contiguous group of five planes. The veto shield is read out in the same manner as the main detector except that the two out of 36 requirement is not applied and the dynode threshold is set to a level corresponding to approximately one and a half photo-electrons.

The MINOS far detector front-end electronics and data acquisition system are described in detail in [16,17].

**B. Detector calibration**

A minimum ionizing particle crossing at normal incidence to a plane gives a combined signal of approximately ten photo-electrons registered by the PMTs at the two ends of the strip. The detector is calibrated using both a dedicated light-emitting diode (LED) system [18] and cosmic-ray muons. The ADC to PE calibration is performed using the LED system and the cosmic-ray muon sample is then used to give a uniform response across the detector. From studies of cosmic-ray muons in the MINOS detector [19], the current uncertainty in the PE calibration is 5%. Cosmic-ray muons are also used to calibrate the recorded times. After calibration, a single hit timing resolution of approximately 2.3 ns is achieved. The timing calibration tracks all hardware changes.

**III. DATA AND MONTE CARLO SAMPLES**

The data described in this paper were recorded in the 18 month period from August 2003 to February 2005. Only data taken when the MINOS far detector, including the veto shield, was fully operational are used. The final data sample corresponds to a live time of 418 days giving an exposure of 6.18 kiloton-years (4.54 kiloton-years fiducial).

The selection of contained-vertex neutrino interactions was optimized using a GEANT 3 [20] simulation of the MINOS detector. For the simulation of atmospheric neutrino events the 3D flux calculation of Bart et al. [21] was used (Bartol 3D). The NEUGEN3 program [22] was used to simulate the neutrino interactions (cross sections and hadronic final states). The earlier 1D flux calculation from the Bartol group [23] (Bartol 1D) and the 3D calculation of Battistoni et al. [24] were used to assign systematic uncertainties. The response of the MINOS detector to electrons, muons, and hadrons has been studied in a test beam at the CERN PS using the 12.5 ton MINOS calibration detector [25]. The test beam detector was constructed and read out in the same manner as the MINOS far detector. The interactions of hadronic particles are modeled with the GCALOR package [26], which is found to give a reasonable description of low energy hadronic interactions in the MINOS calibration detector [27], rather than the default version of GHEISHA (see [20] and references therein). The “SLAC version” [28] of GHEISHA, which also provides a reasonable description of the test beam data, is used as an alternative model for hadronic interactions. A Monte Carlo (MC) sample of atmospheric neutrino interactions corresponding to over 1000 live years was generated and used to optimize both the reconstruction algorithms and the event selection criteria. Two large cosmic-ray muon background samples were generated: a sample of $19 \times 10^6$ events full spectrum (corresponding to approximately 280 days live time) and a further $2 \times 10^6$ events with $E_\mu < 2$ GeV (corresponding to a live time of 4.1 years) as lower energy events are an important component of the cosmic-ray muon background to the contained-vertex atmospheric neutrino selection. A 10% uncertainty on the normalization of the cosmic-ray background is assigned. The error reflects the different normalization obtained when normalizing to the entire cosmic-ray sample or normalizing to just those cosmic-ray muons which stop in the detector (these form the main background to the event selection described below). It should be noted that for the results presented in this paper the cosmic-ray background in the selected event sample is estimated from data. The 10% uncertainty in the cosmic-ray normalization is only used when comparing data and Monte Carlo samples at various stages in the event selection.

**A. Flux normalization and systematic uncertainties**

The theoretical prediction for the atmospheric neutrino event rate has large uncertainties from the primary cosmic-ray flux, hadron production models, and neutrino interaction cross sections. The analysis of the Soudan 2 $\nu_e/\bar{\nu}_e$ data [8] indicates that the combined prediction of the Bartol 3D model [21] and the NEUGEN3 [22] neutrino cross section model should be scaled by $0.88 \pm 0.07$ [29], where the error is statistical and it is implicitly assumed that atmospheric electron neutrinos are not oscillating. This normalization result is compatible with the results from a fit to the Soudan 2 data including oscillations. The MINOS and Soudan 2 detectors are located in the same mine (i.e. at the same geomagnetic latitude) and both are constructed from steel. Consequently, for the analysis presented here the Soudan 2 scale factor $0.88 \pm 0.07$ is used to correct the combined event rate predictions from the Bartol 3D flux model and the NEUGEN3 neutrino interaction model. An additional 5% uncertainty is added in quadrature to that estimated by the Soudan 2 Collaboration to account for differences arising from the different energy thresholds (300 MeV in the case of Soudan 2 compared to $\sim 500$ MeV for MINOS). Finally an additional 2.5% uncertainty is assigned to account for the different phases in the solar cycle for the Soudan 2 and MINOS data sets [30]; because of the relatively high neutrino energy threshold the selected atmospheric neutrino rate in MINOS depends only weakly on the phase in the solar cycle. The resulting total
systematic uncertainty on the expected event rate is estimated to be 10%.

IV. EVENT RECONSTRUCTION

The MINOS detector is optimized for beam neutrinos originating from Fermilab. Because of the curvature of the Earth, beam neutrinos enter the detector from below the horizontal at an angle of 3.3° with respect to the z axis. The standard MINOS reconstruction software has been developed for these events. The analysis presented here uses reconstruction software optimized for atmospheric neutrinos [31].

The first stage of the event reconstruction removes the eightfold ambiguity in the association of raw hits to strips. This is performed utilizing information from both strip ends. For cosmic-ray muons, an average of 99% of the recorded pulse height is associated with the correct strip. At this stage the data are in the form of two 2D event views \( U - z \) and \( V - z \). An example event display of a cosmic-ray muon is shown in Fig. 1. Tracks and showers are reconstructed independently in each view; the two views are then matched to obtain a three-dimensional event. For cosmic-ray events that leave hits in both the veto shield and main MINOS far detector, the root-mean-square (rms) difference in times recorded in veto shield and the detector is 4 ns, allowing association of veto shield hits (indicated in Fig. 1) to activity in the main detector.

