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BAYESIAN METHODS OF ASTRONOMICAL SOURCE EXTRACTION

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Received 2006 November 24; accepted 2007 February 5

ABSTRACT

We present two new source extraction methods, based on Bayesian model selection and using the Bayesian information criterion. The first is a source detection filter, which is able to simultaneously detect point sources and estimate the image background. The second is an advanced photometry technique that measures the flux, position (to subpixel accuracy), local background, and point-spread function. We apply the source detection filter to simulated Herschel SPIRE data and demonstrate the filter’s ability to both detect point sources and simultaneously estimate the image background. We use the photometry method to analyze a simple simulated image containing a source of unknown flux, position, and point-spread function; we not only accurately measure these parameters but also determine their uncertainties (using Markov chain Monte Carlo sampling). The method also characterizes the nature of the source (distinguishing between a point source and an extended source). We demonstrate the effect of including additional prior knowledge. Prior knowledge of the point-spread function increases the precision of the flux measurement, while prior knowledge of the background has only a small impact. In the presence of higher noise levels, we show that prior positional knowledge (such as might arise from a strong detection in another wave band) allows us to accurately measure the source flux even when the source is too faint to be detected directly. These methods are incorporated in SUSSEXtractor, the source extraction pipeline for the forthcoming Akari Far-Infrared Surveyor all-sky survey. They are also implemented in a stand-alone, beta-version tool that is freely available.

Subject headings: infrared: general — methods: data analysis — methods: statistical

1. INTRODUCTION

Source extraction is close to ubiquitous in modern observational astrophysics. The ability to identify and accurately quantify objects of interest in astronomical observations, in particular with reliable automated methods, is becoming ever more important with the advent of modern, large-area surveys. It is crucial that we are able to ask precise, statistical questions of the data from these surveys. Is there a source at a given location in the sky? Is it pointlike or extended? And what set of parameters can define it? Any science derived from the study of astronomical objects proceeds directly from accurate source extraction.

In order to extract sources from astronomical data, we typically face a number of challenges. First, there is instrumental noise. It is often possible to measure this characteristic and use the information to partially offset its effects. More problematic are any so-called backgrounds to the observation. These can be due to Galactic emission, cosmological backgrounds, faint-source confusion, or even simply emission from parts of the telescope itself. These are often much harder to account for and often constitute an in-depth study in themselves. A prime example is the extraction of sources from cosmic microwave background (CMB) data (see, e.g., Vielva et al. 2001). One may also have to contend with systematic effects such as glitches that can be caused by cosmic-ray hits on the detectors of space telescopes.

Because of these challenges and also because it is critical to extract the utmost precision from our (often very expensive to gather) data, we must strive to use all the available information when extracting sources. This means using not only all available data samples but also accurate noise estimates, measurements of the point-spread function, and any other prior knowledge we may have.

Over the years, a number of methods have been created in order to use various sets of information to obtain “optimal” (subject to certain sets of assumptions) source extraction methods. There are many techniques based on the concept of filtering data to enhance relatively the signal due to objects with a certain set of characteristics. Examples of these include the matched, scale-adaptive, and wavelet filters (see, e.g., Vio et al. 2002; Barreiro et al. 2003; Barnard et al. 2004; López-CaniGeo et al. 2005). More recently, Makovoz & Marleau (2005) have derived a filter of this type using the Bayesian formalism, thus allowing for the explicit inclusion of prior knowledge.

Fitting of the point-spread function to image data has also been used as a way of accurately determining the position and flux of a (point) source (e.g., Scott et al. 2002). The model-fitting methodology has been given a much more general grounding in statistical theory by Hobson & McLachlan (2003), who have detailed a very general (and powerful) Bayesian framework for the extraction of sources. Bayesian methodology has also been used in the Poisson noise regime (e.g., Guglielmetti et al. 2004). There are a number of publicly available source extraction packages, which use a variety of the above methods (plus some other measures) in order to accurately extract sources. These include, for example, DAOPHOT (Stetson 1987) and SExtractor (Bertin & Arnouts 1996).

