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Specific star formation and the relation to stellar mass from $0 < z < 2$ as seen in the far-infrared at 70 and 160 $\mu$m


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ABSTRACT
We use the Spitzer Wide-area InfraRed Extragalactic Legacy Survey (SWIRE) to explore the specific star formation activity of galaxies and their evolution near the peak of the cosmic far-infrared (FIR) background at 70 and 160 $\mu$m. We use a stacking analysis to determine the mean FIR properties of well-defined subsets of galaxies at flux levels well below the FIR catalogue detection limits of SWIRE and other Spitzer surveys. We tabulate the contribution of different subsets of galaxies to the FIR background at 70 and 160 $\mu$m. These long wavelengths provide a good constraint on the bolometric obscured emission. The large area provides good constraints at low $z$ and in finer redshift bins than previous work. At all redshifts we find that the specific FIR luminosity decreases with increasing mass, following a trend $L_{\text{FIR}}/M_\star \propto M_\star^\beta$ with $\beta = -0.38 \pm 0.14$. This is a more continuous change than expected from the De Lucia & Blaizot semi-analytic model suggesting modifications to the feedback prescriptions. We see an increase in the specific FIR luminosity by about a factor of $\sim 100$ from $0 < z < 2$ and find that the specific FIR luminosity evolves as $(1 + z)^\alpha$ with $\alpha = 4.4 \pm 0.3$ for galaxies with $10.5 < \log_{10} M_\star/M_\odot \leq 12$. This is considerably steeper than the De Lucia & Blaizot semi-analytic model ($\alpha \sim 2.5$). When separating galaxies into early and late types on the basis of the optical/IR spectral energy distributions we find that the decrease in specific FIR luminosity with stellar mass is stronger in early-type galaxies ($\beta \sim -0.46$), while late-type galaxies exhibit a flatter trend ($\beta \sim -0.15$). The evolution is strong for both classes but stronger for the early-type galaxies. The early types show a trend of decreasing strength of evolution as we move from lower to higher masses while the evolution of the late-type galaxies has little dependence on stellar mass. We suggest that in late-type galaxies we are seeing a consistently declining specific star formation rate $\alpha = 3.36 \pm 0.16$ through a common phenomenon, for example, exhaustion of gas supply, i.e. not systematically dependent on the local properties of the galaxy.

Key words: surveys galaxies: evolution – galaxies: star formation – galaxies: stellar content – infrared: galaxies.

1 INTRODUCTION
A fundamental goal of modern astronomy is to understand the processes driving the formation and evolution of galaxies. A key issue
is the relationship between the assembly of galaxies and the formation history of the stars within those galaxies. A galaxy can increase its stellar mass through the accrual of stars in a ‘dry’ merger where the merger does not trigger new star formation or directly through star formation triggered by a merger or some other process. The star formation rates (SFRs) are determined by a variety of factors including the triggering mechanisms, the supply of gas and the feedback processes. The contribution from all of these processes to stellar mass buildup in galaxies is subtle and has been studied in numerous optical/near-infrared (NIR) photometric and spectroscopic surveys. These surveys have demonstrated that, as we increase in redshift, there is a strong dependency on at least two parameters – galaxy mass and local environment.

Galaxy mass is thought to play an important role, at least at $z \lesssim 1$ (Cassata et al. 2007). At low redshifts ($z \lesssim 0.2$), ongoing star formation in massive galaxies is almost entirely absent. Extreme levels of star formation are found rarely and in many cases are triggered by interactions and mergers. Moderate star formation is probably triggered by internal processes (Owers et al. 2007; Melbourne et al. 2008). As we move to higher redshifts however, this picture changes. Overall, the galaxy stellar mass function at high masses evolves fairly slowly up to $z \sim 0.9$, and then more rapidly up to at least $z \sim 2.5$, suggesting that the majority of stellar mass assembly took place at $z \gtrsim 1$ (Feulner et al. 2007; Pozzetti et al. 2007). Massive galaxies show little evidence for stellar mass assembly via either star formation or dry mergers at $z \lesssim 0.7$, while lower mass systems harbour ongoing star formation at all redshifts, lending support to the idea of ‘down-sizing’, in which more massive galaxies form most of their stars at high redshifts. There is also some evidence for ‘dry’ mergers (Bell et al. 2006). Finally, there is evidence that higher mass galaxies have lower specific star formation rates (sSFR; i.e. the SFR per unit stellar mass) than lower mass systems over a very wide redshift range, possibly up to $z \sim 4$, suggesting that lower mass galaxies form stars more efficiently (Bauer et al. 2005; Feulner et al. 2005; Zheng et al. 2007a), although the sSFRs of massive galaxies appear to increase rapidly with increasing redshift.

Local environment also has a significant effect. In the local Universe, we see a distinct environmental segregation, in which galaxies in rich environments show much lower SFRs than do galaxies in the field (Cassata et al. 2007; Cooper et al. 2007; Zauderer, Veilleux & Yee 2007). At high redshifts however this trend is reversed; at $z \sim 1$, the average SFR increases with increasing environmental density, as does sSFR (Elbaz et al. 2007), and morphological evolution appears to be more rapid in dense environments than in the field (Capak et al. 2007). Star-forming galaxies at $z \sim 1$ are in richer regions than seen in the local Universe (Farrah et al. 2006; Magnier et al. 2007), and there is evidence that star formation gradually shifts to lower density regions from $z \sim 1.5$ to 0 (de La Torre et al. 2007), thus providing a natural explanation for the local environmental segregation. Since environmental effects are so important we can only understand the universal properties when averaging over a representative sample of environments.

An important consideration is the feedback from supernovae or active galactic nuclei (AGN) which is required to suppress star formation in semi-analytic models (SAMs). A growing consensus is that the models require AGN feedback to suppress the star formation in massive objects (Bower et al. 2006; Croton et al. 2006), and this is in fact the dominant mechanism in De Lucia & Blaizot (2007).

The sSFR is a particularly useful probe of these processes. It measures the ratio between the current SFR and the historically averaged rate (e.g. Brinchmann et al. 2004; Walcher et al. 2008). Enhanced SFRs arising simply from an increase in gas reservoirs achieved through ‘dry mergers’ will not affect the sSFR, which is mainly sensitive to the triggering, fuelling and feedback, i.e. the overall star formation efficiency. Thus, the sSFR provides some decoupling of the merging and other phenomena.

There remains however a significant problem with these studies. The discovery of a strong cosmic infrared background (CIRB) by COBE (Puget et al. 1996; Hauser et al. 1998), and its subsequent (partial) resolution into a huge population of obscured star-forming galaxies at $z \gtrsim 1$ by ISO (Rowan-Robinson et al. 1997; Dole et al. 2001; Mann et al. 2002; Verma et al. 2005), Spitzer (Le Floc’h et al. 2005) and in the sub-mm (Hughes et al. 1998; Eales et al. 2000; Scott et al. 2002; Borys et al. 2003; Mortier et al. 2005), demonstrated clearly that a large fraction of the total star formation at high redshifts is heavily shrouded in dust and therefore impossible to detect at optical or near-IR wavelengths. This applies to even moderately luminous systems at $z \sim 1$ (e.g. Le Floc’h et al. 2005, their fig. 14). Therefore, optical/near-IR surveys to probe stellar mass assembly at high redshift miss a significant fraction of ongoing star formation.

The Spitzer Space Telescope (Werner et al. 2004) has allowed us to make great progress in understanding these obscured systems. However, even the recent surveys that combine optical data with 24 μm data do not solve this problem; the peak rest-frame emission from most IR-luminous galaxies is in the range 40–100 μm, but at $1 < z < 2$ the 24 μm Spitzer band probes rest-frame 8–12 μm, a region which can be highly contaminated with a range of features (i.e. polycyclic aromatic hydrocarbon emission, Si absorption, etc.). Spitzer does however have two longer wavelength channels, at 70 and 160 μm. The resolution and sensitivity of these channels are insufficient to directly resolve the far-infrared (FIR) background into the individual galaxies that produce it (e.g. Dole et al. 2004), but techniques exist to alleviate this. One of these techniques is known as ‘stacking’.

To understand galaxy evolution, it is thus essential to understand the obscured sSFR of galaxies (and massive galaxies in particular) over a representative range of galaxy environments. In this paper, we use a stacking technique to measure the specific FIR luminosity at 70 and 160 μm as a function of galaxy mass and redshift. To probe the highest stellar mass objects, which are rare, we use a large survey area. Although we do not explore the variation with environment in this paper, this large survey area also means we can be confident that we have covered a representative range of environments.