A charged-current muon neutrino event is, in general, reconstructed as a muon track and a hadronic shower. A typical 1 GeV muon will traverse approximately 25 planes at normal incidence. Reconstructed tracks are required to consist of at least 8 planes (corresponding to a minimum energy of 0.4 GeV). For muons which start and stop within the detector volume the muon momentum is determined from a range with a resolution of approximately \( \sigma_{p^2}/p^2 = 0.06^2 + (0.045/p)^2 \) for muons traveling at normal incidence to the detector planes (where \( p \) is measured in GeV/c). The first term is dominated by fluctuations in energy loss and the second is dominated by sampling. For events where the muon exits the detector, the muon momentum is obtained from the curvature of the track in the magnetic field. For the selected CC atmospheric \( \nu_\mu/\tau_\mu \) interactions, where the momentum is determined from curvature, the average momentum resolution is approximately \( \sigma_{p^2}/p^2 = \left[0.1^2 + (0.3/p)^2\right] \) GeV\(^{-2} \) (where \( p \) is measured in GeV/c). However, the resolution obtained from individual events depends strongly on how much of the trajectory of the muon is observed before it exits the detector and on the orientation of the trajectory relative to the local magnetic field. The hadronic energy is obtained by summing the pulse height in a shower which is spatially associated with the start of the track. The energy scale is obtained from Monte Carlo samples using the GCALOR [26] model of hadronic showers, which from the test beam results is found to provide a good description of the detector response to single \( \pi^\pm \) and protons [27]. The hadronic energy resolution is approximately \( \sigma_E/E = 0.55/\sqrt{E} \), where \( E \) is measured in GeV.

For the study of atmospheric neutrinos it is necessary to determine whether the reconstructed track is upward or downward going. A relativistic normal incidence particle traverses ten planes in approximately 2 ns which, when compared to the single hit resolution of 2.3 ns, is sufficient to identify the direction of most selected events with little ambiguity. The sense of the direction of muon tracks is determined by comparing the hit times along the reconstructed track with the hypotheses that it is either upward or downward going (assuming that the particle is traveling at the speed of light). The rms deviations of hit times about each of the two hypotheses are calculated, RMS\(_{\text{UP}}\) and RMS\(_{\text{DOWN}}\). The hypothesis with the smallest rms is chosen. In addition, the magnitude of RMS\(_{\text{UP}}\)-RMS\(_{\text{DOWN}}\) provides a measure of the quality of the direction determination. To test the performance of the algorithm a sample of stopping cosmic-ray muons is used (all of which are
tracks due to the limited number of planes crossed. For high momentum tracks, which typically leave the detector, the charge identification efficiency decreases as only the limited curvature at the start of the track is measured.

V. EVENT SELECTION

At a depth of 2070 mwe the cosmic-ray muon rate is approximately 50 000 events per day in the MINOS detector. This rate should be compared to the expected signal rate of $0.54 \pm 0.05$ atmospheric CC $\nu_\mu/\bar{\nu}_\mu$ interactions per day, where the uncertainty is from the 10% uncertainty in the expected event rate (discussed in Sec. III A). In order to achieve a signal-to-background ratio of ten-to-one it is necessary to identify the signal events efficiently while reducing the background by a factor of $10^6$. The event selection is designed to identify both fully contained (FC) and partially contained (PC) $\nu_\mu/\bar{\nu}_\mu$ events. In FC events the entire event is contained within the fiducial volume. In PC events the neutrino vertex is within the fiducial volume but the produced muon exits the detector.

A. Preselection

Candidate CC $\nu_\mu$ neutrino interactions are required to have a reconstructed track passing some basic quality requirements. The majority of the background is rejected by event containment requirements which are applied at both the hit and reconstructed track level. The sense of the track direction (up/down) is determined from timing as described previously. The start of the track, which is considered to be the neutrino interaction vertex, is required to lie within the detector fiducial volume. The fiducial volume is defined as the octagonal region which is at least 50 cm from the detector edges in the xy plane and at least five planes from the start and end of either SM. In addition, the region within 40 cm of the axis of the coil hole, which has a diameter of 25 cm, is excluded from the fiducial volume. This cut is enlarged to 1 m in the first and last ten planes of the detector. The event sample is subdivided into FC and PC events depending on whether the end of the track also lies within the fiducial region.

Event containment cuts are also made at the hit level to reduce the sensitivity to possible reconstruction errors where not all hits are correctly associated with the reconstructed track. For this purpose, the fiducial volume requirement of 50 cm from the detector edges is relaxed to 30 cm. In order to apply the containment cuts at the hit level it is necessary to convert the two-dimensional coordinates of a single hit into a point in space. This conversion is achieved by using the mean value of the orthogonal ($U/V$) coordinate in the surrounding two planes. Hits out-
side the fiducial volume are then assigned to the nearest octagonal edge/SM end. Edges/ends with summed pulse height equivalent to more than six PEs outside the fiducial region are tagged as being uncontained. Candidate FC (PC) events are required to have no (one) such region. The containment cuts reject approximately 99.9% of the cosmic-ray background while retaining 77% of CC $\nu_\mu/\bar{\nu}_\mu$ interactions in the detector volume. The inefficiency for signal events is primarily a fiducial effect; the selection of FC and downward-traveling PC CC fiducial volume before leaving a detectable signal. The such events can penetrate a significant distance into the traveling in the steel or air between the scintillator planes, the detector at small angles to the detector planes. By samples arise from steep cosmic-ray muons which enter thePC event selection criteria are optimized separately for upward- and downward-going events as the backgrounds for the two categories are very different. To ensure the track direction is well determined, candidate PC events are required to have a track of at least 1 m in length and which consists of hits in at least ten planes.

B. Fully contained and downward partially contained event selection

The dominant backgrounds in the FC and downward PC samples arise from steep cosmic-ray muons which enter the detector at small angles to the detector planes. By traveling in the steel or air between the scintillator planes, such events can penetrate a significant distance into the fiducial volume before leaving a detectable signal. The selection of FC and downward-traveling PC CC $\nu_\mu/\bar{\nu}_\mu$ interactions aims to greatly reduce this background and proceeds in four stages:

(i) Cosmic-ray rejection (trace cut).—The reconstructed track is extrapolated back to the outside of the detector and the distance traversed in the direction perpendicular to the detector planes is calculated, $\Delta z$. Events with small values of $\Delta z$ correspond to steep tracks which when extrapolated to the detector edge traverse only a few scintillator planes. Figure 4 shows the $\Delta z$ distribution for MC cosmic-ray muons and CC $\nu_\mu/\bar{\nu}_\mu$ interactions. Events are rejected if $\Delta z < 0.5$ m. Figure 4 also shows the $\Delta z$ distribution for data which is in reasonable agreement with the MC expectation.

