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1 INTRODUCTION

Weak gravitational lensing refers to the subtle distortions in the images of distant galaxies by intervening mass along the line of sight. The measurement of lensing around foreground (lens) galaxies is referred to as galaxy–galaxy lensing (Tyson, Valdes & Mills 1984; Brainerd, Blandford & Smail 1996; dell’Antonio & Tyson 1996). Background (source) galaxies are binned in annuli on the sky centred on lens galaxies; the shapes of the background galaxies are projected along the tangential direction and averaged over a population of lens galaxies. The measurement as a function of angular separation can be converted into an estimate of the projected mass profile of the dark matter haloes where the galaxies reside.

Galaxy–galaxy lensing measurements have been used to infer the mass distribution within the haloes of massive galaxies, the relation of mass to light, the shapes of the haloes, and the large-scale galaxy–mass cross-correlation (Sheldon et al. 2004; Mandelbaum et al. 2006; Mandelbaum, Seljak & Hirata 2008; Cacciato et al. 2009). The measurements have many applications, ranging from fitting Navarro–Frenk–White (NFW) halo mass profiles (Navarro, Frenk & White 1997) to estimating the large-scale bias of galaxies and obtaining cosmological constraints (Cacciato et al. 2009; Mandelbaum et al. 2013; More et al. 2015). Recent surveys such as Canada–France–Hawaii Telescope Lensing Survey (CFHTLenS; Heymans et al. 2012; Erben et al. 2013) have presented measurements on galaxy–galaxy lensing (Gillis et al. 2013; Velander et al. 2014; Hudson et al. 2015). Similarly, measurements from the Kilo-Degree Survey (KiDS; de Jong et al. 2013; Kuijken et al. 2015) have also studied the galaxy–mass connection using galaxy–galaxy lensing (Sifón et al. 2015; Viola et al. 2015; van Uitert et al. 2016). The galaxy–mass connection has also been studied at high redshift by Leauthaud et al. (2012).

In this paper, we measure galaxy–galaxy lensing from Dark Energy Survey (DES) pre-survey Science Verification (SV) data. DES is an ongoing wide-field multiband imaging survey that will cover nearly 5000 deg$^2$ of the southern sky over 5 yr. With this pre-survey SV data, our goals are to establish the feasibility of measuring galaxy–galaxy lensing with DES, test our measurement pipelines, and make an estimate of the halo properties for a selected galaxy sample. The detailed tests presented serve as a necessary foundation for other work relying on galaxy–galaxy lensing measurements with these data. In particular, Kwan et al. (in preparation) obtain constraints on cosmological parameters using the combination of galaxy–galaxy lensing and galaxy clustering information with the same data used in this work. Baxter et al. (2016) present complementary cosmological and systematic constraints using the combination of galaxy–galaxy lensing and cosmic microwave background (CMB) lensing. Frat et al. (2016) measure galaxy–galaxy lensing around a magnitude-limited sample of DES-SV galaxies in order to measure their large-scale bias. Finally, tangential shear measurements of underdensities such as troughs (Gruen et al. 2016) and voids (Sánchez et al. 2017) also benefit from the tests in this work.

The plan of the paper is as follows. Section 2 summarizes the basic theory of galaxy–mass correlations and our halo occupation distribution (HOD) model. Section 3 describes our data: including basic details of DES, descriptions of the lens galaxy sample, pipelines for source galaxy shape measurements, and the photometric redshift estimation of lens and source galaxies. Our estimators and measurement methodology are presented in Section 4. Results of null tests that establish the suitability of the shear and photo-z catalogues for galaxy–galaxy lensing are presented in Section 5.

Our measurement results and HOD model fits are in Section 6, as well as discussion of related results in the literature. We conclude in Section 7.

2 WEAK-LENSING THEORY AND THE HALO MODEL

Galaxy–galaxy lensing involves the distortion of background galaxy images in the presence of foreground dark matter haloes, which are occupied by the lens galaxies. This distortion makes the background galaxy image stretch tangentially to the line joining the background and foreground galaxies. The magnitude of this tangential shear, $\gamma_t(\theta)$, and of the related excess surface density, $\Delta \Sigma(R)$, provides a means of learning about the local dark matter profile and galaxy environment.

We relate the properties of lens galaxies to the underlying dark matter distribution through HOD modelling (Zheng et al. 2005; Zehavi et al. 2011). The HOD model assigns each dark matter halo a probability of hosting $N$ galaxies, $P(N|M_h)$, that is dependent on the halo mass, $M_h$. The galaxy population is divided into centrals, which are generally luminous galaxies that are located at or near the centre of the halo, and satellites, less luminous galaxies which populate the outskirts of the halo. Each halo is allowed only one central but can have multiple satellites. We follow the HOD parametrization of Zehavi et al. (2011): assuming a log-normal mass–luminosity distribution for central galaxies and a power-law distribution for satellite galaxies. The expectation value for the number of galaxies for a luminosity thresholded sample (with absolute r-band magnitude $M_r < M'_r$) is parametrized as

$$\langle N(M_h|M'_r) \rangle = \langle N_c(M_h|M'_r) \rangle \left(1 + \langle N_s(M_h|M'_r) \rangle \right)$$

$$= \frac{1}{2} \left[ \frac{1 + \text{erf} \left( \frac{\log M_h - \log M_{\text{min}}}{\sigma_{\log M}} \right)}{1 + \text{erf} \left( \frac{\log M_{\text{min}} - \log M_{\text{min}}}{\sigma_{\log M}} \right) + \frac{M_h}{M'_r}} \right]$$

with model parameters $M_{\text{min}}$, $M'_r$, $\sigma_{\log M}$, $\alpha$, $f_{\text{cen}}$. For a DES simulation-based study using a similar HOD model, see Park et al. (2016). For simplicity we set the satellite cut-off scale of Zheng et al. (2005) to zero, as it is not constrained by our data.

The central galaxy occupation is described by a softened step function with two parameters: (i) a transition mass scale $M_{\text{tran}}$, which is the halo mass at which the median central galaxy luminosity corresponds to the luminosity threshold, and (ii) a softening parameter $\sigma_{\log M}$ related to the scatter between galaxy luminosity and halo mass. The normalization of the satellite occupation function is $M_1$ and $\alpha$ is the high-mass slope of the satellite occupation function. Finally, we introduce an additional parameter, $f_{\text{cen}}$, the fraction of occupied haloes, which allows us to relax the assumption that every halo above a certain mass contains a central galaxy. Note that we have restricted ourselves to a simplified model in which $f_{\text{cen}}$ is mass independent to reduce the dimensionality of our parameter space. This parametrization (with $f_{\text{cen}} = 1$) is able to reproduce the clustering of Canada–France–Hawaii Telescope Legacy Survey (CFHTLS) and Sloan Digital Sky Survey (SDSS) galaxies over a large range of redshifts and luminosity thresholds (Zheng et al. 2005; Zehavi et al. 2011). redMaGiC galaxies are not quite complete to a luminosity threshold: they were selected using a cut in colour space and this prompted the inclusion of $f_{\text{cen}}$ as an additional free parameter. However, to obtain strong constraints on $f_{\text{cen}}$, we would need to use the observed number density of galaxies as an additional constraint. The priors used for each parameter are...
summarized in Table 1. We choose priors based on earlier work with red galaxies: $f_{\text{cen}}$ from redMaPPer (Rykoff et al. 2014, 2016); $0.01 < \sigma_{\text{log}M} < 0.5$ and $0.4 < \log M_1 - \log M_{\text{min}} < 1.6$ from Brown et al. (2008); $\alpha$ from White et al. (2011) and Parejko et al. (2013). In addition, we check that widening the priors for all parameters does not affect our main results in Section 6.2.

