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What is the optimal way to measure the galaxy power spectrum?

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ABSTRACT

Measurements of the galaxy power spectrum contain a wealth of cosmological information. In Smith & Marian, we generalized the power spectrum methodology of Feldman et al. to take into account the key tenets of galaxy formation: galaxies form and reside exclusively in dark matter haloes; a given dark matter halo may host galaxies of various luminosities; galaxies inherit the large-scale bias of their host halo. In this paradigm, we derived the optimal weighting scheme for maximizing the signal-to-noise ($S/N$) on a given band power estimate. For a future all-sky flux-limited galaxy redshift survey of depth $b_1 > 22$, we demonstrate that the optimal weighting scheme does indeed provide improved $S/N$ at the level of $\sim 20$ per cent when compared to Feldman et al. and $\sim 60$ per cent relative to Percival et al., for scales of the order of $k \sim 0.5 \ h \text{Mpc}^{-1}$. Using a Fisher matrix approach, we show the cosmological information yield is also increased relative to these alternate methods – especially the primordial power spectrum amplitude and dark energy equation of state. Caveats: uncertainties in cluster masses, non-linear halo bias and redshift distortions may reduce information gains.

Key words: large-scale structure of Universe.

1 INTRODUCTION

The matter power spectrum is a fundamental tool for constraining the cosmological parameters. It contains detailed information about the large-scale geometrical structure of space-time, as well as the phenomenological properties of dark energy and dark matter. Given a galaxy redshift survey two things are crucial: how to obtain an unbiased and optimal estimate of the information in the matter fluctuations.

State-of-the-art galaxy redshift surveys, such as the Baryon Oscillation Spectroscopic Survey (Anderson et al. 2012, 2014b,a, hereafter BOSS), Galaxy And Mass Assembly (Blake et al. 2013, hereafter GAMA), and WiggleZ (Blake et al. 2011), have all used the approach of Feldman, Kaiser & Peacock (1994, hereafter FKP) to estimate the power spectrum. This assumes that galaxies are a Poisson sampling of the underlying density field. Hence, provided one subtracts an appropriate shot-noise term, and deconvolves for the survey window function, one should obtain an unbiased estimate of the matter power spectrum.

In the last two decades, our understanding of galaxy formation has made rapid progress since the work of FKP and our current best models strongly suggest that galaxies are not related to matter in the way they envisioned (White & Rees 1978; White & Frenk 1991; Kauffmann et al. 1999; Benson et al. 2000; Springel et al. 2005). Furthermore, observational studies have discovered that galaxy clustering depends on various physical properties: e.g. luminosity (Park et al. 1994; Norberg et al. 2001, 2002; Zehavi et al. 2002a, 2005; Swanson et al. 2008; Zehavi et al. 2011a), colour (Brown, Webster & Boyle 2000; Zehavi et al. 2002b, 2005; Swanson et al. 2008; Zehavi et al. 2011b), morphology (Davis & Geller 1976; Guzzo et al. 1997; Norberg et al. 2002), and stellar mass (Li et al. 2006) etc.

Percival, Verde & Peacock (2004, hereafter PVP) attempted to correct the FKP framework to take into account the effects of luminosity-dependent clustering. In a recent paper (Smith & Marian 2015, hereafter SM15), we argued that the approach of PVP, whilst appearing qualitatively reasonable, is in fact at odds with our current understanding of galaxy formation, and so non-optimal. More recent studies by Seljak, Hamaus & Desjacques (2009), Hamaus et al. (2010) and Cai, Bernstein & Sheth (2011) suggested that weighting the galaxy density field by a linear function of halo mass would reduce stochasticity.

In SM15, we developed a new scheme incorporating a number of the key ideas from galaxy formation: galaxies only form in dark matter haloes (White & Rees 1978); haloes can host galaxies of various luminosities; the large-scale bias associated with a given galaxy is largely inherited from the bias of the host dark matter halo.

In this work we demonstrate that our new optimal estimator indeed provides both improved signal-to-noise (hereafter $S/N$) estimates of the galaxy power spectrum and boosted cosmological information content, when compared with the FKP and PVP approaches.