(ii) Event topology.—About half of the remaining background consists of cosmic-ray muon tracks that bend in the magnetic field and turn over in the $z$ direction. Such events will leave hits in two separate positions in a particular plane. In addition, these events typically have large pulse height in the plane where the muon turns around in $z$. This category of background event is rejected using the pulse-height weighted deviations of the hits in the $U - z$ and $V - z$ views from the fitted track. The pulse-height weighted mean, $\langle \Delta_{UV} \rangle$, and the pulse-height weighted rms deviation of hits from the track, $\langle \Delta_{UV}^2 \rangle^{1/2}$, are calculated. Events are rejected if there is large scatter about the track, $\langle \Delta_{UV}^2 \rangle^{1/2} > 0.5$ m, or if the pulse-height weighted mean deviation from the track lies significantly above the reconstructed track, $\langle \Delta_{UV} \rangle > 0.25$ m. These empirically determined cuts are applied separately to the hits in both the $U - z$ and $V - z$ views. In addition, the event vertex is defined as the first hit on the track taking the highest end (largest $y$) as the start of the track. The maximum displacement from the event vertex of the hit strips which lie within ±4 planes of the event vertex is found, $\Delta R_{\text{max}}$. Events are rejected if $\Delta R_{\text{max}} > 1.25$ m.

(iii) Vertex pulse height/direction.—After the topology cut, the signal-to-background ratio is approximately 1:5. The remaining background consists of steep cosmic-ray muons which travel nearly parallel to the scintillator planes and therefore tend to give a large pulse-height signal in a single plane near the beginning of the track. These events are often poorly reconstructed due to the difficulties of reconstructing tracks for events at small angles to the detector planes. Figure 5 shows, for signal and background, the total pulse height in the event vertex region, $Q_{\text{vert}}$, plotted against the cosine of reconstructed zenith angle at the highest end of the track$^3$ and the modulus of reconstructed track direction cosine with respect to the $z$ axis, $|\cos \theta_z|$.

$^3$The zenith angle, $\theta_{\text{zen}}$, is defined as $\pi$ minus the angle between the reconstructed track direction and the local vertical (the $y$-axis). Negative values of the cosine of the zenith angle correspond to tracks which are reconstructed as upward going.
The vertex pulse height is defined as the maximum number of PEs observed in a single plane within ±0.0006 planes of the event vertex (defined above). The background is characterized by being steep and having large $Q_{vtx}$. Events are rejected if they have $Q_{vtx} > 300$ PEs. Steep events, defined as having $|\cos \theta_{zen}| > 0.7$ and $|\cos \theta_{zen}| < 0.5$, are required to satisfy $Q_{vtx} > 100$ PEs. The above event charge/direction cuts are not applied to events with track lengths of greater than 20 detector planes, as the steep background events tend to cross relatively few planes.

(iv) Veto shield.—The cuts listed above result in a signal-to-background ratio of approximately 1:2. Additional background is removed by rejecting events with activity in the veto shield within a ±100 ns window around the event time, resulting in a signal-to-background ratio of approximately 20:1.

C. Upward partially contained events

The background to the upward-going PC event selection is dominated by cosmic-ray muons which stop in the detector and are reconstructed as upward rather than downward going. The cuts to remove this source of background are based on timing information and identify events which are unambiguously upward going. The event selection cuts fall into two categories:

(i) Event topology.—For the upward PC selection, the relatively small number of badly reconstructed events passing the preselection are removed using a subset of the topology cuts employed in the FC/downward PC analysis. Events are rejected if $Q_{vtx} > 300$ PEs or $\Delta R^{max} > 1.25$ m.

(ii) Track timing rms.—The expected times of hits on the track are calculated for the hypotheses of an upward-going and a downward-going track. The rms scatter of the difference between observed and expected hit times for these two hypotheses is used to identify upward-going events. The event is required to be consistent with the upward hypothesis and significantly more compatible with the upward hypothesis than the downward hypothesis: $\text{RMS}_{\text{UP}} < 4.33$ ns and $\text{RMS}_{\text{UP}} - \text{RMS}_{\text{DOWN}} < -1.66$ ns (these numbers should be compared to the single hit timing resolution of 2.3 ns). Figure 6 shows the effect of the main timing cut, namely...
events in data, consistent within 1 standard deviation with the MC expectation of 149 events using the veto shield cuts. The final veto shield requirement rejects 149 events.

The numbers of events surviving at different stages in event selection are listed in Table I. Reasonable agreement between data and Monte Carlo samples is seen at each stage. The final veto shield requirement rejects 149 events in data, consistent within 1 standard deviation with the MC expectation of 170 ± 24, where the uncertainty is from normalization and MC statistics. For the results in this paper, the cosmic-ray muon background in the combined FC and downward PC event sample is estimated from data rather than relying on MC. From the 149 events rejected by the veto shield cuts the remaining background is estimated to be 4.4 ± 0.4(stat.) ± 0.3(sys.) events using the veto shield efficiency of 97.1 ± 0.2% (described below) and taking account of the expected number of neutrino events rejected by the veto shield requirements.
up-down symmetric, systematic uncertainties are calculated for the MC expectation for the ratio of upward-going to downward-going events. The total uncertainty on the selection efficiency for atmospheric neutrino events is estimated to be 3.3%. The contribution to the systematic uncertainty on the up-down ratio from experimental effects is estimated to be 3.1%. The contributions to these systematic errors are discussed in detail below.

Veto shield.—The efficiency of the veto shield cut is determined directly from data in two independent ways. First, a sample of cosmic-ray muons that stop in the detector and have $|\cos \theta_{\text{zen}}| > 0.5$ is selected. These events occupy a similar region of phase space to the background. The veto shield cut rejects $(97.06 \pm 0.03)\%$ of this sample. A second estimate of the veto shield efficiency is obtained by relaxing the event selection cuts until the sample is dominated by background (i.e. an expected signal fraction of less than 2%). The veto shield cut rejects $(96.2 \pm 0.2)\%$ of this sample which, when the expected signal (assuming $\Delta m^2_{23} = 0.0024 \text{ eV}^2$) is taken into account, leads to an estimated veto shield efficiency of $(97.3 \pm 0.2)\%$. From these two tests the veto shield efficiency is estimated to be $(97.1 \pm 0.2)\%$, where the central value is taken from the high statistics stopping muon sample and a systematic error of 0.2% is added reflecting the difference between the two methods.

The fraction of signal events rejected due to accidental coincidences with hits in the veto shield is estimated by overlaying veto shield hits obtained from special minimum bias data taking runs onto Monte Carlo atmospheric neutrino events. The estimated fraction of signal events rejected due to spurious veto shield hits is $(2.2 \pm 0.4)\%$, where the error represents systematic time dependent variations. In addition, from Monte Carlo studies it is estimated that $(0.3 \pm 0.1)\%$ of the selected signal downward-going events will be rejected due to hits in the veto shield associated with the neutrino interaction.