In Section 2, we discuss the samples. In Section 3, we describe our stacking technique. In Section 4 we present the results, which we discuss in Section 5, before concluding. We assume a spatially flat cosmology with $H_0 = 100h$ km s$^{-1}$ Mpc$^{-1}$, $\Omega = 0.7$, $\Omega_m = 1$ and $\Omega_m = 0.3$, and all magnitudes are Vega magnitudes.

2 CATALOGUES AND MAPS

2.1 SWIRE MIPS maps

The Spitzer Wide-area InfraRed Extragalactic Legacy Survey (SWIRE; Lonsdale et al. 2003, Lonsdale et al. 2004) observed 49 deg$^2$ in six fields [Chandra Deep Field-South (CDFS), Elais-N1, Elais-N2, Elais-S1, Lockman and XMM Large-Scale Structure (XMM-LSS)] using the seven primary Spitzer imaging bands (3.6–160 μm). The SWIRE 70 and 160 μm maps used here were observed using Multiband Imaging Photometer for Spitzer (MIPS; Rieke et al. 2004) medium scans as described in Shupe et al. (2008). The
70 μm maps were made from Basic Calibrated Data (BCD) images produced by the Spitzer Science Center (SSC) pipelines, after applying time filtering and column filtering following the prescription in Frayer et al. (2006), and are part of our Data Release 4. The filtered BCDs were mosaicked using the MOPEx package (Makovoz & Marleau 2005). The 160 μm maps were made by mosaicking the filtered BCD images produced by the SSC pipelines and correcting for a systematic 5 arcsec pointing offset. The maps are calibrated in units of surface brightness (MJy sr⁻¹). To bring the calibration in line with the facility calibration appropriate for the ‘S13’ pipeline processing (2006 May), we scale the maps up by a factor of 1.107 at 70 μm. The 160 μm maps for CDFS, XMM-LSS and Elais-N2 were multiplied by 1.064 while those of Lockman and Elais-N1 were unchanged (having already been reprocessed with the latest calibration), i.e. our map calibration is 702 MJy sr⁻¹ per MIPS-70 unit and 44.7 MJy sr⁻¹ per MIPS-160 unit (Gordon et al. 2006; Stansberry et al. 2006).

We estimate point-source fluxes, f (in mJy), by fitting the point-source response function (PRF) to the map intensity f (in MJy sr⁻¹). Our PRF is based on the default MIPS PRFs as recommended for use with APEX from the Spitzer Science Centre. These PRFs have the same pixel size as the SWIRE maps, i.e. 4 arcsec at 70 μm and 8 arcsec at 160 μm, and are oversampled by a factor of 4, i.e. 1 arcsec (for 70 μm) and 2 arcsec (for 160 μm). These PRFs are not identical to the ones used for the SWIRE catalogue extraction but the resulting difference calibration is less than 5 per cent and smaller than the absolute calibration uncertainty.

We define an effective beam size, \( \Omega_{\text{beam}} = f/I_0 = \int P \, d\Omega/P \) (where P is the PRF, d\( \Omega \) a solid angle and the zero subscript indicates the peak). We obtain \( \Omega_{\text{beam}} = 13.1 \, nSr \) at 70 μm and \( \Omega_{\text{beam}} = 61.5 \, nSr \) at 160 μm.

Finally, for consistency with the SWIRE catalogues we apply a colour correction to convert from the standard calibration for a 10,000 K blackbody to constant v f, more appropriate for galaxies. We therefore multiply the 70 and 160 μm fluxes by 1.09 and 1.043, respectively.

We have checked our calibration by comparing the map intensity at the position of catalogued MIPS sources (Afonso Luis et al., in preparation) and find a good agreement (within the absolute calibration uncertainties).

We note that the absolute SSC calibration is good to an accuracy of 7 per cent for 70 μm and 12 per cent for 160 μm (Gordon et al. 2006; Stansberry et al. 2006).

### 2.2 SWIRE optical/IR band-merged catalogues

The fields Elais-N1, Elais-N2, Lockman and CDFS currently have the most homogenous and well-understood SWIRE data. The catalogues we are using are those that were released as part of SWIRE Data Release 4 (Surace et al., in preparation). All Infrared Array Camera (IRAC; Fazio et al. 2004) and MIPS catalogues have been ‘bandmerged’, i.e. independent catalogues from the seven different bands (3.6, 4.5, 5.8, 8.0, 24, 70 and 160 μm) have been cross-matched to produce one master catalogue. In Elais-N1 and Elais-N2, we have five-band (Ugriz) photometry from the Wide Field Survey (WFS; Irwin & Lewis 2001, McMahon et al. 2001). In the Lockman Hole, we have three-band photometry (gri) from the SWIRE photometry programme, with some additional U-band photometry. In CDFS, we have three-band (gri) photometry, also from the SWIRE photometry programme. Good optical data exist in other SWIRE fields, notably the Canada–France–Hawaii Telescope Legacy Survey data in XMM-LSS and data from European Southern Observatory Wide Field Imager surveys in Elais-S1 (Berta et al. 2006; Berta et al. 2008); however, these fields have not been used for much of our analysis as it is known that our photometric redshift estimates are not as good in these fields.

Frost et al. (in preparation) have estimated completeness limits of u = 22.7, g = 23.8, r = 23.2, i = 22.4, z = 21.2 Vega magnitudes and \( f_{16,\mu m} = 10, f_{4.5,\mu m} = 15 \) mJy, and we use those estimates where required in our following analysis.

### 2.3 Photometric redshifts

We use the photometric redshifts given in Rowan-Robinson et al. (2008). These use the code IsomZ (Babbedge et al. 2004; Rowan-Robinson 2003 with updates as described in Rowan-Robinson et al. 2005; Babbedge et al. 2006) which has been extensively tested and applied to SWIRE data.

IsomZ is a template-fitting code that utilizes the optical and IRAC 3.6 and 4.5 μm detections to produce reliable photometric redshifts for both galaxies and AGN, accounting for extinction. The code has been tested against numerous spectroscopic data sets within the SWIRE fields with optical data down to r < 24 and spectroscopic redshifts \( z \lesssim 3 \) (though with most \( z < 1.5 \)). For all the samples, the mean systematic offset between the photometric and spectroscopic redshifts was found to be negligible to the precision of the photometric redshifts. For example, the Elais-N1 sample used by Babbedge et al. (2006) has a systematic offset of only \( \Delta z/(1 + z) = +0.0037 \). Rowan-Robinson et al. (2008) provide a detailed analysis of the catastrophic failure rate \( \eta \) and photometric accuracy \( \sigma_{\text{photo}} = \langle [\Delta z/(1 + z)]^2 \rangle \) as a function of number of photometric points, \( n_{\text{band}} \), magnitude cuts and \( \chi^2 \) from the fit. From their fig. 11, we estimate that we would find \( n_{\text{band}} \leq 5 \) per cent and \( \eta \lesssim 7 \) per cent with \( \chi^2 < 5 \) and \( n_{\text{band}} \geq 5 \) and \( r < 24 \). We use these constraints for the analysis presented in Section 4.1, though with a much brighter \( r < 23.2 \) limit. However, as shown in Frost et al. (in preparation) and discussed in Section 2.7 these constraints are difficult to model, so we modify them slightly for the analysis in Section 4.2. The \( \chi^2 \) constraint does not affect many galaxies and is difficult to adapt so we maintain this. We create a modified \( n_{\text{band}} \) measure being the number of bands that exceed the specific completeness thresholds \( u = 22.7, g = 23.8, r = 23.2, i = 22.4, z = 21.2 \) and \( f_{16,\mu m} = 10, f_{4.5,\mu m} = 15 \) mJy (as opposed to the more general requirement of a detection). We adopted a selection of \( n_{\text{band}} \geq 4 \) which provided a similar set of galaxies to \( n_{\text{band}} \geq 5 \) and thus, presumably, a similar redshift accuracy.

### 2.4 Optical classes and stellar mass estimation

We also used the spectral energy distribution (SED) classifications and stellar masses given in Rowan-Robinson et al. (2008, hereafter RR08). They adopted a two-pass approach in order to fit the photometric redshift, optical/NIR SED and FIR SED, making maximum use of the near/mid-IR Spitzer data. The optical and IRAC 3.6 and 4.5 μm bands are fit first with a range of optical/near-IR SEDs based on stellar population synthesis models. The main purpose of this first pass is to determine the level (if any) of excess emission in the Spitzer bands from dust, as well as separate AGN and galaxy spectral types for the second pass. The second pass includes a refitting of

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1\url{http://ssc.spitzer.caltech.edu/mips/dh/}

2\url{http://www.cfht.hawaii.edu/Science/CFHTLS/}
the optical SEDs to a finer redshift grid as well as a fit to the far-IR component of the data with a range of mid-IR to FIR templates. In this work, we do not make use of their FIR luminosities or classifications but we note that because of this two-pass method the optical luminosity estimates and hence stellar masses should not be biased by any residual FIR contamination in the mid-IR Spitzer bands.