Since the above prior choices are based on galaxy samples different from the DES redMaPPer sample, we briefly discuss their applicability here. Our fundamental assumption in adopting priors is that the principal impact of the galaxy selection is to set the mass scale $M_{\text{min}}$ required to host a galaxy of the chosen minimum luminosity. Thus, $M_{\text{min}}$ is very clearly sample dependent. The remaining parameters, however, we expect to be roughly comparable for different samples. For instance, the scatter $\sigma_{\text{log}M}$ ultimately reflects the scatter in central galaxy luminosity at fixed mass, so we expect $\sigma_{\text{log}M}$ to be comparable for most galaxy samples. Likewise, the ratio $M_1/M_{\text{min}}$ is likely to be set by the mass $M_1$ required for a halo to host a substructure of mass $M_{\text{min}}$, leading to the expectation $M_1/M_{\text{min}}$ being roughly comparable for different luminosity or stellar mass thresholded samples. Finally, the prior on the slope of the HOD is rather generous, 0.6–1.4, roughly a 40 percent window around the naive expectation $\alpha = 1$ corresponding to a constant galaxy/mass ratio. Again, the critical point is that our principal results in Section 6.2 are insensitive to the details of these priors.

The HOD model allows us to predict, on average, the number of galaxies contained within each halo of a given mass. Together with the halo mass function, which tells us how many haloes of each mass bin to expect within a given volume, and the halo model (Croft & Sheth 2002), we can predict the expected clustering of these galaxies and their dark matter haloes. On large scales, correlations between dark matter and galaxies in different haloes dominate and can be approximated by the two-halo matter–galaxy cross-power spectrum as follows:

$$ P_{\text{gm}}^\text{ih} (k, M) = \frac{1}{\rho_{\text{crit}}(M)} \int \frac{dM_1}{dM_{\text{h}}} b_h(M_1) N(M_{\text{h}}(M_1)|M) \langle N_\text{cen} (M_{\text{h}}(M_1)|M) \rangle $$

where $N_\text{cen}$ is the Fourier transform of the halo density profile of $\Phi_{\text{h}}(k, M)$, and $\Phi_{\text{cen}}$ is supplied by the HOD model as the Fourier transform of the spatial distribution of satellite galaxies in the halo. We assume that the dark matter within a halo is distributed according to an NFW profile (Navarro et al. 1997), with a Bhattacharyya et al. (2013) concentration–mass relation, $c(M) = 9 \times r_{\text{200}}(M) - 0.25 \times D(z)^{1.15}$, where $c(M)$ is the square root of the variance in a filter with mass $M$ and $D(z)$ is the growth factor at redshift $z$. Note that we do not include subhalo one-halo contributions from satellite galaxies in the model. Given our conservative small-scale cut-off (see Appendix A1) of 30 arcsec and our statistical errors (see Fig. 7), such a contribution is unnecessary.

Following Hayashi & White (2008) and Zu et al. (2014), we transition between these two regimes by taking the larger contribution of these two terms, such that

$$ \xi_{\text{gm}}(r, z) = \left\{ \begin{array}{ll} \xi_{\text{ih}}^\text{rh}(r, z) & \text{for } \xi_{\text{ih}}^\text{rh}(r, z) \geq \xi_{\text{ih}}^\text{2h}(r, z), \\
\xi_{\text{ih}}^\text{2h}(r, z) & \text{otherwise,} \end{array} \right. $$

The tangential shear is related to the excess surface density, $\Sigma$, as

$$ W_s(z, z') = \frac{\rho_{\text{crit}}(z)}{(1 + z) \Sigma_{\text{crit}}(z, z')} $$

and the critical surface density $\Sigma_{\text{crit}}(z, z')$ of a flat universe is given by

$$ \Sigma_{\text{crit}}^2(z, z') = \frac{4\pi G}{1 + z} \frac{\chi(z)}{\chi(z')} $$

where $\chi(z)$ is the comoving distance to redshift $z$, the lensing window function $W_s(z, z')$ is

$$ W_s(z, z') = \frac{\rho_{\text{crit}}(z)}{(1 + z) \Sigma_{\text{crit}}(z, z')} $$

and $\Sigma_{\text{crit}}(z, z)$ of a flat universe is given by

$$ \Sigma_{\text{crit}}^2(z, z') = \frac{4\pi G}{1 + z} \frac{\chi(z)}{\chi(z')} $$

We then transform $C_{\text{gx}}(l)$ to real space and obtain the tangential shear $\gamma_t(\theta)$:

$$ \gamma_t(\theta) = \int \frac{dl}{2\pi} C_{\text{gx}}(l) J_2(l\theta) $$

The tangential shear is related to the excess surface density, $\Delta \Sigma$, as

$$ \Delta \Sigma(R|z) = \Sigma(< R) - \Sigma(R) $$

$$ = \Sigma_{\text{cen}}(z, z) \gamma_t(R|z, z) $$

where $\Sigma(R)$ is the surface mass density at the transverse separation $R$ from the centre of the halo and $\Sigma(< R)$ its mean within $R$. Finally, we integrate over the redshift distribution of lens galaxies, $n(z)$, to obtain

$$ \langle \Delta \Sigma(R) \rangle = \frac{1}{n} \int dz \, n(z) \Delta \Sigma(R|z) $$

$\Delta \Sigma$ is a physical property of the lens and so does not depend on the source galaxies: this is clear from equation (11) in which $\Delta \Sigma$ is a sum of central and satellite terms:
can be determined completely from the projected mass density $\Sigma$. This independence from source redshifts is less obvious in equation (12), but note the $\Sigma_{\text{crit}}(z, z_s)$ factor cancels with the same factor in equation (8).

Note that throughout this paper we define the halo mass $M_h$ as the mass within a sphere enclosing a mean density that is 200 times the mean mass density of the universe. (This mass is often labelled $M_{200m}$ in the literature.) For modelling, we fix cosmological parameters to $\Omega_m = 0.31$, $h = 0.67$, $\Omega_{\Lambda} = 0.048$, $n_s = 0.96$, and $w = -1$, all of which are consistent with the results of Kwan et al. (in preparation). We use physical length units throughout the paper.

3 DATA

The DES is an ongoing wide-field multiband imaging survey that will cover nearly 5000 deg$^2$ of the southern sky over 5 yr. The Dark Energy Camera (DECam; Flaugher et al. 2015) holds sixty-two 2048 $\times$ 4096 science CCDs, four 2048 $\times$ 2048 guider CCDs, and eight 2048 $\times$ 2048 focus and alignment chips, for a total of 570 megapixels covering a roughly hexagonal footprint. Five filters are used during normal survey operations, $g$, $r$, $i$, $z$, $Y$. The main survey will cover about 5000 deg$^2$ in the South Galactic Cap region, with approximately 10 visits per field in the $r$, $i$, and $z$-bands, for a 10$\sigma$ limiting magnitude of about $\sim 24.1$ in the $i$-band.

In this paper, we use the largest contiguous region of Science Verification (SV) data which covers 139 deg$^2$ with similar depth and filter coverage as the main DES survey. The SV data were taken during the period of 2012 November–2013 February before the official start of the science survey. All data used in this study are based on the DES SVA1 Gold catalogue1 and several extensions to it. The main catalogue is a product of the DES Data Management (DESDM) pipeline version ‘SVA1’. The DESDM pipeline (Ngeow et al. 2006; Sevilla et al. 2011; Desai et al. 2012; Mohr et al. 2012; Guenel et al., in preparation) begins with initial image processing on single-exposure images and astrometry measurements from the software package SCAMP (Bertin 2006). The single-exposure images were then stacked to produce co-add images using the software package SWARP (Bertin et al. 2002). Basic object detection, point spread function (PSF) modelling, star–galaxy classification, and photometry were done on the individual images as well as the co-add images using software packages SexTRACTOR (Bertin & Arnouts 1996) and PSFEx (Bertin 2011).

For weak lensing, we use the co-add images only for object detection, deblending, fluxes (for use in photo-$z$ measurements), and for the detailed informational flags which are important for determining a good set of galaxies to use for shear measurement. For the purposes of estimating galaxy shears, we instead perform object measurement on all available single-epoch images in which an object was observed, using multi-epoch fitting techniques (Jarvis et al. 2016).