Hadronic response.—The event selection efficiency depends on the detector response to hadrons and consequently the hadronic interaction model used. Comparisons of GCALOR and GHEISHA show no evidence for any significant difference in overall selection efficiency or reconstructed up-down ratio. The GCALOR model is found to provide a good description of the response of the detector to single hadrons. Systematic errors of 2.5% on the selection efficiency and 3.0% on the up-down ratio are assigned; in both cases the estimates reflect the Monte Carlo statistical precision of the comparison.

Scintillator light calibration.—The overall calibration of the MINOS far detector is currently known to 5%. The MC response is tuned to agree with cosmic-ray muon data and has a corresponding 5% uncertainty. Because the selection cuts use pulse-height information, this leads to systematic errors of 0.6% on the selection efficiency and 0.3% on the up-down ratio.

Timing calibration/resolution.—The timing calibration for each scintillator strip is determined from data in a manner that tracks hardware changes. The uncertainty on the timing calibration for the individual strips is 0.3 ns, i.e. significantly less than the single hit resolution of 2.3 ns. The effect on the selection is negligible. A more significant effect is that the single hit resolution in MC is better than that in the data, 2.2 ns compared to 2.3 ns. This is due to an incomplete simulation of the electronics readout. For this reason the times of the Monte Carlo hits are smeared by a Gaussian of width 0.7 ns. The difference between the selection efficiencies before and after this smearing are compared. The overall selection efficiency for the smeared MC is reduced by 1.0%. The effect on the up-down ratio is small (0.1%). These differences are used as estimates of the systematic uncertainties.

Muon $dE/dx$.—One of the main cuts in the event selection is the requirement that tracks leave hits in at least eight scintillator planes. Consequently, the event selection efficiency is sensitive to the Monte Carlo simulation of muon energy loss. The simulation of muon energy loss depends on the underlying simulation of the physics processes and the knowledge of the chemical composition of the MINOS detector. An uncertainty of 3% in the muon range is assumed. These uncertainties result in systematic uncertainties of 1.7% on the selection efficiency and 0.3% on the up-down ratio.

Neutron background.—The background from cosmic-ray induced neutrons has been studied using a GEANT 4 simulation [32] of muon nuclear interactions in the rock and is found to be negligible. In a Monte Carlo sample corresponding to 4 times the data exposure no neutron event passed even the early stages of the event selection.

VI. RESULTS

From the 418 days exposure considered in this paper, 107 candidate contained events are selected. The 107 selected events are consistent with both the expectation of $127 \pm 13$ events assuming no neutrino oscillations, and with the expectation of $96 \pm 10$ events assuming $\Delta m^2_{23} = 0.0024 \text{ eV}^2$ and $\sin^2 2\theta_{23} = 1.0$. The background contribution from cosmic-ray muons, $4.4 \pm 0.5$, is obtained from data as described above. In addition, there is an expected background of $4.5 \pm 0.5$ from the combination of neutral current interactions and $\nu_e/\bar{\nu}_e$ CC interactions. The error in the MC expectation is dominated by the uncertainty on the neutrino flux \times interaction cross section which is estimated to be 10%. Table II gives a breakdown of the various contributions to the expected event rates.

The $xy$ positions of the reconstructed neutrino interaction vertices is shown in Fig. 8. There is no evidence for a nonstatistical accumulation of events in a particular region.

The reconstructed neutrino energy distribution of the 107 candidate events is shown in Fig. 9. The neutrino energy is calculated by summing the reconstructed muon
TABLE II. The numbers of data events in each selection category compared to the expectation from different sources. The MC expectations from neutrino interactions are given for both no oscillations and $\sin^2 2\theta_{23} = 1.0$ and $\Delta m_{23}^2 = 0.0024$ eV$^2$. The expected contributions from the atmospheric neutrino MC were scaled by a factor of 0.88 obtained from the Soudan 2 $\nu_e/\bar{\nu}_e$ data as discussed in Sec. III A. The column referring to “rock $\nu_\mu$” refers to muons which are produced by neutrino interactions in the surrounding rock. The cosmic muon backgrounds in the FC and PC down samples are estimated from data events passing all selection cuts with the exception of the veto shield. Entries marked as $\cdots$ indicate expectations of less than 0.05 of an event. For the entries where no error is quoted the error is less than 0.05 of an event.

<table>
<thead>
<tr>
<th>Selection</th>
<th>Data</th>
<th>Expectation (no oscillations)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Cosmic $\mu$ $\nu_\mu/\nu_\mu$</td>
</tr>
<tr>
<td>FC</td>
<td>69</td>
<td>3.9 ± 0.4</td>
</tr>
<tr>
<td>PC down</td>
<td>25</td>
<td>0.6 ± 0.2</td>
</tr>
<tr>
<td>PC up</td>
<td>13</td>
<td>&lt;0.36</td>
</tr>
<tr>
<td>Total</td>
<td>107</td>
<td>4.4 ± 0.5</td>
</tr>
</tbody>
</table>

Expectation ($\Delta m_{23}^2 = 0.0024$ eV$^2$)

<table>
<thead>
<tr>
<th>Selection</th>
<th>Data</th>
<th>Expectation (no oscillations)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Cosmic $\mu$ $\nu_\mu/\nu_\mu$</td>
</tr>
<tr>
<td>FC</td>
<td>69</td>
<td>3.9 ± 0.4</td>
</tr>
<tr>
<td>PC down</td>
<td>25</td>
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</tr>
<tr>
<td>PC up</td>
<td>13</td>
<td>&lt;0.36</td>
</tr>
<tr>
<td>Total</td>
<td>107</td>
<td>4.4 ± 0.5</td>
</tr>
</tbody>
</table>

The solid lines indicate the active region of the MINOS detector and the dotted lines indicate the boundaries of the fiducial volume.

![MINOS](image_url)

FIG. 8. The reconstructed $x$ – $y$ positions of the neutrino interaction vertices for the 107 selected events. The vertex is defined as the start of the track, which is determined from timing. The solid lines indicate the active region of the MINOS detector and the dotted lines indicate the boundaries of the fiducial volume.

![Events](image_url)

FIG. 9. The reconstructed neutrino energy (logarithmic scale) for the 107 selected events compared to the MC expectation. The neutrino energy is taken to be the sum of the muon momentum and the energy of any hadronic shower associated with the assumed interaction vertex. For the FC and PC samples, the muon momentum is determined from range and curvature, respectively. The solid histogram shows the MC expectation for the case of no neutrino oscillations, the hatched histogram shows the cosmic-ray background and the points with error bars show the data. The dashed histogram shows the expectation for $\nu_\mu \leftrightarrow \nu_e$ oscillations with $\sin^2 2\theta_{23} = 1.0$ and $\Delta m_{23}^2 = 0.0024$ eV$^2$.

energy and the hadronic energy of any reconstructed shower associated with the start of the muon track. For FC events, the muon energy is determined from the track range. For PC events, the less precise momentum from curvature is used.