Perhaps the most flexible of these approaches is that of using Bayesian statistics (see, e.g., Jaynes 2003; MacKay 2003), as it allows one to ask very precise statistical questions of the data. This framework is also highly general, allowing the inclusion of all pertinent information. In this paper, we explore the use of Bayesian statistics for source extraction. We present a pair of new methods based on this formalism, one for simultaneous source detection and background estimation and subtraction, and the other for an advanced form of source photometry that also allows the determination of the nature (pointlike, extended, etc.) of the source.

The contents of this paper are therefore as follows: In § 2, we present a general formalism for performing Bayesian source extraction. We also detail two specific implementations. In § 3, we apply these methods to simulated data sets, in order to
We start with the likelihood. If we are able to assess this, then (after applying a prior), we will have the posterior probability distribution, which is the result we require. Following the normal route for uncorrelated, Gaussian noise, we have the following:

$$ L \propto \exp \left( -\frac{\chi^2}{2} \right), $$

$$ \chi^2 = \sum_{i=1}^{N_{\text{pix}}} \left( \frac{d_i - m(\theta)}{\sigma_i} \right)^2, $$

where $d_i$ is the value of the $i$th data pixel of the subset of image pixels under consideration, $m_i$ is the corresponding value from a (parameterized) model of the signal, and $\sigma_i$ is the standard deviation of the (Gaussian) noise associated with that pixel.

Calculation of the likelihood function therefore depends on the parameterized model of the signal that we are considering. In this case, the model will contain a source (pointlike or extended). It will also contain a representation of the astronomical and instrumental background, as well as possibly containing parameters describing instrumental characteristics. For example, if not well defined by independent measurements, the point-spread function could be parameterized and, hence, simultaneously measured by the model-fitting procedure.

Once the likelihood has been constructed, any prior knowledge that we have about the parameters can be included, in the form of the prior probability (a density function spanning the same parameter space as the likelihood). This function might typically include information such as prior knowledge of the positions of sources, although it is perfectly acceptable to use an uninformative flat prior (i.e., equal-valued at all points in parameter space) if one has no relevant prior knowledge (we note that this is the implicit assumption in maximum likelihood methods).

As the evidence is a constant, normalizing term, we now have the (unnormalized) posterior distribution. We can map this distribution by calculating posterior values over a hypercube of parameter-space points or by Markov chain Monte Carlo (MCMC) sampling. The peak of this distribution is our most likely solution, and (once normalized) the distribution as a whole provides the statistical confidence regions.

The posterior probability distributions of individual parameters can be obtained by marginalizing over the other parameters (see, e.g., Sivia & Skilling 2006). This can be done in a number of ways. If MCMC sampling has been used to map the posterior probability distribution, then simply making a histogram of the samples using the values of a single parameter automatically gives the corresponding one-dimensional (1D) marginalized distribution (a well-known and highly useful feature of sampling from the posterior). If one were considering only a small number (three or fewer, say) of parameters, then it might be feasible to calculate posterior values over a hypercube of parameter points and then marginalize numerically (although this is very much a brute-force approach). Or one can assume a functional form for the posterior and perform the marginalization analytically. One common choice for the functional form is that of a multivariate Gaussian, which is often a reasonable approximation to the posterior and is analytically tractable. It also has the advantage that it can be completely specified by a parameter covariance matrix evaluated at the maximum a posteriori point.

The method yields a complete analysis, given a particular choice of model. However, the question of selecting a good model still remains. This can be addressed by the evidence, which provides a relative measure of the probability of different models being the best fit, given the data (see, e.g., Jaynes 2003).
Bayesian evidence is typically time-consuming to calculate. This makes analytic approximations desirable, in terms of practicality. In particular, the Bayesian information criterion (BIC; Schwarz 1978) provides an easily calculated approximation to the logarithm of the evidence:

\[ \text{BIC} = -2 \ln \mathcal{L}_{\text{max}} + \nu \ln N_{\text{data}}, \quad (4) \]

where \( \mathcal{L}_{\text{max}} \) is the maximum likelihood value for a given hypothesis, \( \nu \) is the number of free parameters in the model, and \( N_{\text{data}} \) is the number of (approximately equally weighted) data used. When comparing how likely different models are, lower BIC values indicate a higher probability of the model being the correct one.