3.1 Lens sample: redMaGiC

The DES SV red-sequence Matched-filter Galaxy Catalog (redMaGiC; Rozo et al. 2016) is a catalogue of photometrically selected luminous red galaxies (LRGs). Specifically, redMaGiC uses the redMaPPer-calibrated model for the colour of red-sequence galaxies as a function of magnitude and redshift (Rykoff et al. 2014, 2016). This model is used to find the best-fitting photometric redshift for all galaxies irrespective of type, and the $\chi^2$ goodness-of-fit of the model is computed. For each redshift slice, all galaxies fainter than some minimum luminosity threshold $L_{\text{min}}$ are rejected. In addition, redMaGiC applies a $\chi^2$ cut $\chi^2 \leq \chi_{\text{max}}^2$, where the cut $\chi_{\text{max}}^2$ as a function of redshift is chosen to ensure that the resulting galaxy sample has a constant space density $\bar{n}$. In this work, we use the sample with $\bar{n} = 10^{-3} h^3$ Mpc$^{-3}$; note that the redMaPPer algorithm assumes a flat cosmology with $\Omega_m = 0.3$ in order to calculate the comoving density and luminosity distances. We expect the result from our analysis to be only marginally sensitive to the cosmological parameters assumed.

The luminosity cut is $L \geq 0.5 L_\ast(z)$, where the value of $L_\ast(z)$ at $z = 0.1$ is set to match the redMaPPer definition for SDSS. The redshift evolution for $L_\ast(z)$ is that predicted using a simple passive evolution starburst model at $z = 3$. We utilize the redMaGiC sample because of the excellent photometric redshifts of the redMaGiC galaxy catalogue: the redMaGiC photometric redshifts are nearly unbiased, with a median bias $\Delta z_{\text{pec}} = z_{\text{photo}} - z_{\text{pec}}$ of 0.005, scatter $\sigma_{\Delta z}/(1 + z) = 0.017$, and a 1σ redshift outlier rate of 1.4 percent. These photometric redshifts are used to split the redMaGiC galaxies into different lens redshift bins in this study. We refer the reader to Rozo et al. (2016) for further details of this catalogue.

We use three redshift bins of lens galaxies, $0.2 < z < 0.35$, $0.35 < z < 0.5$, and $0.5 < z < 0.8$. To plot the redshift distribution $N(z)$ of each bin in Fig. 1, we sum individual Gaussian redshift distributions for each lens, centred at the redMaGiC photo-$z$ estimate and with a width given by the redmagic photo-$z$ error. Note that using a Gaussian for each lens neglects any outlier component: based on Rozo et al. (2016) (especially figs 10 and 11) the fraction of such outliers, and thus their effect on our modelling of the lens redshift distribution, is small. Since the lens photometric redshifts have much higher precision than source redshifts, we do not include a lens photo-$z$ systematic uncertainty contribution. However, an estimate of the true redshift distribution of lenses (as in Fig. 1) is taken into account in our modelling. The number of lenses per redshift bin is $\sim 9000$, 19 000, and 67 000, respectively.

Figure 1. Top panel: redshift distributions of redMaGiC lens galaxies used in this work. For lenses, we show the stacked $N(z)$ from individual Gaussian distributions for each source. See text for details. Bottom panel: the same, but for our weak lensing source samples. For sources, we show the stacked $N(z)$ from individual SkyNet $p(z)$ distributions.
3.2 Source sample

Based on the SVA1 data, two shear catalogues were produced and tested extensively in Jarvis et al. (2016) – the **ngmix**\(^3\) (Sheldon 2014) and the **im3shape**\(^4\) (Zuntz et al. 2015) catalogues. The main results in our paper are based on ngmix, but we also cross-check with the im3shape catalogue to demonstrate the robustness of our results.

The im3shape implementation in this work estimates shears by jointly fitting a parametrized galaxy model to all of the different single-exposure \(r\)-band images, finding the maximum likelihood solution. The PSFEX software is used to fit pixelized models of the PSF, and those models are then interpolated to the galaxy positions. Corrections to bias in the shear measurement associated with noise (Kacprzak et al. 2012; Refregier et al. 2012) are applied. The im3shape catalogue has a raw number density of about 4.2 galaxies per square arcminute.

**ngmix** uses sums of Gaussians to approximate common galaxy profiles: exponential disc, De Vaucouleurs’ profile (de Vaucouleurs 1948), and Sérsic profile (Sérsic 1963). Any number of Gaussians can be fit, either completely free or constrained to be co-centric and co-elliptical. For the DES SV galaxy images, we used the exponential disc model. For the PSF fitting, an expectation–maximization (Dempster, Laird & Rubin 1977) approach is used to model the PSF as a sum of three free Gaussians. Shear estimation was carried out using images in \(r\), \(i\), \(z\) bands, which enabled a larger raw galaxy number density (6.9 galaxies per square arcminute).

Photometric redshifts for source galaxies in DES-SV were studied in detail in Bonnett et al. (2016), using four different photometric redshift codes (**annz2**, **bpz**, **skynet**, and **tpz**). The details and capabilities of these codes on early DES data were already presented in Sánchez et al. (2014), where they showed the best performance among a more extensive set of codes. For the results in this paper, we use the photometric redshifts by **skynet** (Graff et al. 2014; Bonnett 2015), which is a neural network algorithm that was run on DES bands **griz** and produced a probability density function (PDF) for the redshift of each galaxy in the DES-SV shape catalogues. In addition to the source PDFs, we make use of a **skynet** point estimate of source photometric redshift given by the mean of the PDF. Note that we only use **skynet** redshifts for the sources, as the redMaGiC algorithm produces a separate photo-z estimate for each lens.

Our source redshift distributions are shown in Fig. 1. Since our galaxy–galaxy lensing tests will provide validation for the cosmology results of Kwan et al. (in preparation), that work uses these same redshift bins. These bins are also consistent with those used in the DES SV results for cosmic shear (Becker et al. 2016; The Dark Energy Survey Collaboration 2015). Note however that the \(\Delta\Sigma\) estimator, according to the definition in equation (18), uses every background source behind each individual lens.

3.3 Mock catalogues

In Appendix B, we make use of the ‘Buzzard v1.0c’ version DES mocks to validate measurement covariances. Three \(\Lambda\)-body simulations, a 1050 Mpc \(h^{-1}\) box with 1400\(^2\) particles, a 2600 Mpc \(h^{-1}\) box with 2048\(^2\) particles, and a 4000 Mpc \(h^{-1}\) box with 2048\(^2\) particles, are combined along the line-of-sight to produce a full light cone out to DES depths. These boxes were run with **lgadget2** (Springel 2005) and used **2lptic** initial conditions (Crocce, Pueblas & Scoccimarro 2006) with linear power spectra generated with **Camb** (Lewis & Bridle 2002). **Rockstar** (Behroozi, Wechsler & Wu 2013) was used to find haloes in the \(N\)-body volumes. The **Addgals** algorithm (Busha et al. 2013) is used to populate galaxies as a function of luminosity and colour into dark matter only \(N\)-body simulations. **Addgals** uses the relationship between local dark matter density and galaxy luminosity, determined by applying **sham** (Conroy, Wechsler & Kravtsov 2006; Reddick et al. 2013) on a high-resolution tun- simulating simulation, to populate galaxies directly on to particles in the low-resolution simulations. Each galaxy is then assigned a colour by using the colour–density relationship measured in the SDSS (Aihara et al. 2011) and evolved to match higher redshift observations. For our mock lens sample, the same redMaGiC selection (Rozo et al. 2016) was run on the mock galaxies as on the data. For the mock shears, galaxies are assigned sizes and shape noise using **Suprime-Cam** observations processed to match typical DES observing conditions (Szepietowski et al. 2014). Finally, weak lensing shear for each source galaxy was computed using the multiple-plane lensing code **CalcLenses** (Becker 2013).