The neutrino energy spectrum is sharply peaked towards lower energies and the selected event sample is expected to have mean neutrino energy of 3.5 GeV (2.0 GeV for FC events and 7.0 GeV for the PC events) and mean muon energy of 2.4 GeV. For low energy events the ability to determine the sense of the muon track (up/down) is degraded. In MC, 96% of the selected events have the correct direction reconstruction. The remaining 4% of events not
only have the wrong reconstructed sense, but as a consequence, are also assigned the incorrect charge. By requiring that $|\text{RMS}_{\text{up}} - \text{RMS}_{\text{down}}| > 0.66$ ns (see Sec. IV) and that the track traverses at least ten planes, the fraction of misreconstructed events is reduced to 0.1%. For the results that follow, the event sample is divided into two: a “low resolution” sample with $|\text{RMS}_{\text{up}} - \text{RMS}_{\text{down}}| < 0.66$ ns and events with “good timing” for which $|\text{RMS}_{\text{up}} - \text{RMS}_{\text{down}}| > 0.66$ ns. The numbers of events in each category are listed in Table III. The 30 events classified as low resolution are mainly short events and according to MC have a mean neutrino energy of 1.0 GeV. For 85% of the low resolution events, the muon is reconstructed with the correct sense (up/down). However, in the oscillation analysis that follows, the direction information from the low resolution sample is not used, due to the significant fraction of events reconstructed with the wrong direction sense and the fact that for this predominantly low energy sample, the mean angle between the incident neutrino and final state muon is large.

Figure 10 shows the reconstructed zenith angle distribution of the 77 candidate events with good timing. Of these events, 49 are downward going ($\cos \theta > 0$) and 28 are upward going ($\cos \theta < 0$), giving a measured up-down ratio of $0.57 \pm 0.17$ (stat.). The statistical errors correspond to the 68% confidence interval calculated using Poisson statistics [33]. The expected value from Monte Carlo samples in the absence of neutrino oscillations is $0.92 \pm 0.03$ (sys.). The expected value is lower than 1 because of the different selection efficiencies for upward- and downward-going events and the presence of background. The upward-going/downward-going double ratio is

$$R_{\text{up/down}}^\text{data} / R_{\text{up/down}}^\text{MC} = 0.62^{+0.19}_{-0.14} \text{(stat.)} \pm 0.02 \text{(sys.)}$$

This is approximately 2 standard deviations from unity, which is the expectation in the absence of neutrino oscillations. The systematic error is dominated by the experimental uncertainties; the estimated systematic uncertainty on the predicted up/down neutrino flux ratio is less than 1% [30] due to the relatively high energy of the selected neutrino events.

<table>
<thead>
<tr>
<th>Selection</th>
<th>Data</th>
<th>Expected no oscillations</th>
<th>Expected $\Delta m^2 = 0.0024$ eV$^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Good timing</td>
<td>77</td>
<td>90 ± 9</td>
<td>68 ± 7</td>
</tr>
<tr>
<td>Low res.</td>
<td>30</td>
<td>37 ± 4</td>
<td>28 ± 3</td>
</tr>
<tr>
<td>All events</td>
<td>107</td>
<td>127 ± 13</td>
<td>96 ± 10</td>
</tr>
</tbody>
</table>

TABLE III. Classification of events into samples with almost unambiguous direction from timing (“Good timing”) and those where the direction from timing is uncertain (“Low resolution”). The errors are dominated by the systematic uncertainty in the neutrino event rate. The MC expectations are given for both no oscillations and $\sin^2 2\theta_{23} = 1.0$ and $\Delta m^2_{23} = 0.0024$ eV$^2$. 

FIG. 10. The reconstructed $\cos \theta_{\text{zen}}$ distribution for the 77 selected events with good timing compared to the MC expectation. The solid histogram shows the MC expectation for the case of no neutrino oscillations, the hatched histogram shows the cosmic-ray background and the points with error bars show the data. The dashed histogram shows the expectation for $\nu_\mu \leftrightarrow \nu_\tau$ oscillations with $\sin^2 2\theta_{23} = 1.0$ and $\Delta m^2_{23} = 0.0024$ eV$^2$.

FIG. 11. The reconstructed $\log_{10}[L(\text{km})/E(\text{GeV})]$ distribution compared to the expectation. The solid histogram shows the MC expectation for the case of no neutrino oscillations, the hatched histogram shows the cosmic-ray background and the points with error bars show the data. The dashed histogram shows the expectation for $\nu_\mu \leftrightarrow \nu_\tau$ oscillations with $\sin^2 2\theta_{23} = 1.0$ and $\Delta m^2_{23} = 0.0024$ eV$^2$. 

072002-12
A. Oscillation analysis

In the two-flavor approximation, which is adequate for the level of statistical precision considered here, the survival probability $P(\nu_\mu \rightarrow \nu_\mu)$ is given by

$$P = 1.0 - \sin^2 2\theta_{23} \sin^2 \left( 1.27 \Delta m_{23}^2 \frac{L}{E} \right),$$

where $L$ is the distance traveled by the neutrino and $E$ is the neutrino energy. The neutrino path length, $L$, is calculated from the reconstructed zenith angle assuming the neutrinos are produced at a height of 20 km in the Earth’s atmosphere. Figure 11 shows the reconstructed $L/E$ distribution for the 77 candidate events with good timing.

The reconstructed $L/E$ distribution is used as the basis for a fit to the hypothesis of $\nu_\mu \rightarrow \nu_\tau$ oscillations. The resolution on $L/E$ differs greatly event-to-event for three main reasons: for PC events the muon momentum from curvature may be poorly determined; for low energy and/or high $y$ events the opening angle between the observed muon and the true neutrino direction is large; and in the case where the muon direction is close to the plane defined by the horizon, relatively small changes in angle produce large changes in $L/E$. To address the first issue, PC events with little observable curvature, $|Q/p|/\sigma_{Q/p} < 1$, are not used in the fit to the $L/E$ distribution. To account for the different $L/E$ resolutions, in the oscillation fit the data are binned according to $L/E$ resolution. To estimate the event resolution a Bayesian approach has been adopted which allows the event-by-event log($L/E$) probability density function (pdf) to be determined [34]. The rms of the pdf, $\sigma_{\text{log}(L/E)}$, gives a measure of the log($L/E$) resolution of the event. For example, Fig. 12 shows the data binned in four regions of $\sigma_{\text{log}(L/E)}$. For MC, the sensitivity of the $L/E$ distribution to neutrino oscillations increases with decreasing $\sigma_{\text{log}(L/E)}$.