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This letter is broken down as follows: First, in Section 2, we provide a brief overview of the results from SM15. In Section 3, we evaluate the $S/N$ expressions for the various weighting schemes and in Section 4 we assess the cosmological information content of the weighted power spectra measured from a putative all-sky galaxy redshift survey. Finally, in Section 5, we conclude.

2 OPTIMAL POWER SPECTRUM ESTIMATION

In the original work of FKP, the starting concept is that galaxies are simply an independent point sampling of the underlying galaxy field. Hence,

$$n_g(r) = \sum_{i=1}^{N_g} \delta^3(r - r_i),$$

where $N_g$ is the number of galaxies, and $r_i$ is the position of the $i$th galaxy in the survey. From this field one then may construct an effective galaxy over-density field:

$$\delta^F_{FKP}(r) = \Theta(r) \omega(r) \left[ n_g(r) - \alpha n_i(r) \right],$$

where $\Theta(r)$ is a survey mask function, which is 1 if the galaxy lies inside the survey volume and 0 otherwise, $\alpha$ is a scaling factor for the spatially random galaxy field $n_i(r)$ and $\omega(r)$ is an optimal weight function that depends on $r$. If we now follow the FKP logic and compute the power spectrum of the $\delta^F_{FKP}$ field, one finds that it is related to the galaxy power spectrum $P_g(k)$ through the relation:

$$\left\langle \delta^F_{FKP}(k) \right\rangle^2 = \int \frac{d^3k}{(2\pi)^3} P_g(k') \left| \tilde{G}_{FKP}(k - k') \right|^2 + P_{shot},$$

where $\tilde{G}_{FKP}(k)$ is the weighted version of the Fourier transform of the survey mask function $\Theta(r)$, and $P_{shot}$ is an effective shot-noise correction. If one subtracts the shot noise and deconvolves for the survey window function, then one may obtain an estimate of $P_g(k)$.

It is important to realize that the above procedure is only correct under the assumption that the galaxy power spectrum does not depend on any observable, e.g. galaxy luminosity, colour, spectral type, host halo mass, etc. and that shot noise is as was given by FKP. If these assumptions are wrong, then the functions $P_g(k)$, $\tilde{G}_{FKP}$, and $P_{shot}$ will all pick up these dependencies, resulting in a biased and sub-optimal reconstruction of the ‘true’ power spectrum. As noted earlier, current observational evidence indicates that clustering strength does depend on the sample selection. Hence, FKP must be biased and sub-optimal (PVP also came to a similar conclusions).

We now summarize the SM15 formalism, designed to account for a number of these effects. Consider a large survey volume containing $N_h$ galaxies that are constrained to be distributed inside $N_h$ dark matter haloes. Thus the $i$th dark matter halo of mass $M_i$ and position of the centre of mass $x_i$, will have $N_g(M)$ galaxies. The $j$th galaxy will have a position vector $r_j$ relative to the centre of the halo and a luminosity $L_j$. For this more complicated distribution, equation (1) can be generalized to:

$$n_g(r, L, x, M) = \sum_{i=1}^{N_h} \delta^3(x - x_i) \delta^3(M - M_i) \times \sum_{j=1}^{N_g(M_i)} \delta^3(r - r_j - x_i) \delta^3(L - L_j),$$

where the four Dirac delta functions, going from right to left, are: sampling; the luminosity of each galaxy in a given halo; the spatial location of a given galaxy relative to the halo centre; the halo mass from the distribution of masses; and the halo centre in the survey volume.