4 MEASUREMENT METHODOLOGY

The most basic galaxy–galaxy lensing observable is the tangential shear of background source galaxies relative to the line joining the lens and source. For a given lens–source pair \(j\), this is given by

\[
\gamma_{t,j} = -\gamma_{1,j} \cos(2\phi_j) - \gamma_{2,j} \sin(2\phi_j),
\]

where \(\gamma_{1,j}\) and \(\gamma_{2,j}\) are the two components of shear measured with respect to a Cartesian coordinate system centred on the lens, and \(\phi_j\) is the position angle of the source galaxy with respect to the horizontal axis of the Cartesian coordinate system. However, the intrinsic ellipticity of individual source galaxies is much larger than the weak lensing shear, so it is necessary to average over many such lens–source pairs. For our measurements and null tests, we will compute the average in angular bins \(\theta\) so that

\[
\langle \gamma_{t,\theta} \rangle = \frac{\sum_j w_j \gamma_{t,j}}{\sum_j w_j},
\]

where

\[
w_j = \frac{1}{\sigma_{\text{shape}}^2 + \sigma_{m,j}^2},
\]

where \(\sigma_{\text{shape}}\) is the intrinsic shape noise for each source galaxy, and \(\sigma_{m,j}\) is the measurement error. (This weight is the column labelled \(w\) in the shear catalogues described by Jarvis et al. 2016.) We use **TreeCorr**\(^4\) (Jarvis, Bernstein & Jain 2004) to compute all galaxy–galaxy lensing measurements.

One advantage of this galaxy–shear cross-correlation over shear–shear correlations is that additive shear systematics (with constant \(\gamma_1\) or \(\gamma_2\)) average to zero in the tangential coordinate system. However, this cancellation takes place only when sources are distributed isotropically around the lens, an assumption that is not accurate near the survey edge or in heavily masked regions. To remove additive systematics robustly, we also measure the tangential shear around random points: such points have no net lensing signal, yet they sample the survey edge and masked regions in the same way as the lenses. Our full estimator of tangential shear can then be written as

\[
\langle \gamma_t(\theta) \rangle = \langle \gamma_{t,\theta} \rangle = \langle \gamma_{t,\theta}^{\text{random}} \rangle.
\]
This measurement is directly comparable to the model prediction in equation (10).

We will also find it useful to use another estimator that simplifies the dependence of the lensing signal on the source redshift. This will be especially helpful in carrying out null tests that involve splitting the source galaxy sample into two or more samples, then checking consistency between the measured lensing signal of each (see Sections 5.3–5.5). This observable is estimated from the measured shapes of background galaxies as

$$\Delta \Sigma^\text{ens}_i(R;z_l) = \sum_j \left[ w_j y_{ij}(R)/\Sigma^\text{ens}_{ij}(z_l,z_s) \right],$$

where the summation $\sum_j$ runs over all the background galaxies in the radial bin $R$, around all the lens galaxy positions, and the weight for the $j$th galaxy is given by

$$w_j = w_j/\Sigma^\text{ens}_{ij}(z_l,z_s).$$

Note that instead of $\theta$, we have binned source galaxies according to the radial distance $R$ in the region around each lens galaxy. The weighting factor $\Sigma^\text{ens}_{ij}(z_l,z_s)$ is computed as a function of lens and source redshifts for the assumed cosmology as

$$\Sigma^\text{ens}_{ij}(z_l,z_s) = \frac{e^2}{4\pi G} \frac{D_A(z_s)}{D_A(z_l) D_A(z_l,z_s)},$$

where $\Sigma^\text{ens}_{ij}(z_l,z_s) = 0$ for $z_s < z_l$ and $D_A$ is the angular diameter distance. We assume a flat cosmology with $\Omega_m = 0.3$ when measuring $\Delta \Sigma$, although note that the results are not very sensitive to this value: the difference is well under 1 per cent when using $\Omega_m = 0.31$ (as in Section 6.2). Just as with the raw tangential shear, our final estimator involves subtracting the contribution around random points,

$$\Delta \Sigma_i(R) = \Delta \Sigma^\text{ens}_i(R) - \Delta \Sigma^\text{random}_i(R).$$

We use 10 times as many random points as lenses so that noise from the random point subtraction is negligible. We assign each random point a redshift drawn from the distribution of lens redshifts. The measurement in equation (21) is directly comparable to the model prediction in equation (13). Note that in equations (18)–(21) we use a point estimate of photometric redshift for each source (mean of the SKYNET p(z), see Section 3.2). However, we checked that the method of integrating over the full distribution of source redshifts (Nakajima et al. 2012; Sheldon et al. 2012; Mandelbaum et al. 2013) gives consistent results for both our central values and jackknife error bars.

We use a minimum fit scale $\sim 0.5$ arcmin based on deblending constraints (see Appendix A1). The maximum scale we use is 70 arcmin, comparable to the size of our jackknife regions. Using numerical simulations, we have verified that the resulting jackknife covariance matrix estimate is accurate up to this scale (see Appendix B for details), above which the jackknife overestimates the errors from independent simulations. Therefore, including larger scales in the fits would still be conservative but there is very marginal gain in S/N, so we elect to stop at 70 arcmin.

While our photometric redshifts remove or downweight source galaxies near the lens redshift, some fraction of the sources will still be physically correlated with the lenses (e.g. Sheldon et al. 2004; Mandelbaum et al. 2006). This effect, corrected by applying ‘boost factors’, is most problematic near the centre of massive haloes where correlations are strongest. Given our relatively high minimum fit scale of 0.5 arcmin and small halo mass (compared to clusters, see Section 6.2), boost factor corrections are negligible (< 1 per cent) for our sample.

To estimate statistical errors, we divide the survey area into $N = 152$ spatial jackknife regions based on HEALPix5 (Górski et al. 2005), each slightly smaller than 1 deg$^2$. We perform the measurement multiple times with each region omitted in turn. The covariance of the measurement (Norberg et al. 2009) is given by

$$C_{ij}^\text{stat} = \frac{(N-1)}{N} \sum_{k=1}^N \left[ (\Delta \Sigma_i)^k - \bar{\Delta \Sigma}_i \right] \left[ (\Delta \Sigma_j)^k - \bar{\Delta \Sigma}_j \right],$$

where $N$ is the number of jackknife regions, the mean value is

$$\bar{\Delta \Sigma}_i = \frac{1}{N} \sum_{k=1}^N (\Delta \Sigma_i)^k,$$

and $(\Delta \Sigma_i)^k$ denotes the measurement from the $k$th realization and the $i$th spatial bin. Validation of this jackknife method using covariances from independent simulations is presented in Appendix B. Finally, we apply the correction factor of Hartlap, Simon & Schneider (2007), $N - 1_{\text{Njack}}$ to our inverse covariances when performing fits. This factor is intended to correct for noise in the covariance matrix, but with $N = 152$ and a number of bins $N_{\text{bins}} = 13$, this factor causes a very small change to our best-fitting model and error bars shown in Section 6.

### 5 DATA TESTS

We next perform a series of null tests used to check for and quantify the size of systematic uncertainties in our measurement due to biases in the shear and photometric redshift catalogues. In order to quantify the comparison of the data tests in this section with the null hypothesis, we compute the null $\chi^2$ for each of them in the following way:

$$\chi^2_{\text{null}} = \sum_{i,j} y^T (C^\text{stat})^{-1} y,$$

where $y_i$ corresponds to $y_{ij}$, or $\Delta \Sigma_i$, and $C_{ij}^\text{stat}$ is the corresponding covariance matrix. A list of the null $\chi^2$ value for each of the tests can be found in Table 2. While $\chi^2$ is a helpful statistical test, it is possible that two tests, each with the same $\chi^2$ values, could indicate different levels of systematic error. An extreme example is the case where every data point is positive for one test, whereas half the points are positive and half are negative (with the same amplitude) for the second test. Thus, for each test we also quote the result of a single parameter, constant fit to the data (including the full jackknife covariance). Since we perform many tests, some fraction of them are expected to differ from zero simply by chance. For example, even in the absence of systematics, one out of three tests will differ from zero by more than 1σ, and one out of 25 will differ by more than 2σ. Our criteria for declaring a test as ‘passed’ is that the constant fit should be within 2σ of zero, but note that using 1σ instead does not change the status of any tests.