![MINOS](image)

**FIG. 12.** The reconstructed log($L/E$) distribution binned in four regions of log($L/E$) resolution, $\sigma$. PC events with $|Q/p|/\sigma_{Q/p} < 1$ are not used. The solid histogram shows the MC expectation for the case of no neutrino oscillations, the hatched histogram shows the cosmic-ray background and the points with error bars show the data. The dashed histogram shows the expectation for $\nu_\mu \rightarrow \nu_\tau$ oscillations with $\sin^2 2\theta_{23} = 0.90$ and $\Delta m_{23}^2 = 1.3 \times 10^{-3}$ eV$^2$, the oscillation parameters corresponding to the best fit to the MINOS data.
1. Oscillation analysis: Fit procedure

The selected events are divided into ten equal sized bins of the estimated uncertainty in a reconstructed \( L/E \) ratio, \( \sigma_{\log(L/E)} \), ranging from 0.1–1.1. Events with \( \sigma_{\log(L/E)} > 1.0 \) are included in the lowest resolution sample and events with \( \sigma_{\log(L/E)} < 0.1 \) are included in the highest resolution. A simultaneous fit is performed to the overall normalization (using all selected events), the up-down ratio for 77 events with good timing, and separately the shapes of the upward and downward \( L/E \) distributions for events with good timing and \( |Q/p|/\sigma_{Q/p} > 1 \). In this way, each event is used only when the physical observable being fitted is well measured. A maximum likelihood fit to the data is performed using the negative log-likelihood function:

\[
-\ln L = (\mu - N \ln \mu) - \sum_k (N^h_k \ln P^h_k + N^d_k \ln P^d_k)
\]

\[
- \sum_{i_u} \ln f^h_{i_u}(L/E)_{i_u} - \sum_{i_d} \ln f^d_{i_d}(L/E)_{i_d}
\]

\[
+ \sum_j \frac{\alpha_j^2}{2\sigma_{\alpha_j}^2},
\]

where \( N \) is the total number of observed events and \( \mu \) is the total Monte Carlo expectation. The first two terms represent the Poisson probability of observing \( N \) events given the expectation of \( \mu \). The normalization systematic uncertainties are included as nuisance parameters (see below). In the remaining terms, the superscript \( k \) refers to the \( k \)th bin in \( \sigma_{\log(L/E)} \). The sum

\[
\sum_k (N^h_k \ln P^h_k + N^d_k \ln P^d_k)
\]

is the “up-down” likelihood. Here \( N^h_k \) and \( N^d_k \) are the observed numbers of upward- and downward-going events with good timing in bin \( k \) of resolution; \( P^h_k \) and \( P^d_k \) are the Monte Carlo probabilities that an event in resolution bin \( k \) is upward or downward going (\( P^h_k + P^d_k = 1 \)). The terms

\[
\sum_{i_u} \ln f^h_{i_u}(L/E)_{i_u} \quad \text{and} \quad \sum_{i_d} \ln f^d_{i_d}(L/E)_{i_d}
\]

are the likelihood functions for the observed \( L/E \) distributions of upward- and downward-going events, respectively. Here the summations are over the reconstructed upward and downward events, respectively; \( f^h_{i_u}(L/E)_{i_u} \) is the normalized Monte Carlo pdf for the reconstructed \( L/E \) distribution in the \( k \) bin of resolution (that of the event), evaluated at the measured value of \( L/E \) of the event. The MC expectations for \( \mu, P^h_k, P^d_k, f^h_{i_u}(L/E), \) and \( f^d_{i_d}(L/E) \) include contributions from both neutrino interactions and cosmic-ray background and depend on \( (\Delta m^2_{23}, \sin^22\theta_{23}) \) and the nuisance parameters representing the systematic uncertainties. In calculating the expectations as a function of oscillation parameters, the oscillation probabilities are averaged over the distribution of neutrino production heights obtained from the Bartol 3D model. In the fit, systematic effects are included using the nuisance parameters, \( \alpha_j \), which represent the deviation of a particular parameter from its nominal value. The nuisance parameters contribute to the likelihood function through the terms

\[
\sum_j \frac{\alpha_j^2}{2\sigma_{\alpha_j}^2},
\]

where \( \sigma_{\alpha_j}^2 \) is the estimated systematic uncertainty. The following systematic effects are included: (i) a \( \pm 10\% \) uncertainty on the expected neutrino event rate; (ii) a 3% uncertainty on the muon momentum and a 5% uncertainty on the hadronic energy scale; (iii) a 3% uncertainty on the relative efficiency for selecting upward- versus downward-going events; (iv) to accommodate the uncertainty in the shape of the neutrino energy spectrum, the spectrum is allowed to scale according to \( 1.0 + 0.1 \beta (E_\nu - 2) \) for \( E_\nu < 2 \text{ GeV} \) and \( 1.0 + 0.025 \beta (E_\nu - 2) \) for \( E_\nu > 2 \text{ GeV} \), where \( \beta \) is normal distributed; (v) to allow for uncertainties in the modeling of neutrino cross sections, the relative cross section for quasielastic interactions is assumed to have a 20% uncertainty. Since the neutrino flux times cross section is normalized to Soudan 2 data, in the fit the systematic error associated with the quasielastic fraction only affects the shapes of the reconstructed \( L/E \) distributions.

With the exception of normalization, the systematic uncertainties have little impact on the resulting confidence regions. The above form of the likelihood function is chosen to simplify the inclusion of systematic errors in the fit: as normalization and up-down ratio are treated independently of shape.

2. Oscillation analysis: Results

For each hypothesized value of \( (\Delta m^2_{23}, \sin^22\theta_{23}) \) the negative log-likelihood function described above is minimized with respect to the nuisance parameters. For the data, the minimum likelihood occurs at \( (\Delta m^2_{23} = 1.3 \times 10^{-3} \text{ eV}^2, \sin^22\theta_{23} = 0.90) \). The 90% confidence limits are obtained from the difference in the log-likelihood function \( -\Delta \ln L = -\ln L(\Delta m^2_{23}, \sin^22\theta_{23}) + \ln L_0 \). Here \( -\ln L_0 \) is the value of the negative log-likelihood function for the best fit to the data. In the limit of Gaussian errors, the 90% confidence level allowed regions of parameter space are defined by \( -\Delta \ln L < 2.3 \). The frequentist approach of Feldman and Cousins [35] is used to determine the value of \( -\Delta \ln L \) which corresponds to a particular confidence level. For each point in parameter space, \( (\Delta m^2_{23}, \sin^22\theta_{23}) \), 1000 Monte Carlo experiments are generated. In each experiment a value for each systematic bias is drawn from a Gaussian distribution with standard deviation equal to the estimated systematic
FIG. 13. The 68% and 90% confidence limits on the oscillation parameters obtained using the Feldman and Cousins approach. Also shown is the 90% C.L. limit calculated using $-\Delta \ln L < 2.3$.

