Challenges in decomposing encodings of verification problems


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Challenges in Decomposing Encodings of Verification Problems

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Modern program verifiers use logic-based encodings of the verification problem that are discharged by a back end reasoning engine. However, instances of such encodings for large programs can quickly overwhelm these back end solvers. Hence, we need techniques to make the solving process scale to large systems, such as partitioning (divide-and-conquer) and abstraction. In recent work, we showed how decomposing the formula encoding of a termination analysis can significantly increase efficiency. The analysis generates a sequence of logical formulas with existentially quantified predicates that are solved by a synthesis-based program analysis engine. However, decomposition introduces abstractions in addition to those required for finding the unknown predicates in the formula, and can hence deteriorate precision. We discuss the challenges associated with such decompositions and their interdependencies with the solving process.

1 Introduction

Logic-based encodings of the verification problem are more and more widespread in software verification [1]. However, the generated formulae are often too large to be directly handled by the back end solver. Classical divide-and-conquer techniques suggest themselves to cope with such large problems. Work on interprocedural verification, e.g. [6, 3], follows the syntactical, procedural structure of the program to perform a decomposition of the formula. This does not seem ideal, but has been shown to significantly increase efficiency in comparison with monolithic solving.

In recent work, we used a synthesis engine [7, 2] to solve for multiple predicates at once even when they are mutually dependent. Since this scales badly to large formulae, we have to decompose the formula in order to reduce the load on the synthesis engine. However, the decomposition may introduce additional abstractions, in particular when mutually dependent predicates are concerned.

Outline We first show the encoding of a verification problem using the example of universal termination verification. Then we discuss the challenges associated with decomposing this problem and the interdependencies with the solving process.

2 Encoding

We assume that programs are given in terms of call graphs, where individual procedures \( f \) are given in terms of symbolic input/output transition systems. Formally, the input/output transition system of a procedure \( f \) is a tuple of characteristic predicates for relations \( (\text{Init}_f, \text{Trans}_f, \text{Out}_f) \), where \( \text{Trans}_f(x, x') \) is the transition relation; the input relation \( \text{Init}_f(x_{\text{in}}, x) \) defines the initial states of the transition system and relates them to the inputs \( x_{\text{in}} \); the output relation \( \text{Out}_f(x, x_{\text{out}}) \) connects the transition system to the outputs \( x_{\text{out}} \) of the procedure. Inputs are procedure parameters, global variables, and memory objects that are read by \( f \). Outputs are return values, global variables, and memory objects written by \( f \). Internal
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In this formula, recursive procedures produce cyclic dependencies of their \(\text{Summary}_f\) predicates. If abstractions are used to lazily solve the formula, the invariant \(\text{Inv}_f\) and the termination argument \(\text{RR}_f\) become interdependent. Similarly, invariants of nested loops are dependent on each other. Rewriting nested loops into a single loop with invariant \(\text{Inv}_f\) only “hides” these dependencies as relational dependencies between the loop variables.

3 Decomposition

We can decompose a formula that encodes a verification problem, such as (1) above, into a sequence of subproblems that are solved by the synthesis engine. The soundness of the analysis result is ensured by (1) the soundness of the analysis of individual subproblems, (2) the soundness of the combination of the subproblem results, (3) and induction over the decomposition hierarchy. Decomposition causes the following issues: (A) It may introduce additional interdependent predicates. (B) The subproblems may be inference, and not verification problems; hence their solving requires optimisation (like our synthesis engine) instead of decision procedures.

Example In [3] we followed the classical approach of a procedural decomposition. We emulate the traversal of the call graph top-down analysing each procedure separately and propagating the summaries back up. This decomposition splits the \(\text{Summary}_h\) predicate for a call to procedure \(h\) at call site \(i\) into

1Mind that we use the notation \(\exists_2\) to stress the fact that the quantifier binds a predicate.
a calling context predicate \( \text{CallCtx}_h \) that transfers information from the caller to the callee and a summary predicate \( \text{Sum}_h \) that transfers information from the callee to the caller. These two predicates are mutually dependent as illustrated by the cycle in the dependency graph in Figure 1a. The dashed arrows are dependencies resulting from unfolding the diagram along the call graph. The blue, green and red ellipses indicate the decomposition, i.e. predicates that are solved for at once. The algorithm in [3] uses a greatest fixed point computation to resolve this dependency. However, this is very imprecise for recursive procedures. Figure 1b shows the predicate dependencies for the inference of sufficient preconditions for termination. Without going into details (see [3]), we want to direct the attention to the dependency (red dashed ellipse) between the under-approximating summary \( \text{Sum}^u_f \) (of which the sufficient precondition is a projection), the termination argument, and the invariants – which is a maximisation problem.

4 Lessons Learned and Prospects

We have to accommodate the following two conflicting goals: (1) Solving as large subformulae as possible to increase precision and reduce the need for later refinement. (2) Solving as small subformulae as possible to be scalable. In Figure 1a we solve for invariants (green) and termination arguments (red) separately because our synthesis engine currently does not support product domains that could infer both at once, each with their optimised domains, thus eliminating cyclic dependencies. Some domains require least, others greatest fixed point computations, our engine is currently unable to combine both in a single query. Moreover, programs are rarely written with verification in mind; they are often badly structured. Therefore we need a property-, precision-, and capacity-driven dynamic (de)composition to achieve goals (1) and (2). Re-partitioning the verification problem by eliminating predicates and introducing new ones seems essential. Decompositions introducing cyclic dependencies should only be used if the solving capacity is exceeded. On the other hand, precision can be increased by expansion, i.e. unrolling of loops and inlining of recursions, if the capacity allows it. Many of these issues are akin to open problems in neighbouring areas of research, e.g. [5].

References


\[2\] The calling context can be inferred by synthesising a predicate \( \text{CallCtx}_h \) s.t. \( \forall x_f, x'_f, x^\text{in}_h, x^\text{out}_h : \text{Inv}_f(x_f) \land \text{Trans}_f(x_f, x'_f) \implies \text{CallCtx}_h(x^\text{in}_h, x^\text{out}_h). \]