In this section, we present tests that are unique to galaxy–galaxy lensing. Other tests of the shear catalogue, mostly focused on validation of cosmic shear results, have been presented in Jarvis et al. (2016) and Becker et al. (2016). For the tests that were already studied in prior DES SV work, we simply summarize the implications for our galaxy–galaxy lensing measurements in Appendix A. These tests include deblending and sky subtraction (A1), multiplicative shear bias (A2), and stellar contamination and shear around stars (A3). For most tests in this section, we show only the result with

5 http://healpix.sf.net
we show the result, multiplied by a \( \times 10^{-3} \) factor of 100. It is consistent with zero, and furthermore given the small upper bounds on the leakage, even these small fluctuations about zero are much smaller than our measured lensing signal (see Section 6.1).

While our estimator of galaxy–galaxy lensing in equation (21) involves subtracting the signal around random points that trace the same survey geometry, it is nonetheless useful to confirm that this

\[ \chi^2 \] for data and other tests and resulting systematic uncertainties.

<table>
<thead>
<tr>
<th>Test</th>
<th>Lens redshift</th>
<th>( \chi^2/\text{ndf} )</th>
<th>Systematic uncertainty</th>
<th>Passed</th>
<th>( \chi^2/\text{ndf} )</th>
<th>Systematic uncertainty</th>
<th>Passed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cross-component</td>
<td>Medium</td>
<td>8.3/13</td>
<td>((6.7 \pm 5.1) \times 10^{-5}) ✓</td>
<td>10.9/13</td>
<td>((6.0 \pm 7.8) \times 10^{-5}) ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>PSF leakage</td>
<td>Medium</td>
<td>11.0/13</td>
<td>((0.1 \pm 3.5) \times 10^{-5}) ✓</td>
<td>13.3/13</td>
<td>((1.5 \pm 1.1) \times 10^{-5}) ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Random points</td>
<td>Medium</td>
<td>16.4/13</td>
<td>((0.4 \pm 2.8) \times 10^{-5}) ✓</td>
<td>7.2/13</td>
<td>((2.0 \pm 3.6) \times 10^{-5}) ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Flip lens–source samples</td>
<td>High</td>
<td>12.0/13</td>
<td>((0.6 \pm 1.8) \times 10^{-5}) ✓</td>
<td>8.7/13</td>
<td>((1.2 \pm 1.9) \times 10^{-5}) ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source size splits</td>
<td>Low</td>
<td>39.4/13</td>
<td>Up to 18 \pm 4 per cent ✓</td>
<td>7.6/13</td>
<td>Up to 3 \pm 5 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source S/N splits</td>
<td>Low</td>
<td>13.2/13</td>
<td>Up to 1 \pm 4 per cent ✓</td>
<td>18.0/13</td>
<td>Up to 10 \pm 5 per cent ×</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source size splits</td>
<td>Medium</td>
<td>9.1/13</td>
<td>Up to 7 \pm 3 per cent ✓</td>
<td>8.7/13</td>
<td>Up to 5 \pm 5 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source S/N splits</td>
<td>Medium</td>
<td>8.8/13</td>
<td>Up to 4 \pm 4 per cent ✓</td>
<td>16.1/13</td>
<td>Up to 3 \pm 6 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source size splits</td>
<td>High</td>
<td>13.9/13</td>
<td>Up to 9 \pm 4 per cent ✓</td>
<td>23.6/13</td>
<td>Up to 5 \pm 5 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source S/N splits</td>
<td>High</td>
<td>13.2/13</td>
<td>Up to 9 \pm 4 per cent ✓</td>
<td>19.7/13</td>
<td>Up to 6 \pm 6 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source redshift splits</td>
<td>Low</td>
<td>8.8/13</td>
<td>Up to 5 \pm 4 per cent ✓</td>
<td>14.6/13</td>
<td>Up to 4 \pm 4 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Source redshift splits</td>
<td>Medium</td>
<td>11.7/13</td>
<td>Up to 0 \pm 4 per cent ✓</td>
<td>12.3/13</td>
<td>Up to 1 \pm 5 per cent ✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intrinsic alignments</td>
<td>Low, medium</td>
<td>2 per cent</td>
<td>2 per cent</td>
<td></td>
<td>3 per cent</td>
<td>3 per cent</td>
<td></td>
</tr>
<tr>
<td>Intrinsic alignments</td>
<td>High</td>
<td>3 per cent</td>
<td>3 per cent</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Residual multiplicative bias</td>
<td>All</td>
<td>2 per cent</td>
<td>1 per cent</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Stellar contamination</td>
<td>All</td>
<td>2 per cent</td>
<td>2 per cent</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Tangential shear around stars</td>
<td>All</td>
<td>Consistent with 0</td>
<td>Consistent with 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>Low</td>
<td>4 per cent (19 per cent)</td>
<td>3 per cent (10 per cent)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>Medium</td>
<td>4 per cent (8 per cent)</td>
<td>3 per cent (3 per cent)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>High</td>
<td>4 per cent (10 per cent)</td>
<td>4 per cent (3 per cent)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note. Summary of all test results described in Section 5. We show reduced \( \chi^2 \) and constant fit results for all data tests presented in this paper. For the tests based on splitting the sample into two halves, the number in the table is an upper bound on the systematic uncertainty in \( \Delta \chi^2 \) (see the discussion in Section 5.3). For brevity, the first three lines only show results for one lens bin, but the other bins are also consistent with zero. The last three rows show the net systematic uncertainty for each lens bin, obtained by adding in quadrature the systematic uncertainties from individual tests. In each case, the total error is shown both without and with (in parentheses) the inclusion of the results of the source size and S/N split.

NGMIX, but the results for both shear pipelines are summarized in Table 2.

5.1 Cross-component, PSF leakage, and random point shear

For the first three tests (lensing cross-component, PSF leakage, and shear around random points), we show only results using lenses in the range \( 0.35 < \zsource < 0.5 \) and sources \( 0.83 < \zsource < 1.3 \). This range is emphasized because it is the fiducial lens bin of Kwan et al. (in preparation). Note however, these three tests also pass with the other lens and source bin combinations.

In the cross-component test, we measure the cross-shear around lens galaxies, which is a 45° rotated signal with respect to the tangential shear defined in equation (14). This signal should be compatible with zero if the shear is only induced by gravitational lensing, and therefore provides a test for systematic errors related to PSF correction, which can leak into both tangential and cross-components of the galaxy shear. In Fig. 2 we show the resulting cross-shear measured around redMaGiC lenses. The reduced \( \chi^2 = 8.3/13 \) for NGMIX (IM3SHAPE), and the test is consistent with a constant fit equal to zero.

Measuring source galaxy shapes requires modelling them convolved with the PSF pattern imprinted by the atmosphere and optics. However, this process is imperfect, such that \(~1\) per cent (3 per cent) of the PSF shape may ‘leak’ into the measured galaxy shape for NGMIX (IM3SHAPE), based on tests in Jarvis et al. (2016). Note that while Jarvis et al. (2016) found leakage is consistent with zero for both pipelines, the values we quote above conservatively assume the maximum allowed leakage within the 1σ errors of Jarvis et al. (2016). In order to quantify this systematic, we measure the tangential shear of the PSF interpolated to the source galaxy locations, where again the tangential shear is measured around the redMaGiC lenses. In Fig. 2 we show the result, multiplied by a

![Figure 2](link). Cross-component of the shear (purple circles) and PSF leakage given by measuring tangential shear using the interpolated PSF at source positions (red triangles). Scales \( \theta < 0.5 \) arcmin and \( \theta > 70 \) arcmin not used in our fits or \( \chi^2 \) results are indicated by shaded bands. (Note that the pictured PSF leakage result is multiplied by 100, as labelled in the plot.) Both tests pass with constant fits consistent with zero.
correction is small at all scales used in the analysis. This measurement tests the importance of systematic shear which is especially problematic at the survey boundary, and allows us to compare the magnitude of the systematic shear with the magnitude of the signal around actual lens galaxies. In Fig. 3 we show the result, which is consistent with the null hypothesis. Again, see Table 2 for all the detailed test results.