The stellar masses use stellar synthesis templates (see section 3, fig. 1 and table 2 of RR08). Starting with empirical templates from Yoshii & Takahara (1988) for galaxies of type E, Sab, Sbc, Scd, Sdm, and from Calzetti & Kinney (1992) for starbursts, RR08 used spectroscopic data for 5976 galaxies, for many of which they have 10-band photometry from the CFHT12K–VIRMOS survey (Le Fèvre et al. 2004), to improve these empirical templates. The latter were then regenerated to higher resolution using simple stellar populations, each weighted by a different SFR and extinguished by a different amount of dust, $A_V$. This procedure, based on the synthesis code of Poggianti, Bressan & Franceschini (2001), gave the templates a physical validity. Minimization was based on the Adaptive Simulated Annealing algorithm. Details on this algorithm and on the fitting technique are given in Berta et al. (2004).

For each galaxy, they estimate the rest-frame 3.6 μm luminosity, $\nu L_\nu(3.6)$, in units of $L_\odot$, and using the stellar synthesis models estimated the ratio $(M_*/M_\odot)/(\nu L_\nu(3.6)/L_\odot)$ to be 38.4, 40.8, 27.6, 35.3, 18.7 and 26.7, for types E, Sab, Sbc, Scd, Sdm and sb, respectively. (Note: measuring the 3.6 μm monochromatic luminosity in total solar units, not in units of the Sun’s monochromatic 3.6 μm luminosity.) Alternatively estimates of $M_?$ using the B-band luminosity agree with our preferred method to within 10–20 per cent. Estimates based on 3.6 μm should be more reliable, since there is a better sampling of lower mass stars and less sensitivity to recently formed massive stars. These mass estimates would be strictly valid only for low redshift. For higher redshifts, the mass-to-light (M/L) estimates will be lower since for the oldest stellar populations M/L varies strongly with age (Bruzual & Charlot 1993, see their fig. 3). This can be approximately modelled using the Berta et al. (2004) synthesis fits described above, with an accuracy of 10 per cent, as $(M_*/M_\odot)/(\nu L_\nu(3.6)/L_\odot) = 50/\alpha_0 + 1.17(t - \alpha_0^{-0.01})$ where $t_0$ is the present epoch and $\alpha_0 = 0.15, 0.08, 0.06, 0.26, 1.44, 0.70$ for SED types E, Sab, Sbc, Scd, Sdm and sb, respectively.

This approach should correctly capture the different evolutionary behaviours of stellar masses in star-forming galaxies and of early-type galaxies.

For each galaxy, we have the best-fitting photo-$z$, the template classification and stellar mass. There are 15 numbered optical classifications: Ellipticals (1–2), Sab (3), Sbc(5), Scd(7), Sdm (9), starburst (11), AGN (13-15) with types 4, 6, 8, 10 intermediate between the other optical templates. For much of our analysis we exclude the galaxies best fit by AGN templates as their photo-$z$ are poor, and the estimates of their star formation and stellar mass will be strongly contaminated by the AGN.

2.5 Masks

We have constructed a conservative mask based on those used in the clustering analysis of Frost et al. (in preparation). Those clustering masks exclude regions where (1) the optical data are insufficient for reliable photo-$z$ determinations, (2) the IRAC completeness was low and/or variable and (3) foreground stars were located. Specifically we include only those optical frames where the $r_{90}$ depth was recorded as 23.2 or better. This $r_{90}$ depth is an estimate of the $r$-band 95 per cent completeness limit and $r_{90} = 23.2$ is the expected depth for good photometric nights. This means we are selecting good quality optical fields. Our optical catalogues are also restricted to $r = 23.2$. We reject areas where the IRAC coverage was less than four pointings, ensuring the completeness is above 90 per cent and variations are less than 2 per cent at 10 μJy. We also apply a coverage cut of 30 at 24 μm giving completeness >90 per cent and variation of a couple of per cent for 24 μm sources above 400 μJy. To mask stars, we follow the method of Waddington et al. (2007) in which Two-Micron All-Sky Survey (Skrutskie et al. 2006) point-source catalogue sources with $K < 12$ are identified to be stars and a circular mask of radius, $R$, with $\log_{10}(R/\text{″}) = 3.1 - 0.16 K$ is applied. We additionally exclude regions where the MIPS coverage is poor relative to the majority of the data with a threshold chosen by examining the histogram of the coverage. For the MIPS 70 μm we use a coverage threshold of 12, while for the 160 μm we use a coverage threshold of 3.

Although parts of our analysis could be carried out with less conservative masks, we choose to apply the same mask to all the work in this paper so we are always comparing sources in the same area of sky. With our aggressive masking the unmasked areas of the four fields Elais-N1, Elais-N2, Lockman and CDFS are $\Omega = 4.33, 2.41, 2.75$ and 1.85 deg$^2$, totalling 11.33 deg$^2$.

2.6 Subsample selection

For part of our analysis, we divide the sample into stellar mass and redshift ($M_*, z$) cells over a range $0 \leq z \leq 2.0$ and $9.0 \leq \log_{10}(M_*/M_\odot) \leq 12$. Cell sizes were selected to provide relatively uniform number of sources in each cell and thus a reasonable balance between signal-to-noise ratio and resolution on a scale that is easy to compare with other data and models. Our cell boundaries are $z = 0.2, 0.3, 0.4, 0.5, 0.6, 0.8, 1.0, 1.25, 1.5, 2$ and $\log_{10}(M_*/M_\odot) = 9, 9.25, 9.5, 9.75, 10, 10.25, 10.5, 10.75, 11, 11.4, 12$. The stellar mass and redshift distribution of the cells is shown in Fig. 1.

With redshift slices of $\Delta z \approx 0.2$ and area of $\Omega = 11.33$ deg$^2$, our sample covers a co-moving volume of $6.3 \times 10^6 h^3$ Mpc$^3$ at $z = 1$. Numerical simulations (Mo & White 2002) predict that this volume is sufficient to include the progenitors of six of today’s $10^{12} M_\odot$ clusters, which have a comoving number density of $10^{-6} h^3$ Mpc$^{-3}$, arguing that we probe a fair sample of the Universe.

2.7 Selection effects

Our sample and photo-$z$ selection criteria are complex, so we need to be cautious about selection effects. In summary, our selections for the stellar mass analysis are $f_{16 \mu m} > 10 \mu Jy$, $r < 23.2$, $n_{band} \geq 4$, $\chi^2 < 5$, template classification $j_2 < 13$ and lying outside the mask defined in Section 2.5.

We are primarily investigating the mean FIR luminosity to stellar mass ratio, i.e. the specific FIR luminosity, and are not concerned with the total number of sources or the luminosity density. Thus, in any $M_*$, $z$ cell we only need to worry about selection effects that affect subpopulations within the cell in different ways. In other words, our estimate of the mean specific FIR luminosity in a cell would be unaffected if we randomly exclude 50 per cent of all galaxies in the cell but would be affected if we exclude 50 per cent of the most FIR luminous and none of the others.

The $\chi^2$ selection might affect some galaxy types more than others; however, with a broad range of templates, carefully modified to fit

3http://astronomy.sussex.ac.uk/~sjo/masks/
the SWIRE populations, we expect that this cut will have a smaller effect than the flux-related criteria.

The number of bands criteria and the flux cuts do need to be considered. Since different galaxies have different $K$-corrections, this introduces some differential effects. As noted by Frost et al. (in preparation), in a cell of fixed stellar mass (or 3.6 $\mu$m luminosity) and redshift the optical cuts will exclude redder galaxies. As these galaxies typically have lower sSFRs, ignoring this effect would artificially inflate our specific FIR luminosity estimates. To account for this, we weight the galaxies to account for this incompleteness and flag as incomplete cells where our incompleteness corrections may be inadequate.

For all cells we use a $V_{\text{max}}$ weighting. The model templates give us a $K$-correction in every band. For each galaxy, we use our measured $K$-correction and observed magnitude to calculate the maximum observable redshift $z_{\text{max},i}$ in each band, $i$. We then compute $z_{\text{max}}$ taking into account our 3.6 $\mu$m, r-band and $n'$-band constraints. The available volume can then be calculated taking into account the cell limits and $z_{\text{max}}$. We also flag as incomplete any cells in which for any template; (1) we found no examples of galaxies best fit by that template and (2) a galaxy with that template could not, in principle, have been found in the cell, given the quoted selection limits. Later, we also exclude any cells with fewer than 100 galaxies.