In direct analogy with FKP’s equation (2), we define an effective galaxy over-density field:

$$\mathcal{F}_g(r) = \int dL \int d^3x \int dM \Theta(r|L) \frac{w(r, L, x, M)}{\sqrt{\Delta}} \times \left[ n_g(r, L, x, M) - \alpha n_i(r, L, x, M) \right],$$

where $\Theta(r|L)$ is the luminosity-dependent survey geometry function; $\Delta$ is a normalization constant; $\alpha$ is a scaling factor for the random halo catalogue; $w$ is a general weight function. The function $n_i$ is the same as $n_g$, except the spatial locations of the halo centres have been randomized and the number density has been scaled up by a factor of $1/\alpha$. As shown by SM15, in the large-scale limit, when the distribution of galaxies in haloes adopts a Dirac delta distribution, we define an effective shot noise. Note, in arriving at the above result, whilst we have assumed a linear bias model, the matter power spectrum is the fully non-linear spectrum. The set of survey window functions that are required to evaluate these expressions can be written in general:

$$\left\langle |\mathcal{F}_g(k)|^2 \right\rangle \approx \int \frac{d^3q}{(2\pi)^3} \left| P(q) \tilde{\varTheta}^{(1)}(k - q) \right|^2 + P_{shot},$$

where $P(q)$ is the true matter power spectrum, which is convolved with the effective survey window function $\tilde{\varTheta}^{(1)}(k)$, and $P_{shot}$ is a new effective shot noise. Note, in arriving at the above result, whilst we have assumed a linear bias model, the matter power spectrum is the fully non-linear spectrum. The set of survey window functions that are required to evaluate these expressions can be written in general:

$$\varTheta^{(n)}(r, M, \chi) = A^{n/2} \int dM \tilde{B}^n(M, \chi) N^{(n)}(M)$$

$$\times \left[ \int dL \Theta(r|L) \Phi(L|M) w^\prime(r, L, x, M) \right]^n,$$

where in the above $\tilde{B}(M, \chi)$ and $b(M, \chi)$ are the mass function and large-scale linear bias of haloes of mass $M$ at radial position $\chi$ from the observer ($\chi$ here is also acting as coordinate time); $N^{(n)}(M)$ gives the $n$th factorial moment of the halo occupation distribution (hereafter HOD); $\Phi(L|M)$ gives the conditional probability density that a galaxy hosted in a halo of mass $M$ has a luminosity $L$. Using these functions, the effective shot noise term can be written:

$$P_{shot} \equiv (1 + \alpha) \left[ \int d^3q \left( \tilde{\varTheta}^{(2)}_{(1,0)}(q) + \tilde{\varTheta}^{(1)}_{(2,0)}(0) \right) \right].$$

We also introduce the normalization-free window functions $\varTheta^{(n)}_{(l,m)} = A^{n/2} G^{(n)}_{(l,m)}$, which enables us to write: $A \equiv \int d^3q \tilde{\varTheta}^{(1)}(k)^2$. We thus see that, similar to the FKP approach, in order to recover the matter power spectrum, one must subtract the effective shot-noise term and deconvolve for the square of the effective survey window function $\tilde{\varTheta}^{(1)}(k)$.

In the large-scale limit and under the assumption that the matter density field is Gaussianly distributed, SM15 also showed that the
$S/N$ can, for an arbitrary weight $w$, be written in general as
\begin{equation}
\left( \frac{S}{N} \right)^2 = \frac{V(k)}{2(2\pi)^3} \left[ \int d^3r \left( \frac{|\Sigma_{11}^{(1)}(r)|}{\Phi_{11}^{(1)}(r)} \right) \right]^2 \\
\times \left\{ \int d^3r \left( \left( \frac{|\Sigma_{11}^{(1)}(r)|}{\Phi_{11}^{(1)}(r)} \right) \right)^2 \\
+ \frac{(1+\alpha)}{P(k)} \left( \left| \Sigma_{00}^{(2)}(r) + \Sigma_{11}^{(1)}(r) \right| \right)^2 \right\}^{-1},
\end{equation}

where $V(k) = 4\pi r^3 \Delta k \left[ 1 + (\Delta k/k) \right]/12$ is the volume of the $i$th $k$-space shell in which $P(k)$ is estimated.

3 COMPARISON OF WEIGHTING SCHEMES

The failure of the FKP scheme to characterize the true clustering strengths of galaxies means that it is a biased and sub-optimal estimator. We will now show explicitly, under the assumption that the SM15 description of the galaxy population is the correct one, that both the FKP and PVP weighting schemes do indeed lead to sub-optimal measurements of $P(k)$. The weighting schemes are:

(i) The FKP weights: these depend only on the position of the galaxy in the survey:
\begin{equation}
w_{\text{FKP}}(r) = 1/ \left[ 1 + \bar{n}_g(r)P(k) \right],
\end{equation}
where $\bar{n}_g(r)$ is the mean number density of galaxies.

