Flexible couplings: diffusing neuromodulators and adaptive robotics

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Flexible Couplings: Diffusing Neuromodulators and Adaptive Robotics

Abstract Recent years have seen the discovery of freely diffusing gaseous neurotransmitters, such as nitric oxide (NO), in biological nervous systems. A type of artificial neural network (ANN) inspired by such gaseous signaling, the GasNet, has previously been shown to be more evolvable than traditional ANNs when used as an artificial nervous system in an evolutionary robotics setting, where evolvability means consistent speed to very good solutions—here, appropriate sensorimotor behavior-generating systems. We present two new versions of the GasNet, which take further inspiration from the properties of neuronal gaseous signaling. The plexus model is inspired by the extraordinary NO-producing cortical plexus structure of neural fibers and the properties of the diffusing NO signal it generates. The receptor model is inspired by the mediating action of neurotransmitter receptors. Both models are shown to significantly further improve evolvability. We describe a series of analyses suggesting that the reasons for the increase in evolvability are related to the flexible loose coupling of distinct signaling mechanisms, one “chemical” and one “electrical.”

1 Introduction

This article describes recent results from a two-pronged research effort concerned with understanding more about the role of freely diffusing neurotransmitters in biological nervous systems and with exploring properties of artificial nervous systems based on principles abstracted from biological research. The synthetic approach is embraced in both contexts. Artificial systems embodying the particular phenomena and principles in question are synthesized and then analyzed post hoc [4, 9, 7]. Both strands of the work focus on volume signaling, whereby neurotransmitters freely diffuse into a relatively large volume around a nerve cell, potentially affecting many other neurons [22, 54]. This exotic form of neural signaling does not sit easily with classical pictures of brain mechanisms and is forcing a radical rethinking of existing theory [15, 24, 43, 26]. The first part of the work employs detailed computational and mathematical modeling to study how the dynamics of diffusion interact with neural morphology and influence potential functional roles of this form of signaling [43, 44]. The second strand, which is represented more heavily in this article, looks at the efficacy of novel forms of artificial neural networks incorporating abstract analogues of volume signaling influenced by the detailed modeling work [28, 27]. Instances of these networks are synthesized, via an evolutionary search process, to generate behavior in autonomous mobile robots. Shedding light on the reasons for a significant variation in evolvability of different forms of these networks is the

Keywords GasNet, neuromodulation, evolvability, coupling, evolutionary robotics
central focus of this article. *Evolvability* is used in the sense of consistent speed to very good solutions—here, appropriate sensorimotor behavior-generating systems.

The class of ANNs we developed to explore analogues of volume signaling, we have termed GasNets. These are essentially a standard ANN augmented by a chemical signaling system consisting of a diffusing *virtual* gas that can modulate the response of other neurons. The original GasNet has previously been shown to be more evolvable than traditional ANNs in the context outlined above [28]. In this article we present two new versions of the GasNet, which take further inspiration from the properties of neuronal gaseous signaling. The *plexus* model is inspired by the extraordinary NO-producing cortical plexus structure of neural fibers and the properties of the diffusing NO signal it generates. The *receptor* model is inspired by the mediating action of neurotransmitter receptors. Both new GasNet variants are shown to exhibit significantly improved evolvability relative to the original. One of the most significant features of these two new types of ANNs is the fact that the nature of the coupling between the “electrical” and “chemical” processes is more controllable and flexible than in the original GasNet. We later provide evidence, through a series of analyses described in Section 8, indicating that this has an important influence on evolvability.

Since we develop artificial nervous systems for autonomous mobile robots engaged in sensorimotor behaviors, this work sits squarely in the area often referred to as new AI [11, 40] or embodied cognition [3, 13].

The next two sections provide biological background and motivation. These are followed by a brief description of work concerned with the detailed modeling of diffusing neurotransmitters in real nervous systems, which acts as explicit inspiration for the GasNet variants described in Section 5. Results from comparative evolutionary robotics experiments on the evolvability of various forms of GasNet are detailed in Section 6. These are followed by a series of analyses aimed at trying to explain the differences in evolvability highlighted in the robotics experiments. The article finishes with conclusions.

2 From Neuroscience to Robotics

Modern neuroscience has developed enormously since its beginnings in nineteenth century physiology [21]. Its quest to provide us with an understanding of how nervous system work, although very far from complete, has made great strides in the past few decades. Crucial to these later successes was the early twentieth century pioneering work of the likes of Adrian and Sherrington in elucidating key electrical properties and functions of nerve cells [10, 2, 47], work for which these two illustrious figures shared the 1932 Nobel prize for physiology. With the great benefit of hindsight, it is illuminating to step back to this time and consider the following quotation from Lord Adrian's acceptance speech [1]:

The nerve fibre is clearly a signalling mechanism of limited scope. It can only transmit a succession of brief explosive waves, and the message can only be varied by changes in the frequency and in the total number of these waves. But this limitation is really a small matter, for in the body the nervous units do not act in isolation as they do in our experiments. A sensory stimulus will usually affect a number of receptor organs, and its result will depend on the composite message in many nerve fibres.

In this description we can clearly recognize the connectionist point-to-point electrical transmission picture that dominated thinking about the nervous system for several decades, and that was the original inspiration for artificial neural networks (ANNs) [36, 46] and is still a major focus of computational neuroscience today [16]. However, the past decade or so has brought many fresh insights into the range of interacting signaling mechanisms underlying neural activity. These processes act over a wide range of both temporal and spatial scales and, as mentioned earlier, include such unexpected phenomena as chemical signaling, via diffusing neurotransmitters, between
neurons that are not electrically connected [22]. Research is starting to reveal a far richer and more complex picture than was previously imagined [52, 5]. So although Adrian's notion of understanding the "composite message" is still highly relevant, the details of what might constitute such a message have significantly altered.