3 STACKING METHOD

Stacking analysis co-adds the signal in a map at the position of a class of galaxies, allowing for the reduction of noise associated with measurements of individual galaxies, whether this be confusion noise (e.g. Condon 1974) or instrumental/background noise. The level of noise reduction is governed by a number of factors, including the ability to categorize the target catalogues into groups with similar properties and the resulting number of targets on which the stack is performed. Stacking has been used at sub-mm wave-lengths (e.g. Peacock et al. 2000; Dye et al. 2007; Takagi et al. 2007; Serjeant et al. 2008) and has successfully been applied to Spitzer data (Dole et al. 2006). Stacking has also been used to investigate the FIR SEDs of Spitzer galaxies in small fields at $z \sim 0.7$ (Zheng et al. 2007b) and $1.5 < z < 2.5$ (Papovich et al. 2007).

The conventional stacking technique is to extract a region from the map around each target source and stack these together to produce an average image. A mean background is subtracted; usually estimated either from the global map or from the extremities of the average image. The average flux is then determined by either calculating the total flux in some aperture or fitting the point-spread function to the image. If the noise in the original maps is uncorrelated with the target sources (being either instrumental noise, background thermal noise, confusion noise from unrelated galaxies or foregrounds such as Galactic cirrus), then the noise in the average map will be reduced by a factor of $\sqrt{N}$ where $N$ is the number of targets. Furthermore, if $N$ is large then the noise will approach a Gaussian distribution due to the central limit theorem. Under the assumption that the targets are isolated and point-like at the telescope resolution a suitably weighted point-source profile fit is the optimal estimator of the average flux of the targets.

An additional contribution to the average flux will come from sources that are spatially correlated with the target galaxies. This is a difficult contribution to model as it depends on the correlation function of galaxies which may be luminosity- or type-dependent. We discuss this further in Section 3.1. In order to minimize this bias, we fit the point-source profile and a constant background simultaneously over a limited radius. (A similar technique for source detection and photometry has been discussed by Savage & Oliver 2007.) The simultaneous fit means that the background is estimated from a local area that includes the region under the source, in contrast to methods using a sky annulus which exclude the source region. The point-source fitting and limited radius means that the central parts of the image, where the source flux dominates any correlated background, have a greater weight.
We performed the fit in one dimensional using a radial point-source intensity profile $P(r)$ estimated from the two-dimensional (2D) calibration profile $I(r) = I_0 N_P(r)/P_0 + b$ was fit, limiting the data to that within the first Airy disc minimum. We used a minimum $\chi^2$ fit with errors in the mean image intensity estimated from the scatter between the individual images in the stack. This would be optimal if the population variation is small and the errors are uncorrelated, so it probably underweights the central pixels but is adequate for our purposes. From $I_0$ we deduce the flux, $f$, using the effective beam calibration factor, $\Omega_{\text{beam}}$, given earlier. Looking at the $\chi^2$, we find reasonable fits whenever we have nine or more galaxies.

It is simple to use the central limiting behaviour of the stacking technique to get a good estimate of statistical error in the flux. However, we are concerned about systematic noise terms and so will use an error calculation based on the variation from field to field (see Section 3.3). Our technique can easily be extended to include correlated errors, to accommodate a model for any background (e.g. one from correlated sources) and also to provide an estimate for the variation in the population flux as well as the mean.

### 3.1 Simulations

From the beam sizes calculated above we see that the density of beams on the sky is 21,000 and 4700 deg$^{-2}$ at 70 and 160 $\mu$m, respectively. Comparing these with Table 1 we can see the number of sources per beam can be high, particularly at 160 $\mu$m. We should thus be concerned about confusion, i.e. where correlated neighbouring sources spuriously increase the stacked flux.

Our method aims to mitigate this problem by using the simultaneous source and background fitting. To test this we have run some simulations. We need to investigate the behaviour in high and low source density regimes and to include galaxy clustering. Our approach is to use the real catalogue positions. For the low source density case, we take the sources with $S_{24} > 400$ $\mu$Jy. We are not interested in the absolute fluxes, so we model the long-wavelength fluxes as $S_{30} = S_{160} = S_{34}$. We insert these fluxes at the catalogue positions and convolve with the corresponding 2D PRF. For the high source density case we repeat this using sources with $S_{16} > 10$ $\mu$Jy. We then undertake our stacking analysis using the same stellar mass and redshift cells. We do not add noise to the simulations as we are concerned here with systematic biases from confusion. The results are shown in Fig. 2.

These simulations show that the uncertainties increase as the mean flux in the stack decreases. The results are roughly similar for the two different sample densities and the two different beam sizes. At any given flux, the uncertainties appear to be larger for smaller stack samples. If we only consider the larger stack samples, then there is some indication of systematic underestimation of the simulated flux at faint fluxes. This effect appears to be less than 0.5 dex. At first glance this is surprising since our naive expectation was that the correlated signal would increase the fluxes. This suggests that our background estimation is biased upwards by the correlated flux. In principle, we could model this bias. However, our simulation is limited as (1) we have assumed a direct correlation between the long- and short-wavelength fluxes and (2) we have ignored the contribution from sources with higher space densities than the SWIRE 3.6 $\mu$m sample. The first assumption is difficult to model as it relies on an understanding of both the luminosity and clustering properties of the FIR-emitting galaxies which are poorly constrained.

As we show in Table 1 the second assumption is relative modest as we appear to resolve much of the FIR background within the SWIRE sample. However, we note that the SWIRE catalogues will not have resolved sources closer than the 3.6 $\mu$m beam and so will underestimate the number of close pairs. Had such close pairs been included it would have counteracted the observed bias.

We conclude from the simulations that systematic effects due to source correlation in highly confused regions may underestimate the fluxes at low fluxes, but by a factor smaller than 0.5 dex.

### 3.2 From stack fluxes to background intensities and luminosities

The stacking technique naturally gives us the mean flux of galaxies in a class.

---

**Table 1.** Contributions to the 70 and 160 $\mu$m FIR background from various populations. All catalogues and maps have been masked by the mask described in the text. The first four rows are galaxies extracted from the Spitzer data only catalogues. The fifth row comes from the Spitzer/optical cross-matched catalogues. The remaining rows above the line are extracted from the photo-z catalogues of RR08 which have been filtered to remove galaxies with poor-quality photo-z and classifications (i.e. those with $n_{\text{band}} < 4$, or $\chi^2 \geq 5$). The data are averaged over four fields, Elais-N1, Elais-N2, Lockman and CDFS, weighted by the unmasked areas of 4.33, 2.41, 2.75, 1.85 deg$^2$, respectively, for a total of 11.33 deg$^2$. Errors are deduced from the field-to-field variations. The last two rows are estimates extracted from table 1 of Dole et al. (2006).