5.2 Flip lens and source samples

In reality, only source galaxies which are behind foreground lenses will be lensed. However, in the presence of redshift errors some low-redshift sources will mistakenly be put behind the lenses, and vice versa. To get some handle on this effect, we repeat the measurement of $\langle \gamma_t \rangle$ but using foreground sources ($0.2 < z_s < 0.5$) stacked around our highest redshift lenses ($0.5 < z_L < 0.8$). Note that this test is noisy and thus easily satisfied when applied to the lower and medium redshift lens samples due to insufficient numbers of foreground sources. The result is shown in Fig. 3 and Table 2, and is consistent with the null hypothesis.

5.3 Source size splits

Shape measurements may be more biased for source galaxies which are smaller and less well resolved. Although we have applied multiplicative bias corrections to our measurements (for IM3SHAPE) or checked they are small (for NGMIX) (see Jarvis et al. 2016), we test to ensure that there is no residual bias by splitting the source galaxies into two samples with different size. We use the ‘round’ measure of size (Jarvis et al. 2016) for NGMIX, EXP_T_R, splitting the two samples at 0.45 and measuring their difference relative to the central values of the combined sample. For IM3SHAPE, the corresponding cut is 1.4 using the $R_{\text{pp}}/R_p$ size parameter, where $R_{\text{pp}}/R_p$ is the full width at half-maximum (FWHM) of the convolved model divided by the FWHM of the PSF for each exposure. We use these values in order to make a 60 per cent/40 per cent split of the source galaxies, with slightly more sources in the smaller size bin. This choice is made since smaller sources may be somewhat more noisy, but the test results are not strongly dependent on the exact cut.

Figure 4. Upper panels: the difference between the $\Delta \Sigma$ signals from small and large source galaxies relative to the central values of the full sample for NGMIX (purple circles) and IM3SHAPE (red triangles), measured for all three lens samples. Lower panels: the same, but showing results for the split between low and high signal-to-noise ratio sources. These splits are not always consistent with zero, see the text in Section 5.3 for a detailed discussion. Only data in the middle, unshaded region of each plot is used for our tests and measurements.
The result for the lowest redshift lens bin, shown in Fig. 4, has a reduced $\chi^2 = 39.4/13$ (7.6/13) for NGMIX (IM3SHAPE). This is a very high $\chi^2$ result for NGMIX. As described at the beginning of this Section 5, to quantify any possible systematic uncertainty we fit a constant to the fractional difference to determine its magnitude. The result is a constant $\sim 0.36 \pm 0.08$, thus the difference in the shear of small and large source galaxies is significant at about $4\sim 5\sigma$. We assume that the true shear induced by lensing falls somewhere between the answer given by small and large sources. The best-case scenario is that the true shear falls exactly between the two, in which case our full sample would have an unbiased average shear. The worst case scenario is that either small or large sources give biased estimates of the true shear while the other is unbiased. In this case, the bias of the full sample is half the constant fit above, $0.36/2 = 18$ per cent. However, this scenario is at odds with other tests, including the fact that NGMIX and IM3SHAPE shears are in close agreement. In Fig. 5 we show the measured $\Delta \Sigma$ ratio between the two shear pipelines. The consistency is excellent for the two lower lens redshift bins, with systematic differences of $\sim 1$ per cent for the two lower lens redshift bins. Even for the highest lens bin, which relies on the highest redshift sources, the difference is only 9 per cent. The good agreement between pipelines provides some evidence for the smaller estimate of systematic uncertainty. In Table 2 we note the total systematic uncertainty for NGMIX, both with and without this size split. When performing HOD fits in Section 6.2 we do not include this 18 per cent.

The picture is significantly better for NGMIX when using the middle and highest lens redshift bins. These results are also shown in Fig. 4 and indicate a conservative $\sim 2\sigma$ systematic of 7 per cent (9 per cent) for the size split of middle (highest) lens redshift bin. These two lens bins use nearly the same sources, but weighted differently according to equation (19). We have not been able to identify the source of the size split difference, but note here another possibility for investigation. A size-filtered subsample might have a redshift distribution that is different from what was estimated based on g, r, i, and z magnitudes alone. For example, Gruen et al. (2014) found an $\sim 5\sim 10$ per cent effect in the mean $D_N(z_L, z_s)/D_N(z_s)$ from a size split (between a large size subset and the full sample) selected in B, R, and I filters. This means that given the same colour and magnitude – and therefore the same implied redshift – the difference in the shear between the large sources and the full sample was $\sim 5\sim 10$ per cent. Similarly, Applegate et al. (2014) found a 5 per cent difference in the lensing signal when using a large size subset. We do not have the resources to explore this effect further in DES-SV, but it will be worth studying in DES Year 1 data.

### 5.4 Source S/N splits

While source galaxy S/N is partially correlated with size, it is a distinct parameter that may separately influence the accuracy of fitted shapes. Thus, we find the difference of two samples with S/N $< 45$ and S/N $> 45$, where S/N is the NGMIX ‘round’ signal-to-noise ratio measure $\exp_s S_{2N_R}$. For IM3SHAPE, source S/N is given by SNR in the IM3SHAPE catalogue. (See Jarvis et al. 2016 for more details on these measurements of galaxy S/N.) Again, this split puts 60 per cent of the sources into the smaller S/N bin. The result is shown in Fig. 4 and summarized in Table 2 for both pipelines. While the size split in Section 5.3 failed for NGMIX and passed for IM3SHAPE, here the trend is reversed. The constant fit to the difference is consistent with zero for NGMIX, but indicates a systematic uncertainty with magnitude $\sim 10$ per cent for IM3SHAPE, using the lowest lens redshift bin. The middle and high lens redshift bins pass this test for both pipelines as summarized in Table 2.

Note that when repeating this test for the highest redshift lens bin, we adjust the cut between low and high S/N samples to 35. This is necessary because for both catalogues the source S/N distribution is significantly different for small and large S/N galaxies. The adjusted cut ensures the number of galaxies in the small S/N sample remains $\sim 60$ per cent.

### 5.5 Source redshift splits

For the following null test, we look for differences in the lensing signal computed using two source samples split on redshift. For continuity, these are the two higher redshift bins used by Becker et al. (2016). The bins are $0.55 < z < 0.83$ and $0.83 < z < 1.30$, where $z$ is the mean of the source $\text{SKYNET} p(z)$. We compute the difference of $\Delta \Sigma(R)$ for both samples, for both the low- and medium-redshift lens bins. The result is shown in Fig. 6, and for both NGMIX and IM3SHAPE shears the result is consistent with zero for both lens samples. For NGMIX, the lowest redshift lens bin has a constant fit $5 \pm 4$ per cent, which is outside $1\sigma$. However as described at the beginning of Section 5, one in three independent tests are expected to fail at this level. As with previous sections, the $\chi^2$ and constant fit numbers are described in detail in Table 2.

### 5.6 Intrinsic alignments

We have so far assumed that a source galaxy’s observed tangential ellipticity is an unbiased estimate of its tangential shear. This is valid if the source galaxy’s intrinsic ellipticity is not correlated with the direction to the lens, which is reasonable if source and lens galaxies are separated in redshift, i.e. not physically close. However since we have only imperfect, photometric redshift estimates, there is some overlap in redshift between sources and lenses (see Fig. 1).