uncertainty. The generated data sample is fitted in the same manner as the data and the value of $-\Delta \ln L(\Delta m^2_{\text{gen}}, \sin^2 2\theta_{\text{gen}})$ is determined. The generated point is included in the 90% confidence region if less than 90% of the experiments yield a smaller value than obtained in the data. For the MINOS data the 68% and 90% confidence limits obtained using the Feldman and Cousins approach are shown in Fig. 13. The 90% C.L. contour is close to that obtained using $-\Delta \ln L = 2.3$. With the current statistics, the MINOS atmospheric neutrino data are consistent with a wide range of oscillation parameters including the most recent results from Super-Kamiokande [9] and K2K [10]. The data disfavor the null oscillation hypothesis at the 98% confidence level.

For completeness, Fig. 14 shows the likelihood as a function of $\Delta m^2_{23}$ for $\sin^2 \theta_{23} = 1.0$. The rises at large and small values of $\Delta m^2_{23}$ are mainly due to the normalization and up-down ratio. The structure within this broad minimum arises from the fit to the shape of the $L/E$ distribution. The quality of the fit is good. As a measure of the fit quality, 10,000 simulated experiments were generated with $\Delta m^2_{23} = 0.0024\,\text{eV}^2$, $\sin^2 2\theta_{23} = 1.0$ and the minimum value of $-\ln L_0$ determined; in 84% of these experiments the minimum value of $-\ln L_0$ exceeded that obtained from the fit to the data. Figure 14 also shows the expected sensitivity.

B. Charge ratio

The selected contained events with unambiguous timing information are divided into neutrino and antineutrino interactions on the basis of the reconstructed muon charge obtained from the curvature of the reconstructed muon track. Only events with unambiguous direction from timing are considered; events with an incorrect direction will be reconstructed with the wrong zenith angle and will have their charge inverted. Figure 15 shows the distribution of $(Q/p)/\sigma(Q/p)$ for the 77 events with well-determined direction from timing compared to the MC expectation. Events are classified as $\nu_\mu$ for $(Q/p)/\sigma(Q/p) < -2$; $\bar{\nu}_\mu$ for $(Q/p)/\sigma(Q/p) > +2$; or events which are ambiguous, $| (Q/p)/\sigma(Q/p) | \leq 2$. The selected numbers of events in

FIG. 14. The $\Delta L$ curve as a function of $\Delta m^2_{23}$ for the case of maximal mixing. The dotted curve shows the expected sensitivity which is the average likelihood curve obtained from 10000 Monte Carlo experiments.

FIG. 15. The reconstructed distribution of $(Q/p)/\sigma(Q/p)$, the ratio of the charge divided by momentum obtained from the track curvature divided by its error. The solid histogram indicates the Monte Carlo expectation assuming no oscillations, the hatched histogram shows the cosmic-ray background and the points with error bars show the data. The dashed histogram shows the expectation for $\nu_\mu \leftrightarrow \nu_\tau$ oscillations with $\sin^2 2\theta_{23} = 1.0$ and $\Delta m^2_{23} = 0.0024\,\text{eV}^2$. 

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constructed values of estimated by shifting and smearing the Monte Carlo associated with charge identification. The uncertainty was the experimental uncertainty in the relative uncertainty in the neutrino flux \times cross section. The MC expectations are given for both no oscillations and \( \sin^22\theta_{23} = 1.0 \) and \( \Delta m_{32}^2 = 0.0024 \text{ eV}^2 \).

<table>
<thead>
<tr>
<th>Selection</th>
<th>Data</th>
<th>Expected no oscillations</th>
<th>Expected ( \Delta m_{32}^2 = 0.0024 \text{ eV}^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low res.</td>
<td>30</td>
<td>37 \pm 4</td>
<td>28 \pm 3</td>
</tr>
<tr>
<td>Ambig. ( \nu_\mu/\overline{\nu}_\mu )</td>
<td>25</td>
<td>26 \pm 3</td>
<td>20 \pm 2</td>
</tr>
<tr>
<td>( \nu_\mu )</td>
<td>34</td>
<td>42 \pm 4</td>
<td>31 \pm 3</td>
</tr>
<tr>
<td>( \overline{\nu}_\mu )</td>
<td>18</td>
<td>23 \pm 2</td>
<td>17 \pm 2</td>
</tr>
</tbody>
</table>

Each charge category are compared to the MC expectations in Table IV.

Of the events where it is possible to cleanly tag the charge of the muon, 18 are identified as \( \overline{\nu}_\mu \) candidates and 34 as \( \nu_\mu \) candidates, yielding a \( \overline{\nu}_\mu \) to \( \nu_\mu \) ratio of

\[
R_{\text{data}}^{\overline{\nu}_\mu/\nu_\mu} = 0.53^{+0.21}_{-0.15}(\text{stat.}) \pm 0.03(\text{sys.}).
\]

The systematic uncertainty is the experimental uncertainty associated with charge identification. The uncertainty was estimated by shifting and smearing the Monte Carlo reconstructed values of \( (Q/p)/\sigma(Q/p) \) while maintaining reasonable agreement between data and Monte Carlo samples for the stopping muon data shown in Fig. 3. For the purposes of studying possible biases in the charge reconstruction, 37% of the data were recorded with the coil current reversed. Consistent values for the \( \overline{\nu}_\mu/\nu_\mu \) ratio are found in the normal and reversed current data samples; 22 (12) events are identified as \( \nu_\mu \) and 12 (6) are identified as \( \overline{\nu}_\mu \) in the normal (reversed) field data samples. From Monte Carlo samples, the expected ratio of identified \( \overline{\nu}_\mu \) to \( \nu_\mu \) events is 0.550, where it is assumed that both neutrinos and antineutrinos oscillate with the same parameters. This expected ratio is almost independent of the values of the oscillation parameters provided they are the same for neutrinos and antineutrinos. The ratio of \( \overline{\nu}_\mu \) to \( \nu_\mu \) events in the data compared to the Monte Carlo expectation (Bartol 3D and NEUGEN3) assuming the same oscillation parameters for neutrinos and antineutrinos is

\[
R_{\text{data}}^{\overline{\nu}_\mu/\nu_\mu} / R_{\text{MC}}^{\overline{\nu}_\mu/\nu_\mu} = 0.96^{+0.38}_{-0.27}(\text{stat.}) \pm 0.15(\text{sys.}).
\]