<table>
<thead>
<tr>
<th>Selection</th>
<th>Number</th>
<th>Number Density /1000 (deg$^2$)$^{-1}$</th>
<th>$I_{70}$ /nW m$^{-2}$ sr$^{-1}$</th>
<th>$I_{160}$ /nW m$^{-2}$ sr$^{-1}$</th>
<th>$I_{70}/I_{160}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{24} &gt; 10$ $\mu$Jy</td>
<td>394014</td>
<td>34.8 ± 1.6</td>
<td>4.231 ± 0.085</td>
<td>8.77 ± 0.44</td>
<td>0.48 ± 0.03</td>
</tr>
<tr>
<td>$S_{24} &gt; 400$ $\mu$Jy</td>
<td>21446</td>
<td>1.87 ± 0.05</td>
<td>2.159 ± 0.066</td>
<td>3.17 ± 0.06</td>
<td>0.68 ± 0.02</td>
</tr>
<tr>
<td>$S_{30} &gt; 30$ mJy</td>
<td>856</td>
<td>0.076 ± 0.004</td>
<td>0.703 ± 0.039</td>
<td>0.68 ± 0.03</td>
<td>1.04 ± 0.08</td>
</tr>
<tr>
<td>$S_{34} &gt; 90$ mJy</td>
<td>877</td>
<td>0.077 ± 0.003</td>
<td>0.542 ± 0.041</td>
<td>0.71 ± 0.04</td>
<td>0.76 ± 0.07</td>
</tr>
<tr>
<td>$S_{36} &gt; 10$ $\mu$Jy; $13.5 &lt; r &lt; 23.5$</td>
<td>223402</td>
<td>19.7 ± 0.6</td>
<td>3.247 ± 0.099</td>
<td>5.71 ± 0.32</td>
<td>0.57 ± 0.04</td>
</tr>
<tr>
<td>$13.5 &lt; r &lt; 23.5$; $\chi^2 &lt; 5$; $n_{\text{band}} \geq 4$</td>
<td>182672</td>
<td>16.1 ± 1.0</td>
<td>2.390 ± 0.235</td>
<td>4.28 ± 0.38</td>
<td>0.56 ± 0.07</td>
</tr>
<tr>
<td>E ($j_2 = 1, 2$)</td>
<td>29700</td>
<td>2.62 ± 0.09</td>
<td>0.260 ± 0.023</td>
<td>0.56 ± 0.05</td>
<td>0.47 ± 0.06</td>
</tr>
<tr>
<td>Sab ($j_2 = 3, 4$)</td>
<td>9727</td>
<td>0.86 ± 0.05</td>
<td>0.198 ± 0.013</td>
<td>0.38 ± 0.02</td>
<td>0.52 ± 0.05</td>
</tr>
<tr>
<td>Scb ($j_2 = 5, 6$)</td>
<td>23306</td>
<td>2.06 ± 0.12</td>
<td>0.417 ± 0.043</td>
<td>0.80 ± 0.06</td>
<td>0.52 ± 0.07</td>
</tr>
<tr>
<td>Scd ($j_2 = 7, 8$)</td>
<td>54864</td>
<td>4.84 ± 0.20</td>
<td>0.911 ± 0.070</td>
<td>1.63 ± 0.12</td>
<td>0.56 ± 0.06</td>
</tr>
<tr>
<td>Sdm ($j_2 = 9, 10$)</td>
<td>37504</td>
<td>3.32 ± 0.28</td>
<td>0.293 ± 0.056</td>
<td>0.45 ± 0.08</td>
<td>0.65 ± 0.17</td>
</tr>
<tr>
<td>Starburst ($j_2 = 11$)</td>
<td>23549</td>
<td>2.08 ± 0.17</td>
<td>0.276 ± 0.078</td>
<td>0.46 ± 0.08</td>
<td>0.60 ± 0.20</td>
</tr>
<tr>
<td>AGN ($j_2 = 13 - 15$)</td>
<td>3887</td>
<td>0.34 ± 0.12</td>
<td>0.053 ± 0.019</td>
<td>0.06 ± 0.03</td>
<td>0.89 ± 0.51</td>
</tr>
<tr>
<td>$S_{24} &gt; 60$ $\mu$Jy</td>
<td>594 ± 1.02</td>
<td>10.72 ± 2.28</td>
<td>6.4</td>
<td>15.5</td>
<td></td>
</tr>
</tbody>
</table>
Specific star formation in the FIR

Figure 2. Ratio of the output to input flux ratios for simulations of our stacked samples. Flux units are arbitrary. We use the stack samples from the Elais-N1 field (our largest field, the total sample has over twice this area). The colours of the symbols indicate whether we placed the FIR fluxes at the location of 3.6 or 24 μm sources and whether we used the 70 or 160 μm beam. Symbol sizes relate to sample sizes in the same way as Fig. 1, except the symbol sizes are reduced by a factor of 2. Cells with fewer than 10 sources are marked with crosses.

To derive the contribution of that class to the background intensity (νfν), we take the flux per unit frequency and divide by the unmasked area of the catalogue from which that class was selected, i.e. νfν = ν ∑ wi. Then, rather than dividing the total stack by the number of galaxies, we divide by ∑ νi. The luminosity distance, Dl, and K-correction, K_FIR, transform flux into FIR luminosity while the stellar mass, M_*c, converts to specific luminosity and the Vmax terms correct for the incomplete sampling of the cell volume.

To calculate K_FIR, we use a mean SED averaged over all galaxies in the cell. In Fig. 3, we compare the 70/160 colours of all the cells with model templates from Polletta et al. (2007) and individual galaxies detected in both bands. The individual detections have similar colour distribution to the stack samples but with a tail to warmer colours. This tail is expected because the detection criteria select the most FIR luminous objects and there is a well-known correlation between FIR luminosity and dust temperature (e.g. Chapman et al. 2003). No single template fits all the samples at all redshifts. However, we see that the Sc template (plotted with a thicker line style) provides as good a fit as any other template over the range of classes and redshifts. This is natural as we would expect the mean SED to be roughly the same as a galaxy with a moderate level of FIR activity.

We thus adopt an Sc template as a reasonable compromise between the different SEDs and use this to compute the FIR luminosity, LFIR, where we define the FIR range to be from 5 μm < λ < 1000 μm, from 70 or 160 μm fluxes. It should be noted that the Sc template peaks at 100 μm (in νfμ) or 130 μm (in fν) so the K-corrections at the two different wavelengths are different (in opposite directions for z < 0.2). Fig. 4 shows a wide variety of empirically based SEDs for galaxies detected in IR bands. We see that the 160 μm band on its own is reasonable bolometric power indicator, i.e. any uncertainties in which template is appropriate have a small effect on the K-correction.

If the FIR luminosity traces the star formation activity, then the specific FIR luminosity is a measure of the sSFR. However, the FIR luminosity also traces emission from AGN and from diffuse dust heated by the ambient stellar radiation field (‘cirrus’). The AGN emission is warmer than either star formation or cirrus and is expected to be less significant at these long wavelengths. This is confirmed by our SED analysis in Section 4.1. The well-known FIR–radio correlation (e.g. Condon 1992) suggests that even the cool ‘cirrus’ emission indirectly traces star formation. Strong AGN with modest extinction are excluded by the optical SED modelling. Weaker or more obscured AGN will remain and provide some level of contamination. The level of this contamination is hard to estimate but typically AGN fractions are found to be ~30 per cent (e.g. Polletta et al. 2006). A strong AGN contamination would reveal itself in differences between our estimates arising from 70 and 160 μm. Thus, it is plausible to relate the total FIR luminosity to the obscured SFR. We relate the FIR luminosity to the total SFRs (i.e. including an estimate of the unobscured contribution) using the conversion from Rowan-Robinson et al. (1997) and RR08 expressed as

$$\frac{L_{\text{FIR}}}{L_{\odot}} = 0.51 \times 10^{10} \frac{\text{SFR}}{M_{\odot}\text{yr}^{-1}},$$

where we have taken the fraction of ultraviolet (UV) energy absorbed by dust to be $\epsilon = 2/3$, and $L_{\text{FIR}}/L_{\odot} = 1.67$. These values
3.3 Error estimation

To estimate the systematic uncertainties, we calculate our errors using the variation in mean fluxes we get from field to field.

are appropriate for an M82-like spectrum. It is worth noting that if the obscuration is less than this, as you might expect for systems with less active star formation, then we will underestimate the SFR.

Figure 3. $f_ν$ colours ratios at 70/160 μm for stack subsamples. Filled circle data points are stack samples, colour coded according to stellar mass using the same scheme as for Figs 9–11. Black data points are catalogued galaxies extracted from the SWIRE Elais-N1 field. Model templates are taken from Polletta et al. (2007).

Figure 4. Bolometrically normalized SEDs for a range of models from Xu et al. (1998). SEDs are shown in the rest frame and are normalized to have the same power over the range 5 < $λ/μm$ < 1000. The models include starburst galaxies, normal spirals and AGN. Overplotted are the three Spitzer MIPS bands (24, 70 and 160 μm) for a galaxy observed at $z = 1$. Note that the bolometric normalization is similar to normalization at 100 μm. Our analysis uses 70 and 160 μm, much previous work uses 24 μm.
This approach accounts for sampling variance errors and some of the systematic errors arising from our use of photometric redshifts. Although our photometric redshift technique is the same across all the fields, the optical data come from different telescopes; this means the field-to-field variations could be significant if the photo-$z$ has any subtle dependencies on the bands or optical limits.

The areas of each field $\Omega_i$ are given in Section 2.5. For each subsample, we calculate an average flux (or specific star formation) weighted by these areas $\bar{f} = \sum_i \Omega_i f_i / \sum_i \Omega_i$. We estimate the error on the resulting weighted average as

$$\sigma_{\bar{f}}^2 = \frac{1}{\sum_i (\sum_i \Omega_i)^2 - \sum_i \Omega_i^2} \sum_i \Omega_i (f_i - \bar{f})^2.$$  

The first term is a factor to scale from the population variance to the variance in the mean, the next two terms are the weighted estimator for the population variance.\(^4\)

Any stacks with fewer than nine galaxies (the threshold for reasonable $\chi^2$ found in Section 3) were excluded from the average and any cells that had fewer than 100 galaxies after the averaging were excluded.