The intrinsic shapes of galaxies are correlated with the cosmological density field, an effect known as ‘intrinsic alignments’ (IA). Thus, for lens–source pairs which are physically close, source galaxies may be preferentially aligned with the direction to the lens
galaxy. For example, in the commonly used linear alignment model (Catelan, Kamionkowski & Blandford 2001; Hirata & Seljak 2004), the intrinsic ellipticity is linearly related to the tidal field (with a free amplitude), producing a correlation between intrinsic ellipticity and density that has the same scale dependence as the shear on linear scales. On large (two-halo) scales, the linear alignment model is expected to describe elliptical source galaxies well, especially when non-linear contributions are included, such as in the 'non-linear linear alignment model' (Bridle & King 2007) or the 'complete tidal alignment model' (Blazek, Vlah & Seljak 2015). This has been confirmed by measurements of LRG alignment (e.g. Singh, Mandelbaum & More 2015).

Accounting for the full photometric redshift distributions, we find that for our 0.35 < z < 0.5 lens bin and 0.55 < z < 0.83 source bin, the non-linear linear alignment model predicts at most an ~4 per cent contamination of the tangential shear signal. The 4 per cent results from using the fiducial IA amplitude (A = 1) from Bridle & King (2007). (See fig. 8 of The Dark Energy Survey Collaboration 2015, which estimated IA amplitude for this source sample for different model scenarios. The model with the largest value of A found A = 2 ± 1, but the result was highly model dependent with some scenarios consistent with 0.) Roughly half of the S/N of the 0.35 < z < 0.5 lens bin comes from sources in the range 0.55 < z < 0.83; based on the N(z) in Fig. 1 the higher redshift sources will not overlap in redshift with the lenses. Thus, we estimate a 2 per cent intrinsic alignment contamination of our measurement for this lens bin. This contamination is likely to be reduced further when using the ΔΣ(R) statistic, which downweights sources with redshift close to the lens. The lower lens bin 0.2 < z < 0.35 will have less contamination (see Fig. 1), so we conservatively use 2 per cent for this bin as well. Repeating the above calculation for the 0.5 < z < 0.8 lens bin and 0.83 < z < 1.3 source bin, we find a 3 per cent contamination. For each lens bin we add the estimated IA contamination in quadrature to our other sources of error.

As an additional check, we compare the 2 per cent estimate for the 0.35 < z < 0.5 lenses and 0.55 < z < 0.83 sources to the most relevant current observational constraints of Blazek et al. (2012).

Using an SDSS Data Release (DR7) LRG lens sample and photometric source sample, Blazek et al. (2012) solve simultaneously for the intrinsic alignment and lensing signals. They find model-independent upper limits (95 per cent confidence level) on the contamination of ΔΣ(R) of ~6 per cent for a projected separation 1 h⁻¹ Mpc. This is further reduced to ~3 per cent when assuming that blue source galaxies have zero intrinsic alignment amplitude. Thus, the 2 per cent estimated using our specific lens and source redshift distributions is compatible with previous observational constraints. Although it is beyond the scope of this work, the approach in Blazek et al. (2012) of constraining the intrinsic alignment signal simultaneously with the lensing signal should be pursued in future DES analyses with improved statistical power.

5.7 Non-weak shear and magnification

The observable reduced shear will differ from γᵣ, according to

\[ g_i = \gamma_i \frac{1}{1 - \kappa}. \]

Since κ is always rising with decreasing distance from the halo centre, the error from using γᵣ rather than gᵢ will be highest at our lowest fit radii, R ≈ 0.1 Mpc h⁻¹. Taking our largest best-fitting halo mass ~2 × 10¹³ M⊙ h⁻¹ from Fig. 8, and assuming an NFW profile for κ, we find that the fractional difference between the shear and reduced shear (γᵣ − gᵢ)/gᵢ is at most 3.5 per cent. The difference falls to 2 per cent by our second data point at R ≤ 0.13. At a halo mass 3 × 10¹³ M⊙ h⁻¹, roughly the upper edge of the most massive 1σ constraints in Fig. 8, the difference at the lowest fit radius is at most 5 per cent. Since the error in ignoring non-weak shear effects is much less than our other sources of systematic and statistical error, we neglect it in the analysis. Similar to non-weak shear, magnification is a potential systematic effect that is more important for lenses with larger κ than our sample. See Mandelbaum et al. (2006) for a galaxy–galaxy lensing-specific discussion of the effects of magnification.

5.8 Total systematic uncertainty budget

All sources of systematic uncertainty studied in this paper are summarized in Table 2. This list should account for all the important systematic uncertainties in our measurements. The final lines of Table 2 show the net systematic uncertainty for each lens redshift bin, obtained by adding the individual sources of systematic uncertainty in quadrature. The systematic difference between large and small sources, photo-z bias, shear calibration, and stellar contamination all cause multiplicative biases on ΔΣ. Thus, we estimate the systematic covariance matrix for each lens bin as Ωs = f² ΔΣ ΔΣ, where f is the total systematic uncertainty for that lens bin in Table 2 (e.g. 4 per cent for the NGMIX shears and middle-z redMaGiC sample), and ΔΣ(R) is abbreviated ΔΣ. In Table 2 we show results both with and without the size and S/N splits, as discussed in Section 5.3. Our total covariance matrix used in the HOD fits (Section 6.2) is then Ω = Ωs + Ωi, where we drop the size and S/N splits. This approach is similar to that followed for galaxy–galaxy lensing measurements by e.g. Mandelbaum et al. (2006). That work folded together shear calibration, photo-z bias, and stellar contamination into a systematic uncertainty which was added in quadrature to the statistical errors when performing fits to the halo mass.
difference between the pairs of bins is $0.12 \pm 0.2$, $-0.06 \pm 0.21$, and $0.17 \pm 0.13$: the result is within 1σ of zero for two cases and just outside 1σ for the final case. We conclude that our measurements are consistent with no evolution of the red sample, although they still leave open the possibility that future, higher signal-to-noise ratio data will measure a difference.

Having checked that the measurements from every redshift bin are consistent, we also measure $\Delta \Sigma$ using the full redshift range, $0.2 < z < 1.3$. We calculate the signal-to-noise ratio of the measurement of the full sample as $S/N = \sqrt{\chi^2 - N_{\text{null}}}$, where the $\chi^2$ is calculated using the jackknife covariance and a null model equal to zero. We subtract the expectation value of the null hypothesis $\chi^2$ distribution, $N_{\text{null}}$, to make this an unbiased estimator of $S/N$.

We also show $\gamma_i$ measurements in Fig. 7 with the same lens samples, calculated according to equation (17). For the lower and middle (upper) lens redshift bins, we use source redshifts 0.55 < $z_s$ < 1.30 (0.83 < $z_s$ < 1.30). The gap between lens and source redshifts is helpful in minimizing the inclusion of source galaxies that are actually in front of the lens, and therefore not lensed. For $\gamma_i$ results with source tomography, and the implications for cosmology, see Kwan et al. (in preparation).

### 6.2 Mean mass constraints

In this section, we use the measurements of $\Delta \Sigma(R)$ to explore the dark matter environment of redMaGiC galaxies. We fit the HOD model described in Section 2 with six free parameters, $M_{\min}$, $M_1$, $\sigma$, $\alpha$, $f_{\text{cen}}$, and $\sigma_s$. We only consider scales in the range $0.09 < R < 15$ Mpc $h^{-1}$, due to deblending (Appendix A1) and covariance (Appendix B) constraints. We vary $\sigma_s$ along with HOD parameters because the mass is somewhat sensitive to $\sigma_s$ at large scales: $\sigma_s$ and bias are degenerate, the two-halo term is proportional to bias, and bias is a monotonic function of mass in our model. Our model fits are less sensitive to the other cosmology parameters, which we fix to $\Omega_m = 0.31$, $h = 0.67$, $\Omega_b = 0.048$, $n_s = 0.96$, and $w = -1$, all of which are consistent with the results of Kwan et al. (in preparation). Note that the results for redMaGiC galaxy bias are given in Kwan et al. (in preparation), which uses large-scale clustering in order to break the degeneracy between bias and $\sigma_s$. We use the COSMOSIS package\(^6\) (Zuntz et al. 2015) to perform all fits.