Using model selection criteria allows us to address the question of which from a range of models is the best description of the data, and to do so in a statistically rigorous way. This becomes vital when one’s data contain millions of sources, some pointlike, some extended (and with different morphologies), and some not real at all but rather the product of contamination.

### 2.2. Implementation: Bayesian Source Detection Filter

The first implementation that we present of the above formalism is a Bayesian source detection filter. Source detection is necessary if one has observations of a region of sky but has no explicit knowledge of the positions of sources in the image (the case with many astronomical surveys). Our task is therefore to analyze the entire image, identifying the positions where it is likely that there is a source present.

One consideration that is often critical for such source detection is speed of analysis. Modern photometric surveys, in particular, often produce many large images, necessitating source detection methods that are computationally quick to apply. With this in mind, we derive an analytic Bayesian solution to determine the relative probability (at each pixel position in an image) of the data’s being best described by an empty sky or a point source (with an unknown, uniform background in each case).

The two models we therefore consider are the following:

**Empty sky, uniform background.**—This model consists solely of a flat, uniform background, described by a single parameter (the level of the background).

**Point source, uniform background.**—This model builds on the empty-sky model, adding a single point source centered at the pixel currently being considered. The point source is modeled as a circularly symmetric, two-dimensional (2D) Gaussian profile of known FWHM. This model has two parameters: the background level and the integrated flux of the source.

We will compare these models using BIC. This means (see eq. [4]) that we only need to calculate the maximum posterior value for each model. By doing this at each (fixed) pixel position, we can therefore calculate a map of the relative evidence for point sources across the image.

Because we are considering (for each pixel) a fixed position, each model comprises a linear sum of fixed components. This means that we can find analytic solutions in each case for the maximum likelihood values. Using the condition that the partial derivatives of the likelihood must be zero at the maximum likelihood solution, we can solve to find the following maximum likelihood solutions for each model:

For the point-source model, we have the following description of the model:

\[ m_i = F \mathcal{P}_i + B. \quad (5) \]

For the empty-sky model, we have the following simple description:

\[ m_i = B. \quad (6) \]

Here \( m_i \) is the \( i \)th model pixel, \( F \) is the source flux, \( \mathcal{P}_i \) is the (Gaussian) point-spread function (normalized such that it integrates to unity), and \( B \) is the uniform background.

From this, we find the following analytic maximum likelihood solutions for \( F \) and \( B \):

\[
F_{\text{source}} = \frac{\gamma \beta - \delta \epsilon}{\alpha \beta - \epsilon^2}, \quad B_{\text{source}} = \frac{\alpha \delta - \gamma \epsilon}{\alpha \beta - \epsilon^2},
\]

\[
B_{\text{empty}} = \delta / \beta,
\]

where the calculated values used in the above equations are given by the following (with all sums being performed over the image pixels in a local region; see § 2.4 for a discussion of how to choose this region):

\[
\alpha = \sum_{i=1}^{N_{\text{pixels}}} \frac{\mathcal{P}_i^2}{\sigma_i^2}, \quad \beta = \sum_{i=1}^{N_{\text{pixels}}} \frac{1}{\sigma_i^2}, \quad \gamma = \sum_{i=1}^{N_{\text{pixels}}} \frac{d_i \mathcal{P}_i}{\sigma_i^2},
\]

\[
\delta = \sum_{i=1}^{N_{\text{pixels}}} \frac{d_i}{\sigma_i^2}, \quad \epsilon = \sum_{i=1}^{N_{\text{pixels}}} \frac{\mathcal{P}_i}{\sigma_i^2}.
\]

By then feeding the best-fit model back into equations (2) and (3), we obtain the maximum likelihoods. We can therefore calculate the relative BIC at each pixel position (note that we implicitly use flat, uninformative priors in the preceding steps). The resulting map is an estimate of the (logarithm of the) relative probability of there being a point source, rather than empty sky, at any given pixel position.

The local extrema of this map therefore give us the locations where one model is (locally) most favored over the other. Constructing the map so that (by convention) high values correspond to the point-source model’s being more likely, we can identify the most likely source positions in the input image by identifying the local maxima in the map, subject to some minimum threshold value.

This method is closely modeled in some respects on traditional filtering methods such as matched, scale-adaptive, and wavelet filters. It does, however, have several key advantages.