4 RESULTS

4.1 Contributions to CIRB from various observational subsamples

Before we examine the specific FIR luminosity, we explore the contribution of different subsets of the SWIRE catalogues to the CIRB. These are tabulated in Table 1.

The SWIRE galaxies which are bright enough to be detected individually at 70 or 160 $\mu$m (rows 3 and 4) contain only a small fraction ($\lesssim 12$ per cent) of the CIRB information of the SWIRE data set as a whole (row 1) which provides strong motivation for our stacking analysis. The optical subsample (row 5) contains about 60 per cent of the FIR information. This selection is similar to that used in most of this paper. It is encouraging that we detect much of the FIR flux, however, it emphasizes the need for deeper optical data to fully exploit the SWIRE data. The SWIRE 24 $\mu$m catalogues detect about half of the CIRB seen in the 3.6 $\mu$m sources. We find that SWIRE 24 $\mu$m catalogues resolve 30–40 per cent of the CIRB seen by Dole et al. (2006) in fainter 24 $\mu$m samples, while the SWIRE 3.6 $\mu$m catalogues resolve 70–80 per cent. Estimation of the total CIRB from direct measurement is highly uncertain but if we use the estimates quoted by Dole et al. (2006) then the SWIRE 3.6 $\mu$m catalogues resolve about 70 per cent of the 70 $\mu$m background and 60 per cent of the 160 $\mu$m background. Roughly half of the background is resolved in the optical samples at $r < 23.5$.

Some other points to note from this table are that the FIR colours generally become warmer as we move from early to late types, starbursts and AGN (as expected). As we noted before when discussing Fig. 3, the colours of sources catalogued at 70 or 160 $\mu$m are warmer than those selected at other bands. This is because these sources tend to have higher FIR luminosity and are thus preferentially starburst galaxies or AGN. This effect is less pronounced at 160 $\mu$m which picks up cooler sources.


4.2 Specific far-infrared luminosity as a function of stellar mass

To explore the specific star formation, we measure the ratio of FIR luminosity to stellar-mass, i.e. the specific FIR luminosity. An early exploration of this as a function of optical luminosity (as a proxy for stellar mass) from ISO data was presented by Oliver & Pozzi (2005). We use the stellar mass and redshift cells described in Section 2.6.

In Figs 5 and 6, we plot the specific FIR luminosity as a function of stellar mass. We omit points where the fractional error (calculated using the field-to-field variations) is more than 1. Data points flagged as incomplete (Section 2.7) are unfilled.

We see similar results at both 70 and 160 $\mu$m. This agreement is an important validation of our method as the data are completely independent and the $K$-corrections applied are very different. We are thus confident in combining the two data sets to give a single estimate of the specific FIR luminosity (being a weighted average of the estimate at each wavelength). The scatter between the two independent wavelengths is indicated in the error bars.

In Fig. 5, we compare our average specific FIR luminosity in our lowest redshift bin (where we cover the widest mass range) with other data from the literature. We see a simple power-law trend but a shallower slope, particularly with higher specific star formations at higher masses. The Chen et al. (2009) work models the Sloan Digital Sky Survey (SDSS) spectra and is sensitive to star formation over a longer time-scale ($\sim 1$ Gyr) than the FIR. This may lead them to find higher sSFRs due to the evolution over that timescale. Alternatively, this may be an obscuration effect, if the optical observations miss heavily obscured star formation and if that deficit is greater in higher mass systems. This might be expected if star formation in massive systems tends to be in more deeply embedded sites as seen in Arp 220. The analysis of Damen et al. (2009) includes star formation measures from 24 $\mu$m and so should include obscured star formation, but may miss cooler contributions that we pick up at longer wavelengths. This latter explanation is tentatively supported by the IRAS measurements from Zheng et al. (2007b) at longer wavelengths which lie between our results and those of Damen et al. (2009). The remaining discrepancy between our work and Zheng et al. (2007b) (at lower $z$) could then be explained as due to evolution over our redshift bin, which will preferentially increase the sSFR in the higher mass bins. A final possibility is that there are inconsistencies in the stellar mass estimates, either through modelling or through photo-$z$ estimates. This is likely to be more of a problem for us at these lower $z$, where photo-$z$ errors are more significant, than it is at higher $z$.

Comparing with data at higher redshifts (Fig. 6), the agreements are much better. Our large area means we are able to divide our data into finer redshift bins than previous work while still maintaining high statistical precision. We find similar slope and amplitude to obscured tracers, for example, estimated from 24 $\mu$m data (Zheng et al. 2007b). Their observations were over a much smaller field and so they were limited to lower stellar masses. At $z > 1$ we find sSFR significantly higher than Damen et al. (2009) (who included FIR indicators), but similar to those found by Dunne et al. (2009) (who use radio). Our slope is hard to compare with Dunne et al. (2009) as their redshift ranges are much larger and differential evolution across their bin will be significant. Elbaz et al. (2007) derived an empirical relation from 24 $\mu$m and UV data and quote SFR/(M$_\odot$ yr$^{-1}$) $= 7.2(M_{\odot}/(10^{10} M_\odot))^{0.7}$ at $0.8 < z < 1.2$, again limited to lower stellar masses. The Elbaz et al. (2007) measurement has a consistent amplitude in the limited range where our stellar mass ranges overlap. However, they have a shallower slope than
Figure 5. Specific FIR luminosity or sSFR as a function of stellar mass in redshift classes. Redshift ranges from 0 < z < 0.2. Filled circles are the average of our estimates from the 70 and 160 μm data which are the weighted average over four fields (Elais-N1, Elais N2, Lockman and CDFS). Thick vertical error bars come from the field-to-field scatter and thin error bars with hats from the variation between 70 and 160 μm estimates. All points have used at least 100 galaxies in the stacking analysis. Solid lines are our power-law trends with parameters given in Table 2. Calibration to specific star formation (right-hand axis) is given in the text. Previous estimates of specific star formation rates are estimated from 24 μm data (stars) (Damen et al. 2009) (0.1 < z < 0.3), IRAS (open circles) (Zheng et al. 2007a) z ≲ 0.02 and from SDSS spectra (triangles) z ∼ 0.1 (Chen et al. 2009). Dashed lines are predictions from the SAMs of De Lucia & Blaizot (2007).

Ours and that of Zheng et al. (2007b); this might be an effect of differential evolution across their wide redshift bin.

Overall it seems that the relations are smooth and there is no strong evidence for any breaks. However, there is a need for consistent measurements over a wide dynamic range in mass and in narrow redshift bins.

There is a strong evolutionary trend which we explore in more detail in Section 4.3. Looking within each redshift bin (while bearing in mind that we only see lower mass objects at lower redshifts) we see that there is a consistent decline in specific FIR luminosity as we move to higher stellar mass. We model this trend as

$$sSFR = \frac{SFR}{M_*} \propto \left( \frac{M}{10^{11} M_\odot} \right)^\beta$$

This power-law model is a reasonable fit and parameters for the average fit are given in Table 2. There is some variation in the slope with redshift, the slope is steeper for 0.6 < z < 0.8, but a mean value of $\beta = -0.38 \pm 0.14$ provides a plausible description of the data.

For a direct comparison with SAMs, we take the simulations of De Lucia & Blaizot (2007) and select galaxies in the same stellar mass and redshift cells as our data. This model includes AGN feedback which effectively suppresses star formation for galaxies with large central black holes (typically galaxies with $M > 10^{10.5} M_\odot$). The comparison is shown in Fig. 5 for our lowest z bin and in Fig. 6 for the others. This model fits our low-mass data well, but the model underpredicts our high-mass end. The same model agrees better with other data sets at the high-mass end but not as well at lower mass. The shapes of the model curves are identical at higher redshifts with just the normalization increasing. The clear break in the model curves arises at the mass scale where the AGN feedback becomes important. We do not see such a break in any redshift bin. In addition, this model fails to predict the amplitude of the evolution with redshift which we discuss in Section 4.3.

We perform the same analysis for galaxies separated by the optical/NIR SED class. We show the separation into late-type galaxies (SED types 3–11) in Fig. 7 and early-type galaxies (SED types 1–2; Fig. 8) with fit parameters in Table 2. It is immediately striking that the relationships are much steeper (though naturally lower amplitude) for the late-type galaxies $\beta \sim -0.15$ for the early-type galaxies.

We have performed the same analysis on all of the different optical galaxy classifications, and these show a logical progression between the behaviours seen in the early and late groupings shown here. A figure illustrating this is shown in Roseboom et al. (2009).