(ii) The PVP weights: these depend explicitly on the luminosity dependence of the galaxy bias and also the position in the survey:
\begin{equation}
w_{\text{PVP}}(r, L) = b(L)/ \left[ 1 + \bar{n}_g(r) \bar{b}_7^2(r)P(k) \right],
\end{equation}

where the luminosity-dependent galaxy bias is
\begin{equation}
b(L) \equiv \int dM f(M)b(M)N_{11}^{(1)}(M)\Phi(L)/\Phi(L), \quad b_7^2(r) \equiv \int_{\text{limit}} \left( DL b^2(L)\Phi(L)/\bar{n}_g(r) \right), \quad \text{is the average square of the luminosity bias.}
\end{equation}
The galaxy luminosity function is given by \(\Phi(L) \equiv \int dM h(M)N_{11}^{(1)}(M)\Phi(L)/\Phi(L)\), and \(N_{11}^{(1)}(M)\) was introduced after equation (7).

(iii) Optimal weights: the large-scale limit, these weights depend only on the galaxy’s spatial position and its host halo mass, and not explicitly on its luminosity. The weights are
\begin{equation}
w_{\text{OPT}}(r, M) = b(M)/ \left[ 1 + R(M)S(r, M) \right] \left[ 1 + \bar{n}_\text{eff}(r)P(k) \right],
\end{equation}

The effectiveness number density of galaxies: \(\bar{n}_\text{eff}(r) \equiv \int dM h(M)b(M)N_{11}^{(1)}(M)\Phi(L)/\Phi(L)\), where we define \(S(r, M) \equiv \int_{\text{limit}} \left( DL b^2(L)\Phi(L)/\bar{n}_g(r) \right), \quad \text{as the fraction of galaxies hosted by haloes of mass } M \text{ that are observable at a spatial position } r, \text{ with } L_{\text{min}}(r) \text{ the minimum luminosity that a galaxy could have and still be observable given the survey flux-limit. Explicitly, } L_{\text{min}}(r) \equiv 10^{-2} (m_\text{min} - 25 - M_\odot h^{-1} Mpc^2/L_\odot), \quad \text{where } m_\text{min} \text{ is the apparent magnitude limit of the survey, } M_\odot \text{ is the absolute magnitude of the sun, } h \text{ is the dimensionless Hubble parameter and } d_\odot(r) = (1 + z)h(z) \text{ is the luminosity distance in flat cosmological models. Note that } S(0, M) = 1 \text{ and } S(\infty, M) = 0. \text{ For more details on the } S/N \text{ expressions for the three weights considered, we refer the interested reader to SM15.}

We now show the $S/N$ on the galaxy power spectrum corresponding to the FKP, PVP and SM15 methods for weighting the galaxy distribution. As a concrete example we consider a flux-limited, full-sky galaxy redshift survey spanning the redshift range $z = 0.3-0.9$. In order to evaluate the above expressions, we need to specify several model ingredients. For the evolution of $\bar{n}(M)$ and $b(M)$, we use the models of Sheth & Tormen (1999). For the conditional probability distribution $\Phi(L|M)$ and the first factorial moment of the HOD $N_{11}^{(1)}(M)$, we use the Conditional Luminosity Function model of Yang, Mo & van den Bosch (2003). For the second factorial moment, we use the model: $N_{11}^{(2)}(M) = \beta(M)N_{11}^{(1)}(M)^2$, where from fitting to semi-analytic models of galaxy formation $\beta^{1/(2)}(M) = 1/2 \log_1(M/10^{11}h^{-1} M_\odot)$ for the case that $M < 10^{11}h^{-1} M_\odot$ and unity otherwise (Cooray & Sheth 2002). From these ingredients, all required variables may be computed.