1. **Simultaneous background estimation, subtraction.**—In real astronomical data, background subtraction is a highly nontrivial task. In particular, more traditional methods such as median filtering are biased by the presence of sources. By performing the subtraction simultaneously, we largely avoid this problem.

2. **Proper accounting for flagged data and locally varying noise.**—Real astronomical images will typically have gaps due to flagging and uneven scan strategies, as well as point-to-point variations in noise levels. This approach allows us to properly account for these effects by including an individual statistical weight (i.e., \( 1/\sigma^2 \)) for each image pixel. Similarly, setting a given weight to zero effectively flags out the corresponding datum (see eq. [3]). This is mathematically well defined; the principal challenge in such cases is in fact to estimate accurately the statistical weight (via the standard deviation) for each image pixel, which will depend on exactly how the image was created (e.g., if it is the sum of many repeated observations, the multiple samples contributing to each image pixel can be used to estimate the standard deviation).
3. Extensibility.—As it is based on a very flexible and general formalism, this source detection filter can be straightforwardly modified to accommodate more complex and realistic data models. For example, many data are subject to “glitches” (caused by cosmic-ray hits on detectors). By including in this method a third model of a single very high pixel value, it would be possible to distinguish between a source and a glitch spike.

2.3. Implementation: Bayesian Source Photometry

Once a source has been detected, we wish to more completely measure and characterize it. Considering only regions of the sky in which there is likely to be a source means that we can afford to devote substantially more computational effort to each candidate position. This is the principal advantage of performing source extraction in two distinct stages.

In this method, we again adopt the approach of fitting multiple models to the local data (again using the fact that we are interested in compact sources, to minimize the data we must consider). However, in this case, we will use a more in-depth approach, allowing more parameters to vary and mapping out the posterior probability distribution in each case. The result will be more precise results (in particular, subpixel positional accuracy) and the determination of the errors on each parameter (without assumptions as to the form of the error distributions).

We proceed again by defining a number of models that we will fit to the data.

Empty sky, uniform background.—This model consists solely of a flat, uniform background, described by a single parameter (the level of the background).

Point source, uniform background.—This model builds on the empty-sky model, adding a single point source at a given (parameterized) position ($X$, $Y$). The point source is modeled as a circularly symmetric 2D Gaussian profile of known FWHM. This model has four parameters: the background level, $X$- and $Y$-positions, and the integrated flux of the source.

Extended source, uniform background.—This model is the logical extension of the point-source model and is identical, with the exception that the FWHM is now allowed to vary as a model parameter (giving five in total). This allows us either to account for circularly symmetric extended sources or, alternatively, to measure the FWHM of the point-spread function if this is not known.

We emphasize that there are many other models that can be usefully applied. Examples would be noncircular extended sources, models in which the noise is unknown, and models in which there are two or more adjacent (blended) sources.

For simplicity, we will again reply on the BIC for model comparison, although a full Bayesian evidence calculation could be used (computational resources permitting). As before, the likelihood functions are thus defined for any given set of parameter values of the relevant model. Multiplying by the prior distribution for each model, we have the posterior for each model, which is mapped using MCMC sampling (except for the empty-sky model, for which we only require the analytic best-fit solution, unless a prior is imposed).

The MCMC sampling returns the best-fit value for each model. We use this to calculate BIC values and hence determine which model is mostly likely to be the best representation of the data. This characterizes the nature of the source in question.

Returning to the MCMC samples for the most likely model, we have also mapped the posterior probability distribution for that model. From this we can straightforwardly determine the confidence intervals and best-fit values for all fitted parameters.

The power of this method lies in its ability to ask precise, statistical questions as to the nature of a source and to recover the theoretically optimal amount of pertinent information given the data. The flexibility of the Bayesian framework means that we are able to adapt this method, depending on the type of sources (and data) that we are expecting. It is entirely realistic to deploy a whole battery of models, fitting each one in turn and determining which is the most likely representation.

2.4. Determining Optimal Data Subset Size

Because we are concerned with the extraction of compact sources, above analyses need only consider a small subset of local data, for each source position. This subset will be large enough that we obtain good constraints on the source flux and local background, but small enough that our assumption of a flat background does not break down. Our definition of the size and shape of this region will therefore have a direct impact on our source extraction.