If we ignore the highest redshift bin, for which the slope is poorly constrained, there is some indication from these figures and Table 2 that the slope of the relation between sSFR and stellar mass becomes steeper with increasing redshift for both early- and late-type galaxies and for all galaxies combined.

4.3 Specific FIR luminosity as a function of redshift

By plotting the same data as a function of redshift but in stellar mass classes the evolutionary trend is readily apparent, see Fig. 9. It is

$^5$Publicly available on the Millennium Simulation data download site (see Lemson & Virgo Consortium 2006).
Again, we see the same trends in both the 70 and 160 μm bin which has poor statistics and a limited redshift baseline. Power-law fits to complete data are shown with solid lines. Comparison samples from similar redshift ranges are plotted with fainter symbols. Since the redshift bins are not identical these sometimes appear on more than one plot or with data from two bins in the original work on the same plot. Estimates for combined 24 μm data. Averages and standard deviations of β are given below the line. Fits are calculated for all galaxies and separately for 'blue' (templates Sab-Sdm and starburst, 3 ≤ z ≤ 11) and 'red' galaxies (both E templates, j2 ≤ 2). Reduced χ^2 are quoted if the number of points used in the fit is more than 2.

Table 2. Power-law fits to the specific star formation as a function of stellar mass as plotted in Figs 5–8. Modelled as sSFR = Y(M/10^11 M⊙)α in redshift ranges indicated. Combined 70 and 160 μm data. Averages and standard deviations of β are given below the line. Fits are calculated for all galaxies and separately for 'blue' (templates Sab-Sdm and starburst, 3 ≤ j2 ≤ 11) and 'red' galaxies (both E templates, j2 ≤ 2). Reduced χ^2 are quoted if the number of points used in the fit is more than 2.

<table>
<thead>
<tr>
<th>z_{min}</th>
<th>z_{max}</th>
<th>log_{10} Y/log(Gyr^{-1})</th>
<th>All galaxies</th>
<th>Blue galaxies</th>
<th>Red galaxies</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>β</td>
<td>β</td>
<td>β</td>
<td>β</td>
</tr>
<tr>
<td></td>
<td></td>
<td>χ^2/ν</td>
<td>χ^2/ν</td>
<td>χ^2/ν</td>
<td>χ^2/ν</td>
</tr>
</tbody>
</table>

| 0.0     | 0.2     | -1.41 ± 0.01              | -0.23 ± 0.02 | 2.28         | -1.08 ± 0.01 | 0.00 ± 0.02 | 2.26         | -1.91 ± 0.03 | -0.37 ± 0.06 | 2.73         |
| 0.2     | 0.3     | -1.28 ± 0.01              | -0.37 ± 0.03 | 3.48         | -0.93 ± 0.01 | 0.01 ± 0.01 | 3.58         | -1.81 ± 0.04 | -0.37 ± 0.08 | 1.10         |
| 0.3     | 0.4     | -1.19 ± 0.02              | -0.32 ± 0.04 | 3.91         | -0.96 ± 0.01 | -0.16 ± 0.03 | 3.99         | -1.67 ± 0.03 | -0.59 ± 0.14 | 0.50         |
| 0.4     | 0.5     | -0.99 ± 0.02              | -0.27 ± 0.05 | 0.71         | -0.84 ± 0.01 | -0.12 ± 0.03 | 4.12         | -1.29 ± 0.02 | -0.49 ± 0.05 | 2.28         |
| 0.5     | 0.6     | -0.91 ± 0.02              | -0.46 ± 0.05 | 4.65         | -0.75 ± 0.01 | -0.20 ± 0.04 | 1.63         | -1.28 ± 0.03 | -0.48 ± 0.11 | 5.11         |
| 0.6     | 0.8     | -0.78 ± 0.01              | -0.64 ± 0.06 | 1.66         | -0.61 ± 0.02 | -0.26 ± 0.04 | 0.45         | -1.23 ± 0.05 | -0.78 ± 0.21 | 2.78         |
| 0.8     | 1.0     | -0.47 ± 0.03              | -0.39 ± 0.07 | -0.37 ± 0.02 | -0.30 ± 0.05 | 5.33         | -1.04 ± 0.26 | -0.12 ± 0.50 |               |
| 1.0     | 1.25    |                         | -0.17 ± 0.04 | -0.32 ± 0.07 |               |               |               |               |               |
| 1.25    | 1.5     |                         | 0.09 ± 0.11  | -0.30 ± 0.20 |               |               |               |               |               |
| 1.5     | 2.0     |                         | 0.04 ± 0.16  | 0.17 ± 0.28  |               |               |               |               |               |

|         |         | -0.38 ± 0.14              | -0.15 ± 0.16 | -0.46 ± 0.21 |               |               |               |               |               |

immediately clear that there is a dramatic increase in FIR-to-optical ratio (or specific FIR luminosity) by a factor of >100 over the interval 0 ≤ z ≤ 2.4. This is seen at all masses apart from the lowest mass bin which has poor statistics and a limited redshift baseline. Again, we see the same trends in both the 70 and 160 μm data. This is an important corroboration as the FIR data are independent and the K-corrections will be different. We have fit this trend with a simple model

sSFR = X(1 + z)^a.
Figure 7. Specific FIR luminosity or sSFR as a function of stellar mass in redshift classes for ‘blue’ galaxies, i.e. those with SED types 3–11. Points are the weighted average over four fields (Elais-N1, Elais N2, Lockman and CDFS) and over 70 and 160 μm data with error bars are as for Figs 5 and 6. Incomplete points are unfilled. The parameters of the power-law fits to our data are tabulated in Table 2.

Figure 8. Specific FIR luminosity or sSFR as a function of stellar mass in redshift classes for ‘red’ galaxies, i.e. those with SED types 1–2. Points are the weighted average over four fields (Elais-N1, Elais N2, Lockman and CDFS) and over 70 and 160 μm data with error bars are as for Figs 5 and 6. Incomplete points are unfilled. The parameters of the power-law fits to our data are tabulated in Table 2.

The best fits are shown in Figs 9–11, and the parameters and goodness of fit are given in Table 3.

The simple power-law fit provides a good description of the data in most cases. As already seen in Section 4.2, the zero redshift specific FIR luminosity, i.e. the parameter X, declines with increasing stellar mass. We see no strong indication that α increases with increasing mass (in the range $10^{10.5} M_\odot < M < 10^{12}$), as would be expected in the ‘downsizing’ scenario.

We also compare with the observations from Zheng et al. (2007b). Their data show similar evolutionary behaviour at lower stellar masses. If we assume that the variations of evolutionary rate with stellar mass are statistical variations, then we can make a simpler model with the same α for all classes. We take the average of the α estimates in Table 3 for $M > 10^{10.5} M_\odot$. From this we deduce that the $L_{\text{FIR}}/M_*$ ratio varies as $(1 + z)^{4.4\pm0.3}$, with the error bar being the standard deviation of the measurements. The lowest mass bins are, however, inconsistent both with this mean evolutionary rate and the lower mass estimates from Zheng et al. (2007b).

We show the redshift trend for the SAMs in Fig. 9. The SAMs show sSFRs decreasing smoothly with cosmic time as the gas
Supplies are declining and the stellar masses are building up. The trend with redshift in the SAMs has a mean slope of $\alpha = 2.4$, which is considerably shallower than the observed data ($\alpha = 4.4 \pm 0.3$).

We do the same analysis for late/blue (Fig. 10) and early/red galaxies (Fig. 11) as before. It is striking that for the late-type galaxies the variation with stellar mass seen in Fig. 9 is considerably reduced and that there is negligible difference between galaxies with $M > 10^{10.5} M_\odot$. Assuming, therefore, that they are measuring the same relation, we average the fits in Table 3 to estimate $\log_{10}(\text{sSFR})/\text{Gyr}^{-1} = -1.36(\pm 0.20) + 3.36(\pm 0.16) \log_{10}(1 + z)$, where the error bars are errors in the mean calculated from the standard deviations given in Table 3.
log10(μcordance between our independent analysis at 70 and 160 signature of the AGN in the optical SED may be masked. The con-
to higher AGN contamination in more massive systems where the may bias us against star formation correlated with AGN activity, or to field. Excluding galaxies with signs of AGN in the optical SED in our error bars which take into account the variation from field variance is minimized by our large survey volume and is included to slightly shallower slopes of sSFR versus stellar mass. Sampling underestimate faint fluxes exposed in the simulations may bias us either of the basic trends we found. The possible bias to reduce redshift cells. The bias against very obscured objects would act to be weak and should only affect the lowest luminosity or highest luminosity the remaining selection effects are expected with redshift. Before we consider the implications of this it is worth drawing together some of the caveats. Having corrected for the optical incompleteness the remaining selection effects are expected to be weak and should only affect the lowest luminosity or highest redshift cells. The bias against very obscured objects would act to reduce either of the basic trends we found. The possible bias to underestimate faint fluxes exposed in the simulations may bias us to slightly shallower slopes of sSFR versus stellar mass. Sampling variance is minimized by our large survey volume and is included in our error bars which take into account the variation from field to field. Excluding galaxies with signs of AGN in the optical SED may bias us against star formation correlated with AGN activity, or to higher AGN contamination in more massive systems where the signature of the AGN in the optical SED may be masked. The concordance between our independent analysis at 70 and 160 μm also argues against any of these effects being significant. Our biggest remaining caveat is that we are strongly reliant on the accuracy of the photometric redshifts and resulting stellar masses from RR08 but we have mitigated against systematic errors in these by applying conservative constraints on the photometric redshifts and from our field-to-field comparison.