Our best-fitting models are shown in Fig. 7 for each of the three lens bins. The model goodness-of-fit is excellent in each case, with reduced $\chi^2 = 7.7/7$, 10.6/7, and 8.1/7, in order of increasing redshift. In Fig. 8 we show constraints on the mean halo mass derived from the HOD:

\[
M_{\text{mean}} = \frac{1}{R} \int M_b \frac{dn}{dM_b} \langle N(M_b|M'_b) \rangle dM_b, \tag{26}
\]

where $\frac{dn}{dM_b}$ is the halo mass function and $\langle N(M_b|M'_b) \rangle$ is the number of central and satellite galaxies. The mean mass ranges from $\sim 10^{13.35}$ to $10^{13.12} M_{\odot} h^{-1}$ and shows little evolution between redshift bins. Although the $z = 0.5$–0.8 bin has a lower best-fitting central value, much of the difference is due to pseudo-evolution (Diemer, More & Kravtsov 2013), the change in mass between haloes at different redshifts due to defining mass relative to the mean matter density at that redshift. Based on the results of Diemer et al. (2013), this effect accounts for a drop in halo mass of $\Delta \log_{10} M_{\text{mean}} \sim 0.1$ between $z = 0.3$ and 0.7. This is roughly the size of our error bars, reducing the difference between bins to about 1σ. Note also

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\(^6\) https://bitbucket.org/joezuntz/cosmosis
that the errors in Fig. 8 are correlated; our quantitative test for consistency of $\Delta \Sigma$ between different redshift bins (see Section 6.1) takes into account these correlations.

Our results on $\sigma$ and $\alpha$ were strongly informed by our choice of priors. $M_{\text{min}}$ is constrained by our lensing data, but its central value is sensitive to the choice of priors in $\sigma$ and $\alpha$. However, our key result for the mean mass of redMaGiC haloes is not sensitive to the choice of priors. We checked this by changing the priors significantly (e.g. doubling the prior width) from the fiducial choices in Table 1 and noting that the mean mass results of Fig. 8 were unaffected. Thus, at the level of our measurement errors, weak lensing is able to constrain the mass regardless of the uncertainty in the full HOD.

7 CONCLUSIONS

The main goal of this work was to validate galaxy–galaxy lensing measurements made with DES SV data. To that end, we have performed a number of null tests on the shear catalogues and photometric redshifts and have quantified remaining systematic uncertainties. We performed these null tests and all measurements with two independent shear pipelines, NGmix and m3Shape, and found good consistency between the two methods. The null tests and theory uncertainties are described in Section 5. One unresolved issue is the size split test with the NGmix catalogue, which showed significant differences in $\Delta \Sigma$ measured from large and small source galaxies. We discuss in Section 5.3 the results of this test and why it is difficult to interpret, and leave its resolution for future work. We validated our jackknife statistical errors using a suite of 50 mock surveys. Such detailed tests are a necessary foundation for other work relying on tangential shear measurements with these data, for example, the cosmology results of Kwan et al. (in preparation) and Baxter et al. (2016), bias results of Prat et al. (2016), and trough (Gruen et al. 2016) and void lensing results (Sánchez et al., 2017).

We measured the lensing signal of redMaGiC galaxies, a sample selected specifically to minimize photometric redshift error and outlier rate. The total S/N of 29 allowed us to fit a simple HOD model and constrain the lens sample’s central halo mass. Dividing the lenses into three redshift bins over the range $0.2 < z < 0.8$, we found no evidence for evolution in the mean halo mass $\sim 2 \times 10^{13} M_\odot h^{-1}$ of our constant comoving density sample, at the level of current errors.

As the analysis begun here continues with DES Year 1 data and eventually the full 5 yr of the survey, the statistical errors will continue to improve. For example, assuming the full survey reaches the goal of 5000 deg$^2$ with the same depth as the SV data, the volume probed by our lens sample will increase by a factor of 36. Shape noise, our dominant small-scale error, depends on the number of lenses as $1/\sqrt{N_{\text{lens}}}$, for fixed source density. Shape noise will thus be a factor of 6 smaller. With this greater volume of data, new challenges will surface in ensuring the measurement is still statistics dominated. This will require further work in understanding and modelling systematic uncertainties, but as those challenges are addressed our HOD constraints will improve quickly. Another improvement for future work will involve adding information from galaxy clustering, as done by Park et al. (2016) in simulations.

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APPENDIX A: SYSTEMATICS TESTS

Here we describe various systematic tests that were studied in other work, but are also relevant for our results. These include deblending and sky subtraction, multiplicative shear bias, stellar contamination, and shear around stars. The impact of these tests on our systematic uncertainty budget is summarized in Table 2.

A1 Deblending and sky subtraction

Both shape measurement methods considered here fit parametric models across square ‘postage-stamps’ of pixels centred on the galaxy being measured. These postage-stamps may contain light from neighbouring objects that could bias the shape measurement. The direction of the bias is likely to be related to the direction of the neighbour with respect to the galaxy being measured – hence if the contaminating light is from the lens, or from objects spatially correlated with the lens, a small-scale contamination to the tangential shear signal could arise. Any such effect is likely to be mitigated by the masking of neighbouring objects during fitting, and removing blended objects from the catalogues, as described in Jarvis et al. (2016) (sections 5.2 and 8.1, respectively). Fig. 20 of Jarvis et al. (2016) shows the tangential shear around bright stars as a function of angular separation, and this shows no evidence for a systematic signal around bright objects at small scales. Nonetheless, we choose a conservative lower angular scale of 30 arcsec for the results in Section 6.

A2 Multiplicative shear biases

Jarvis et al. (2016) studied in detail residual multiplicative biases for these shear catalogues. They found that multiplicative bias should be less than 3 per cent in order to satisfy requirements for cosmic shear. In fig. 24 of that work, they show that residual multiplicative biases are at most 1 per cent for IM3SHAPE and 2 per cent for NGMIX. The one exception is the lowest redshift bin for NGMIX, which has a residual bias ~4 per cent. However, since most of our signal comes from the higher redshift bins, we assume residual multiplicative bias is 2 per cent, and add this in quadrature with the other sources of error.

A3 Stellar contamination and shear around stars

Since stars will not be gravitationally lensed by our lens galaxies, contamination of the source sample by stars will dilute our signal by the fraction of stars in the sample. The DES SV galaxy clustering sample in Crocce et al. (2016) had at most 2 per cent stellar contamination. While the sample selection for clustering differs somewhat from that for the weak lensing shear catalogues (Jarvis et al. 2016), the differences should not increase stellar contamination. Thus, we take 2 per cent as our estimated systematic uncertainty from stellar contamination.

Similarly, stars do not act as gravitational lenses of distant source galaxies. The measurement of tangential shear around faint stars provides a null test that can diagnose problems with PSF interpolation and PSF modelling (Jarvis et al. 2016). This measurement was shown for DES SV data in fig. 20 of Jarvis et al. (2016), and was consistent with the null hypothesis.

APPENDIX B: VALIDATION OF STATISTICAL ERRORS

In order to test the jackknife error bars obtained from the data, we compare to covariances from simulations. The same redMaGiC algorithm has been run on mock galaxies in 50 nearly independent realizations of a 150 deg$^2$ survey constructed by dividing a wide area simulation into 50 pieces (see Section 3.3). First, we compare the covariance from these independent realizations to errors obtained by dividing each 150 deg$^2$ simulation into 144 jackknife regions. This comparison is made using the fiducial lens and source bins from Kwan et al. (in preparation): lenses in the range 0.35 < $z_L < 0.5$ and sources 0.83 < $z_s < 1.3$. Right-hand panel: the same, but showing the covariance from applying the jackknife method to our low-redshift lens sample. This covariance is less noisy since it is an average of the jackknife method applied to 10 simulations, but the qualitative features are very similar. With both methods correlations are only significant on large scales, ~10 arcmin and above.
methods have significant correlations just off the diagonal, starting around \( \sim 10 \) arcmin. At \( \theta \sim 70 \) arcmin, our largest scale used in tests and fits, the jackknife method may overestimate the true error by a factor up to 2.

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