We choose to determine an optimal region size in terms of a minimized BIC value (and hence maximized Bayesian evidence). This will give us a data model that best describes our data (for the types of models we are considering here). If we define the region as circular, then we reduce this problem to an optimization (in BIC) with respect to the radius of the region.

One complication is that for BIC comparisons to be valid, the same data set must be considered in each case. This would plainly not be true if we simply used the data inside the circular region of interest. To avoid this problem, we also define a larger superregion (also circular) and label the superregion image pixels that lie outside the region of interest as external pixels. We then redefine our model as fitting the source and background to the region of interest, as well as allowing additional free parameters for each of the external pixels so that they are fitted exactly and do not contribute to the $\chi^2$ of the model fit. Therefore, the external pixels will contribute to the BIC solely as extra parameters, the number of which will vary depending on the radius of the region of interest.

These nuisance parameters are not trivial to deal with, and we emphasize that the above procedure makes the simplifying assumption that the nuisance parameters can be fitted to the data with no uncertainty, so that marginalization over them is not necessary. In practice this is not true and would alter the BIC calculation (via the maximum likelihood value).

This could be accounted for in the photometry method because MCMC methods can straightforwardly include large numbers of nuisance parameters, which can be marginalized over without extra effort. Doing so will incur a need for longer sampling chains to be generated, to ensure adequate convergence.

One peculiarity of this procedure is that the BIC has a weak dependence (going as the logarithm) on the radius of the super-region (and hence the maximum possible region radius). While this is clearly undesirable, the effect will be small for reasonable ranges of radius.

The minimum sensible region radius will typically be dictated by the FWHM of the point-spread function, with perhaps a radius equal to the FWHM being a reasonable starting point. The maximum radius is less well defined, but a value of 4 or 5 times the FWHM would seem intuitively reasonable, and our experiences in this paper suggest that this is not unreasonable.

For the case of fitting a single source (i.e., when we are applying source photometry), this process is unambiguous. In the case of the source detection filter, where we may have many detected sources (and that number may change as we optimize with radius), we need to choose what metric we will optimize. In general, this
choice will depend on the exact nature of both the data and the science in question.

One simple approach (and the one that we have adopted here) is to use an intermediate-radius case (say, twice the FWHM of the point-spread function) as a starting point, identifying the sources detected in this case. We then use as our metric the sum of BIC values for the fits to these sources.

This procedure gives us a way of selecting an optimized definition for a local region of the data. This optimizes the performance of the source extraction algorithm but also means that the user need not waste any time optimizing by trial and error.

2.5. Prior Knowledge

A strength of the Bayesian formalism is its explicit inclusion of prior knowledge. In the case of source extraction, one typically assumes that the noise characteristics and the point-spread function are known (although this need not be the case). One could also assume prior knowledge about any of the fitted parameters; for example, source position may have already been determined in another observing band.

It is also possible to select priors on the basis of more general knowledge. For example, if one is attempting to detect a population of galaxies, it may be reasonable to assume a power-law distribution for the source flux (e.g., from a model of the galaxy population). Even in the absence of such knowledge, one could still choose the Jeffreys prior (a power law with index of $-1$), which is the indifference prior for a positive-only scaling parameter.

The source flux is also of particular note, because it will typically (although not always; e.g., the Sunyaev-Zel’dovich effect for galaxy clusters in CMB observations) be subject to the constraint of being nonnegative. In this case, it is important to properly apply this as a prior constraint. Because the above source photometry method uses MCMC sampling, it is straightforward to quantify the assumptions on the prior. In §3.2, we show examples of this.

The source detection filter relies on analytic solutions in order to yield a plausible speed of analysis. This makes the application of non-top-hat priors more difficult, if convenient analytic solutions are to be possible. The potential size of this topic takes it beyond the scope of this paper, but we note that the exploration of different priors represents a largely untapped area where source detection methods could be improved.