The specific FIR luminosity we measure includes energetic contributions from star formation, AGN and the ambient stellar radiation field which we relate to sSFR. Assuming these different contributions track each other with redshift then evolutionary trends will be unaffected.

With these caveats we consider that the trends we have observed in specific FIR luminosity mirror trends in sSFRs. The sSFR is dependent on the factors triggering star formation, the availability of gas supplies and the importance of feedback processes that regulate the star formation. The decline of sSFR with stellar mass (which has already been observed at other wavelengths) may be due to declining resources, i.e. more massive galaxies have locked more of their baryons into stars in the past. Feedback also plays a role, for

Table 3. Fits to sSFRs as function of z in stellar mass bins. Fit is to the function SSFR = X(1 + z)^α. Averages and standard deviations for α from data with M > 10^{10.5} M⊙ are shown below the line. Calculated for all galaxies and separately for ‘blue’ (templates Sab-Sdm and starburst, 3 ≤ z ≤ 11) and ‘red’ galaxies (both E templates, 1 ≤ z ≤ 2). Reduced χ^2 are quoted if the number of points used in the fit is more than 2. α for SAM model varies between 2.44 and 2.67 over same mass range.

<table>
<thead>
<tr>
<th>log10(M/4⊙)</th>
<th>log10(X/Gyr^{-1})</th>
<th>α</th>
<th>χ^2/ν</th>
<th>log10(X/Gyr^{-1})</th>
<th>α</th>
<th>χ^2/ν</th>
<th>log10(X/Gyr^{-1})</th>
<th>α</th>
<th>χ^2/ν</th>
</tr>
</thead>
<tbody>
<tr>
<td>10.0−10.3</td>
<td>-1.09 ± 0.24</td>
<td>-0.6 ± 3.1</td>
<td>-0.82 ± 0.19</td>
<td>-2.9 ± 2.2</td>
<td>-1.59 ± 0.29</td>
<td>1.9 ± 3.9</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>10.3−10.5</td>
<td>-1.38 ± 0.13</td>
<td>2.9 ± 1.2</td>
<td>0.59</td>
<td>-1.31 ± 0.10</td>
<td>3.4 ± 0.8</td>
<td>1.34</td>
<td>-1.85 ± 0.34</td>
<td>2.2 ± 4.7</td>
<td></td>
</tr>
<tr>
<td>10.5−10.8</td>
<td>-1.57 ± 0.09</td>
<td>4.6 ± 0.6</td>
<td>0.34</td>
<td>-1.27 ± 0.09</td>
<td>3.0 ± 0.6</td>
<td>1.03</td>
<td>-2.32 ± 0.11</td>
<td>8.5 ± 0.9</td>
<td>4.35</td>
</tr>
<tr>
<td>10.8−11.1</td>
<td>-1.64 ± 0.09</td>
<td>4.2 ± 0.6</td>
<td>0.33</td>
<td>-1.31 ± 0.08</td>
<td>3.1 ± 0.4</td>
<td>0.47</td>
<td>-2.42 ± 0.14</td>
<td>6.6 ± 0.9</td>
<td>0.58</td>
</tr>
<tr>
<td>11.0−11.4</td>
<td>-1.74 ± 0.11</td>
<td>4.1 ± 0.6</td>
<td>0.34</td>
<td>-1.38 ± 0.08</td>
<td>3.5 ± 0.4</td>
<td>0.26</td>
<td>-2.32 ± 0.12</td>
<td>4.9 ± 0.6</td>
<td>1.22</td>
</tr>
<tr>
<td>11.4−12.0</td>
<td>-1.95 ± 0.10</td>
<td>4.7 ± 0.4</td>
<td>1.15</td>
<td>-1.46 ± 0.13</td>
<td>3.7 ± 0.5</td>
<td>0.34</td>
<td>-2.13 ± 0.18</td>
<td>2.7 ± 0.8</td>
<td>1.18</td>
</tr>
<tr>
<td>4.4 ± 0.3</td>
<td>-1.36 ± 0.41</td>
<td>3.4 ± 0.3</td>
<td>5.7 ± 2.5</td>
<td></td>
<td></td>
<td></td>
<td></td>
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</tbody>
</table>

Figure 11. Specific FIR luminosity as a function of redshift in stellar mass classes for ‘red’ galaxies, i.e. those with SED types 1–2. Filled circles are the average of our estimates from the 70 and 160 μm data which are the weighted average over four fields (Elais-N1, Elais N2, Lockman and CDFS). Thick vertical error bars come from the field-to-field scatter and thin error bars with hats from the variation between 70 and 160 μm estimates. Solid lines are our power-law trends with parameters given in Table 3. The dashed line shows the inverse Hubble time, galaxies above this line are ‘bursting’ producing stars at a higher rate than their historical average.

5 DISCUSSION

Our stacking analysis shows that the specific FIR luminosity declines as a function of increasing stellar mass and evolves strongly with redshift. Before we consider the implications of this it is worth drawing together some of the caveats. Having corrected for the optical incompleteness the remaining selection effects are expected to be weak and should only affect the lowest luminosity or highest redshift cells. The bias against very obscured objects would act to reduce either of the basic trends we found. The possible bias to underestimate faint fluxes exposed in the simulations may bias us to slightly shallower slopes of sSFR versus stellar mass. Sampling variance is minimized by our large survey volume and is included in our error bars which take into account the variation from field to field. Excluding galaxies with signs of AGN in the optical SED may bias us against star formation correlated with AGN activity, or to higher AGN contamination in more massive systems where the signature of the AGN in the optical SED may be masked. The concordance between our independent analysis at 70 and 160 μm also
example AGN feedback in the more massive galaxies may suppress star formation (e.g. Bower et al. 2006; Croton et al. 2006). However, it seems that the abrupt changes in specific star formation resulting from some models of AGN feedback (i.e. those of De Lucia & Blaizot 2007) are not supported. So either the impact of AGN feedback on specific star formation is marginal or the AGN feedback is not as differentially dependent on stellar mass as in these models.

The evolutionary trend is both remarkably consistent across different stellar masses in the range $10.5 < \log_{10} M_\star / M_\odot < 12$, and stronger than the models. This discrepancy between the models and data could arise from an evolution in the feedback prescription which would need to be less restrictive at higher redshift. Alternatively the triggering mechanisms (e.g. environmental effects) or decline in gas supplies in the models may need adjusting. It is worth noting that enhanced evolution of the SFRs enhances the change in specific star formation both through the star formation directly but also through the more rapid stellar buildup.

It should also be noted that the parameters in the models, including the ones controlling the AGN feedback strength, were only adjusted to reproduce galaxy properties at redshift zero and any resemblance at all to observed data at high redshift might be viewed as a partial success.

The presence or absence of a break in the sSFR as a function of stellar mass and the evolution of this with redshift appears to place significant constraints on feedback models. Our large sample means we have small statistical errors and so present results in finer redshift and mass bins. This means our results are less subject to changes across a bin. Our work extends previous work to lower redshift and mass bins. This means our results are less subject to sampling variance problems (so are not differentially dependent on stellar mass as in these models).

(vii) For early-type galaxies, the average evolution in this mass range is stronger ($\alpha \sim 5.7$) but decreases to higher mass.

(viii) For late-type galaxies, the trend is weaker but apparently independent of stellar mass, giving a mean rate $\alpha = 3.36 \pm 0.16$.

REFERENCES


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Optical data used for photometric redshifts have come from the Isaac Newton Telescope and Palomar Observatory.

We have benefitted from using TOPCAT, http://www.star.bristol.ac.uk/~mbt/topcat