Fig. 1 shows the $S/N$ for the SM15 (blue lines) and PVP (red lines) schemes ratioed with the $S/N$ for the FKP scheme, respectively. The results are presented as a function of limiting $b_1$ magnitude and for various $k$-mode bins. Clearly, the optimal scheme of SM15 does indeed lead to the largest $S/N$: $\geq 5$ per cent improvement over FKP at $k \sim 0.2 h\ Mpc^{-1}$, and $\geq 20$ per cent improvement at $k \sim 0.5 h\ Mpc^{-1}$ for surveys with depth $b_1 \geq 22$. Interestingly, the scheme of PVP leads to the least optimal set of estimates, being $\sim 20$ per cent lower than FKP at $k = 0.2 h\ Mpc^{-1}$ and $\sim 40$ per cent lower by $k = 0.5 h\ Mpc^{-1}$, again for surveys with $b_1 \geq 22$.

4 FORECASTING COSMOLOGICAL INFORMATION

The ability of a set of power spectrum band-power estimates to constrain the cosmological parameters $\theta_c$, can be forecasted through construction of the Fisher information matrix (Tegmark, Taylor &
Heavens 1997). For a continuum limit of Fourier modes the Fisher matrix can be expressed as (Tegmark 1997):

$$ F_{\alpha\beta} = \int \frac{d^3k}{V(k)} \frac{\partial \log P(k)}{\partial \theta_{\alpha}} \frac{\partial \log P(k)}{\partial \theta_{\beta}} \left( \frac{S}{N} \right)^2(k). $$

Thus, in order to compute the Fisher matrix, one needs to specify the $S/N$, and the derivatives of the power spectra with respect to the cosmological parameters. The former were computed in the previous section, and we estimate the latter at a single redshift. Therefore our forecasts will be pessimistic, since we do not fully take into account the information in the growth of structure, but here we are only interested in the relative differences between the three weighting schemes.

For our fiducial model, we adopt a flat, dark-energy dominated cosmological model, characterized by eight parameters: $\theta_{\alpha} \in \{ w_0, w_1, \Omega_{DE}, \Omega_c h^2, \Omega_b h^2, A_s, n_s, \alpha_s \}$. The first two characterize the equation of state for dark energy: $w(a) = p_a/\rho_a = w_0 + (1 - a) w_1$; $\Omega_{DE}$ is the dark energy density parameter; $\Omega_c h^2$ and $\Omega_b h^2$ are the physical densities in cold dark matter and baryons, respectively; and $A_s$, $n_s$, and $\alpha_s$ denote the amplitude, spectral index, and running of the primordial scalar power spectrum, respectively. We adopt the values $\theta_{\alpha} = \{-1, 0, 0.69, 0.12, 0.08, 2.15 \times 10^{-9}, 0.96, 0\}$, consistent with Planck data (Planck Collaboration XVI 2014). The power spectrum derivatives we compute through finite differencing matter power spectra from CAMB (Lewis, Challinor & Lasenby 2000).

Fig. 2 shows the forecasted 1D marginalized errors on the parameters, as a function of the maximum wavenumber $k_{\text{max}}$ entering the integral of equation (13). The panels show the fractional error, or if the fiducial value is zero, the error. Clearly, the smallest errors are obtained when one implements the optimal weighting scheme of SM15 (red solid lines), followed by FRP (blue dashed line) and then PVP (black dotted lines). We notice that the constraints on $(A_s, w_0, w_1)$ show the most significant improvements from the optimal weighting.

Fig. 3 shows the forecasted 2D marginalized errors on various parameter combinations. The line styles are the same as in Fig. 2. Again, the optimal weighting of SM15 performs best and the parameters $(A_s, w_0, w_1)$ appear to be the most affected by the new scheme.

**5 DISCUSSION AND CONCLUSIONS**

In this paper, we presented an overview of the optimal power spectrum estimation scheme of SM15. We argued that the FKP scheme was biased and sub-optimal since it does not take into account variations of clustering with the galaxy sample. We argued that the SM15 framework, which encodes several key concepts from the theory of galaxy formation, is able to describe these variations. We evaluated the $S/N$ resulting from the FKP, PVP, and SM15 weighting schemes for the case of an all-sky galaxy survey. The SM15 weighting scheme was indeed found to be the most efficient estimator. We then turned to the issue of cosmological information and using the Fisher matrix approach showed that the SM15 scheme also produced the smallest errors on cosmological parameters. In particular, the parameters governing the amplitude of the primordial power spectrum and the evolution of the dark energy equation of state were noticeably improved.