3. RESULTS

In this section, we present example results from the two methods detailed in the previous section. We highlight the speed of analysis of these methods. Running on a desktop machine (using two 2.4 GHz AMD Opteron 250 CPUs) and implemented in IDL, the source detection filter processed $9 \times 10^4$ pixels s$^{-1}$ (a $784 \times 912$ pixel image in 8 s), and the photometry method was able to analyze one source every 9 s (producing $10^5$ MCMC samples per model, per source). At this rate, for example, the whole Akari all-sky survey could be source detection–filtered in 4 days and 4 hours (assuming 40,000 deg$^2$ of coverage, with $8'' \times 8''$ image pixels and four observing bands) using a single desktop machine.

3.1. Bayesian Source Detection Filter

Figure 1 shows images from the analysis of a simulated Herschel SPIRE (the Spectral and Photometric Imaging Receiver; see, e.g., Pilbratt 2004) observation of a number of point sources, along with a diffuse Galactic foreground (data courtesy of P. André, B. Sibthorpe, & T. Waskett). Shown are the input flux image, a map of the background (as estimated by the source detection filter), and a map of the residuals between input flux image and background map.

The background map is created using the maximum a posteriori estimate of the model background at each pixel position. In each case, the model used is that which is most likely, on the basis of BIC score. The residuals map is created by subtracting the background map from the original input flux image. The residuals will therefore contain the point sources, plus any imperfections in the background estimation.

![Simulated images on which photometry was performed. Both images contain the same underlying signal, consisting of a uniform background (of level 0.5 units), plus a Gaussian point source with position relative to the image center of (0.3, 0.4) pixels, a FWHM of 5.2 pixels, and an integrated flux of 10 units (corresponding to a peak height of 0.231 units). The left image has Gaussian noise with rms of 0.075, and the right has rms noise of 0.3 (i.e., higher than the peak of the source).](image)
3.2. Bayesian Source Photometry

The analyses in this subsection are carried out on a simple, simulated test image (shown in Fig. 2). The image contains a single point source on a uniform background, with uncorrelated Gaussian random noise added to each pixel. While this is a benign data set, it is instructive to consider such an idealized case in order to better understand the features of the algorithm.

Figure 3 shows the 1D marginalized posterior probability distributions for a variety of cases. The solid lines show a five-parameter "compact" source model fitted to the data. The five parameters are a flat background, the FWHM of a Gaussian point-spread function, the flux of the source, and its X- and Y-coordinates within the image. The dashed lines show the 1D marginalized posteriors for the case that the FWHM of the point-spread function is known (e.g., it may have been measured independently of this "observation"). The dotted lines show the 1D marginalized posteriors for the case in which the FWHM of the point-spread function is known and we have prior knowledge of the level of the background. Figure 4 shows the 1D marginalized posteriors for two parameters of the point-source photometry model. Prior positional knowledge has been included, in the form of a Gaussian prior on both X and Y (FWHM of 0.1 pixels). In this case, the rms noise of the observation has been increased four-fold, so that in the absence of the prior, the BIC value would favor an empty sky. This shows the case in which a source has been detected to high precision in another band but is very faint in this band. The Bayesian formalism allows us to fully and properly account for this.

![Figure 3](image3.png)

**Fig. 3.**—One-dimensional marginalized posterior probability distributions for the five parameters of the extended source photometry model (solid lines). Also shown are cases in which the FWHM prior is known perfectly (dashed lines) and where both the FWHM is known and there is a Gaussian prior on the background (dot-dashed lines). The input values are marked by vertical dotted lines.

![Figure 4](image4.png)

**Fig. 4.**—One-dimensional marginalized posterior probability distributions for two parameters of the point-source photometry model. Prior positional knowledge has been included, in the form of a Gaussian prior on both X and Y (FWHM of 0.1 pixels). In this case, the rms noise of the observation has been increased four-fold, so that in the absence of the prior, the BIC value would favor an empty sky. This shows the case in which a source has been detected to high precision in another band but is very faint in this band. The Bayesian formalism allows us to fully and properly account for this.
arising from analyzing the same source with 4 times the rms Gaussian noise. The FWHM is taken as known, as is prior knowledge of the source position. This simulates the case in which a source has been strongly detected at another band and we now wish to find an estimate of that source’s flux in this band. Figure 5 shows examples of 2D marginalized posteriors for the five-parameter “compact” source model. These illustrate the different correlations that exist between the fitted parameters.