The statistical errors correspond to the 68% confidence interval calculated using Poisson statistics [33]. The systematic error includes the experimental uncertainty associated with the muon charge identification (0.06), the uncertainty in the relative \( \overline{\nu}_\mu \) to \( \nu_\mu \) flux (0.04), and the relative uncertainty in the \( \nu_\mu \) to \( \overline{\nu}_\mu \) cross section (0.13). The systematic errors on the relative \( \overline{\nu}_\mu \) to \( \nu_\mu \) fluxes and cross sections were estimated taking into account the energy spectra of the charge-tagged neutrino and antineutrino events. From Monte Carlo samples, the sample of events where the charge of muon is cleanly identified has a mean neutrino energy of 3.7 GeV, with 95% of the expected events having neutrino energies between 1 GeV and 10 GeV. In Monte Carlo samples, 40% of these events arise from quasielastic interactions, 30% arise from resonance production, and 30% arise from deep inelastic scat-

<table>
<thead>
<tr>
<th>Events</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \nu_\mu )</td>
</tr>
<tr>
<td>( \overline{\nu}_\mu )</td>
</tr>
</tbody>
</table>

![Figure 16](image_url)
tering. In this energy range the uncertainty on the ratio of atmospheric $\nu_\tau$ to $\nu_\mu$ flux was estimated to be 8% [36] for the Bartol 1D model. Recent studies based on the Bartol 3D model give an estimated uncertainty of 4% [30]. Since there is limited data on antineutrino cross sections in the energy range 1–5 GeV[37–39], the variation in the predicted $\nu_\mu/\bar{\nu}_\mu$ event rate was studied through conservative changes to the neutrino cross section model. The variations considered include parameters affecting the free nucleon cross sections such as axial vector masses, choice of PDF set, and model for the resonance region. Similarly the effect of changes to the nuclear physics model which affect the rate via Pauli blocking of quasielastic and nuclear shadowing of deep inelastic scattering (DIS) events was studied. The quadrature sum of these changes is 13.5%. The largest contribution to this uncertainty comes from the treatment of resonance production and the resonance/DIS transition region. A 12% difference is found in comparing a model which explicitly includes resonance production [22,40] versus one which uses a QCD-based approach [41]. The size of this difference ultimately reflects the uncertainty in the experimental data to which these models are tuned.

CPT violating models which attempt to explain the LSND data suggest a large value of $\Delta m_{23}^2$ for antineutrinos [12,13]. In principle, the MINOS data will be able to address this possibility by measuring the oscillation parameters for the selected antineutrino sample. Figure 16 shows up/down distribution of the 18 $\bar{\nu}_\mu$ and 34 $\nu_\mu$ events compared to the expectation for (i) no oscillations; (ii) the case where both $\nu_\mu$ and $\bar{\nu}_\mu$ oscillate with $\Delta m_{23}^2 = 0.0024$ eV$^2$ (maximal mixing); and (iii) the case where $\nu_\mu$ oscillate with $\Delta m_{23}^2 = 0.0024$ eV$^2$ (maximal mixing) and $\bar{\nu}_\mu$ oscillate with $\Delta m_{23}^2 = 1.0$ eV$^2$ (maximal mixing). The data are consistent with the same oscillation parameters for neutrinos and antineutrinos. However, with the current statistics the possibility of a large value of $\Delta m_{23}^2$ for antineutrinos cannot be excluded.

VII. SUMMARY

The MINOS far detector has been taking data since the beginning of August 2003 at a depth of 2070 m water-equivalent in the Soudan mine, Minnesota. This paper presents the first MINOS observations of $\nu_\mu$ and $\bar{\nu}_\mu$ charged-current atmospheric neutrino interactions based on an exposure of 418 days. A total of 107 candidate contained-vertex neutrino interactions are observed, consistent with both the expectation of $127 \pm 13$ for no neutrino oscillations and $96 \pm 10$ for $\Delta m_{23}^2 = 0.0024$ eV$^2$ and $\sin^2 2\theta_{23} = 1.0$. The expected numbers of events include the estimated background from cosmic-ray muons, 4.4 $\pm$ 0.5, obtained from data. The errors on the expectation are dominated by 10% uncertainty on the neutrino event rate which was obtained using results from the Soudan 2 Collaboration. Of the events for which the direction can be cleanly identified, the ratio of upward- to downward-going events in the data is compared to the Monte Carlo expectation in the absence of neutrino oscillations, giving

$$R_{\text{data}}^{\text{up/down}} / R_{\text{MC}}^{\text{up/down}} = 0.62^{+0.19}_{-0.14}(\text{stat.}) \pm 0.02(\text{sys.})$$

An extended maximum likelihood fit to the observed log$(L/E)$ distribution yields a best fit value of $(\Delta m_{23}^2 = 1.3 \times 10^{-3}$ eV$^2$, $\sin^2 2\theta_{23} = 0.90$) and 90% confidence limits of $(7 \times 10^{-5}$ eV$^2 < \Delta m_{23}^2 < 5 \times 10^{-2}$ eV$^2$, $\sin^2 2\theta_{23} > 0.2)$. The consistency of the data with the null hypothesis of no neutrino oscillations is investigated; the data exclude the null hypothesis at the 98% confidence level.

The curvature of the observed muons in the 1.3 T MINOS magnetic field is used to separate $\nu_\mu$ and $\bar{\nu}_\mu$ interactions. Of the selected events for which it is possible to cleanly determine the charge of the muon, 18 are identified as $\bar{\nu}_\mu$ candidates and 34 as $\nu_\mu$ candidates, giving an observed $\bar{\nu}_\mu$ to $\nu_\mu$ ratio of $0.53^{+0.15}_{-0.03}$ (stat.) $\pm 0.03$ (sys.). The fraction of $\bar{\nu}_\mu$ events in the data is compared to the Monte Carlo expectation assuming neutrinos and antineutrinos oscillate in same manner, giving

$$R_{\bar{\nu}_\mu/\nu_\mu}^{\text{data}} / R_{\bar{\nu}_\mu/\nu_\mu}^{\text{MC}} = 0.96^{+0.38}_{-0.27}(\text{stat.}) \pm 0.15(\text{sys.})$$

Although the statistics are limited, this is the first direct observation of atmospheric neutrino interactions separately for $\nu_\mu$ and $\bar{\nu}_\mu$. The data are consistent with neutrinos and antineutrinos oscillating with the same parameters, although CPT violating scenarios with large values of $\Delta m_{23}^2$ for antineutrinos are not excluded with the current data.

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[34] M. Thomson, A Bayesian Approach to Fitting Atmospheric Neutrino Data (to be published).