It is interesting to note that studies that have looked into minimizing the stochasticity in the halo density field (Seljak et al. 2009; Hamaus et al. 2010), or reconstructing the mass density field (Cai et al. 2011), have demonstrated that optimal results can be achieved through weighting galaxy groups by some linear function of halo mass. In contrast, others have argued that better results can be
What is the optimal galaxy power spectrum?

Figure 3. Forecasted 2D marginalized errors on cosmological parameters for the eight cosmological parameters considered. The maximum wavenumber was set to $k = 0.5 \, h \, \text{Mpc}^{-1}$ and the flux-limit was taken to be $b_j = 22$. Note that we have not properly taken into account the growth evolution of structure, and have used only power spectrum derivatives suitable for a single redshift. Nevertheless, it can be clearly seen that the optimal weighting scheme provides the tightest constraints on parameters.

achieved by ‘clipping’ the density field (Simpson et al. 2011). They argue that saturation of the dense regions enables tree-level calculations to be pushed to smaller scales, thus, gaining information. In the limit of large numbers of galaxies per halo, the mass dependence of the SM15 weights is $w \propto b(M)/N^{(1)}(M)$ per galaxy, hence, dense regions are weighted by $b(M)$, and in the limit of small numbers we also have $w \propto b(M)$. Clearly, the SM15 weighting scheme does not follow the linear functional form of the optimal density field schemes nor the clipping. In any case, it is not obvious that the weighting schemes should be similar. We would simply argue that if one wishes to optimize galaxy power spectra measurements, then one should follow the SM15 scheme. We also point out that uncertainties in the estimation of cluster masses may likely reduce some of the potential gains. However, for SM15, since the weights depend on $b(M)$ which is a slower function of mass than $M$ alone (at least over the scales $0.1 < M/M_\ast < 10$). A scatter in $M$, therefore does not move the weight as much as one might expect, since as was shown in Seljak & Warren (2004), $b(M) \sim \text{const}$ for $M/M_\ast < 0.1$.

In this study, we have incorporated a number of key ideas from galaxy formation theory, however there are other important effects that we have not yet taken into account. In particular, we have neglected redshift space distortions. In the FKP formalism, this was examined by Yamamoto (2003), who found that the mathematical structure of the optimal weights was unchanged, except for the fact that the number density and power spectrum that enter are now both functions of the galaxies position in redshift space. In addition, the more pernicious non-linear distortions (see e.g. Okumura, Seljak & Desjacques 2012), may be minimized through use of optimal Finger-of-God compression algorithms (Reid, Spergel & Bode 2009). Based on this, one might conjecture that the optimal weights
of SM15 may not be too significantly modified in redshift space and so any changes to our results would be relatively small. We intend to explore this in a future work.

We have also made the assumption that halo biasing is linear – but note that this does not mean that the galaxy biasing is linear in our approach, since there is still the halo internal structure. A more advanced estimator is needed to take into account non-linearity and non-locality in the halo bias relation (Smith, Scoccimarro & Sheth 2007; Baldauf et al. 2012; Chan, Scoccimarro & Sheth 2012). However, it is necessary that any improved estimator must converge to the SM15 estimator on large scales. Owing to the fact that linear halo biasing is only valid on scales $k < 0.1 \, h \, \text{Mpc}^{-1}$ (Smith et al. 2007; Angulo et al. 2008), it may be that our weighting is sub-optimal on smaller scales and the information gains that we find are more modest.

Another effect that we have so far neglected is halo-exclusion. As was pointed out in Smith et al. (2007) and later by Smith, Desjacques & Marian (2011) and Baldauf et al. (2013), this has the effect of making shot-noise terms sub-Poissonian on large scales. Again, this may need to be incorporated in the estimation procedure. However, we might expect this to be a second-order correction. Incorporating these effects will be the subject of future study.

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