4. CONCLUSIONS

In this paper, we have described a Bayesian formalism for the extraction of sources from astronomical data and have used it to derive two new source extraction methods. We then demonstrated the methods on simulated data.

The source detection filter is a deliberately uncomplicated implementation of this formalism; it is designed to analyze images quickly, something that is often crucial given the size of many modern astronomical surveys. Estimation of the image background is an often overlooked (and highly nontrivial) aspect of source extraction, and the simultaneous estimation performed by our filter makes unbiased background subtraction much more tractable. An additional point not to be overlooked is that by combining background subtraction and source detection, we have created a method that has essentially only one user-defined parameter (threshold), substantially simplifying its use.

We applied this filter to a deliberately challenging simulated image. The presence of a strong diffuse astronomical background introduces fluctuations on similar angular scales to the point-spread function, presenting a particular challenge for source extraction. Despite this, we are still able to detect the majority of sources, with only a few spurious detections. If computationally fast ways can be found to better model this background (work that is beyond the scope of this paper), even more impressive results may be possible in the future.

Once a candidate source position has been identified, we wish to characterize the source as precisely as possible. The advanced photometry method allows just that. It can determine the flux, position (to subpixel accuracy), local background, and (if required) point-spread function FWHM, along with the uncertainties on those estimates. Furthermore, it allows the meaningful comparison of different models, allowing us to determine (in an automated way) whether any given source is pointlike, extended, or even just a patch of empty sky. We can also include any additional prior knowledge we may have about the source. For example, if the FWHM is known, then the precision of our flux estimate is improved. With prior positional knowledge (from a strong detection in another band), we can obtain a flux estimate even when there is insufficient evidence from the data alone to identify a source.

This formalism allows us to ask precise, statistical questions of our data. We are able to include all pertinent information, giving us the best possible measurement and characterization of the sources. We can also determine a number of figures of merit, such as Bayesian evidence, BIC, and reduced $\chi^2$, all of which give measures of the quality of the extraction. Parameter-space search techniques such as MCMC sampling allow us to recover the statistical uncertainties on our measurements while making minimal assumptions. And model selection techniques allow us to ask which of a range of models best characterizes any given source.
In conclusion, in this paper we present the following:

1. A Bayesian formalism for the detection and extraction of compact sources from astronomical data.

2. The derivation of an analytic source detection filter that simultaneously detects point sources and estimates the image background.

3. The detailing of an advanced photometry method, which determines source parameters such as flux and position (to sub-pixel accuracy), as well as their uncertainties. It also allows us to determine the nature of the source (pointlike, extended) and to include any prior knowledge we may have, thus enhancing the precision of our results.

4. A method for optimizing the local region from which data should be used to make the source fits.

Bayesian source extraction is a highly powerful and (perhaps just as importantly) immensely flexible methodology. The ability to adapt our methods to the peculiarities of the data we are considering is a key degree of freedom when dealing with real astronomical data. Bayesian methods have historically been limited by lack of computing power; this is demonstrably no longer the case, giving us an array of new statistical tool with which to improve astronomical source extraction and hence the astrophysical science that depends upon it.

The methods described in this paper have been implemented as a beta-version, publicly available software tool (written in IDL). The code plus associated documentation and test data can be downloaded from the Sussex Astronomy Centre.1

R. S. thanks the Particle Physics and Astronomy Research Council for support under grant PPA/G/S/2002/00481. S. O. thanks the Leverhulme Trust for support in the form of a Leverhulme Research Fellowship. We thank Philippe André, Bruce Sibthorpe, and Tim Waskett for their kind provision of the simulated flux image shown in Figure 1. We thank Mike Hobson, Emmanuel Bertin, and Douglas Scott for useful comments and discussions. We thank the anonymous referee for useful comments.

1 See http://astronomy.sussex.ac.uk/~rss23/sourceMiner_v0.1.2.0.tar.gz.

REFERENCES


Guglielmetti, F., Fischer, R., Voges, W., Boese, G., & Dose, V. 2004, in Proc. 5th INTEGRAL Workshop, ed. V. Schönfelder et al. (ESA SP-552) (Noordwijk: ESA), 847


Pilbratt, G. L. 2004, BAAS, 36, 824

Schwarz, G. 1978, Ann. Stat., 6, 461