However, it is as yet very difficult to gather accurate empirical data for processes such as non-classical neurotransmitter diffusion [44]. Therefore it is natural to turn to computational modeling to shed light on volume signaling. As will be seen in Section 4, detailed models involving diffusing chemicals are computationally very expensive and at the moment have to be restricted to small numbers of neurons rather than whole behavior-generating neuronal circuits. Hence, in order to further investigate functional roles involved in the generation of behavior, we advocate the study of more abstract artificial robot nervous systems incorporating mechanisms based on volume signaling. These systems are computationally tractable and can generate sensorimotor behaviors in real time in the real world.

In order to provide background and context for the experimental work described later, the next section gives more details on volume signaling.

3 Volume Signaling: Beyond Connectionism

In the traditional connectionist model of neuron-to-neuron communication referred to above, neurons generate brief electrical signals (action potentials), which propagate along wirelike axons terminating at highly localized junctions (synapses) on other neurons, where the release of a chemical signaling molecule, or neurotransmitter, is triggered. The neurotransmitter is confined to the region of the synapse, and here the receiving neuron is equipped with receptors that directly translate the chemical signal into a brief electrical signal, either excitatory or inhibitory [45, 10]. Hence in standard ANNs based on this incomplete model, the notion of chemical signaling can be safely factored out, leaving only the idea of electrical signals flowing between nodes in a network.

But some receptors do not directly activate electrical events in the receiving neuron at all. They interact with messenger molecules that are best regarded as modulatory, because among other things they regulate, or modulate, the actions of conventional transmitters. Modulatory neurotransmitters are indirect in that they can cause a range of medium- and long-term changes in the properties of neurons by influencing the rate of synthesis of so-called second messenger molecules. By altering the properties of proteins and even by changing the pattern of gene expression, these second messengers cause complex cascades of events resulting in fundamental changes in the properties of neurons [45]. In this way modulatory transmitters greatly expand the diversity and the duration of actions mediated by the chemicals released by neurons. Thus while simple direct transmission between neurons certainly does exist, it operates in parallel with and sometimes conjointly with indirect chemical signaling systems that operate on an extended temporal scale [12].

The precise action of neurotransmitters also depends on the receptors they bind to. Although most receptors are highly selective, responding to a single transmitter only, most transmitters can bind to a variety of receptors, with different consequences for different transmitter-receptor pairings, even in the same cell [45, 30]. There are a great variety of receptors on different types of cells, suggesting the possibility of a combinatorially explosive range of pairings and effects.

In addition to this, the spatial scale over which neurons can communicate is extended by the recent discovery of non-synaptic chemical signaling [50]. The most important feature of this derives from the ability of some neurotransmitters, in particular small gaseous molecules, to diffuse away from their site of release and to occupy a volume of the nervous system perhaps containing many other neurons and synapses [18]. To date three gaseous neurotransmitter molecules, NO, CO, and H₂S, have been identified; all of them, curiously, are highly poisonous. The most studied among them by far is NO, which is known to diffuse at above-threshold concentrations many tens of microns away from a site of release [43]. Diffusion takes time, so this is not a rapid signaling system. Furthermore, the main receptor for NO is of the indirect type and can have long-term modulatory
effects on neurons [5, 50]. So not only can NO operate over a large region, it can also mediate extended temporal changes in the chemical and electrical properties of neurons within that volume.

Transmission by gases is not and perhaps cannot be confined to the highly localized region of the synapse as in classical point-to-point signaling; thus it loosens the tight coupling between electrical and chemical signals. Thus *volume signaling* can now be added to the growing list of phenomena in the nervous system that might be a source of inspiration for new and perhaps improved styles of ANNs. This is probably especially true for ANNs intended for use as artificial nervous systems, an area where taking inspiration from biology is often particularly fruitful.

Interneural chemical communication systems of the volume signaling variety operate on different temporal and spatial scales from electrical signaling. Thus an important principle we have used in the GasNets is the existence of two separate, yet interacting, signaling systems: one *electrical* and one *chemical*.

Before moving on to the GasNet work, the next section covers elements of the detailed biological modeling work mentioned above. This provides further context and background to the GasNet studies, particularly the plexus GasNet.

### 4 Modeling NO Diffusion in Real Brains

In the previous section the role of NO in neuronal volume signaling was sketched. NO spreads in three dimensions away from the site of synthesis, regardless of intervening cellular or membrane structures [54]. Another very important feature of NO signaling follows from the fact that nitric oxide synthase (responsible for the production of NO) is soluble and thus highly likely to be distributed throughout a neuron’s cytoplasm. This means that the whole surface of the neuron is a potential release site for NO, in marked contrast to conventional transmitter release. These properties suggest that the 3D structure of the NO source, and of any NO sinks, will have a profound influence on the dynamics of NO spread. Hence an accurate structure-based model of neuronal NO diffusion is an indispensable tool in gaining deeper insight into the signaling capacity of the molecule. Figure 1 shows the results generated by the first accurate model of NO diffusion from a continuous biologically realistic structure [43]. The source is an irregular neuronlike structure where the main cell body is a hollow sphere (NO is synthesized in the cell walls but not in the interior of the sphere). Diffusion was modeled using accurate difference equation methods on a fine grid [44]. The modified diffusion equation is approximated as

\[
\frac{\partial C(x,t)}{\partial t} - D \nabla^2 C(x,t) = P(x,t) - S(x,t)C(x,t) - \lambda C(x,t)
\]

where the terms on the left-hand side describe general diffusion and those on the right-hand side take into account NO production and depletion processes. Here \(C(x,t)\) is the concentration at point \(x\), \(D\) is the diffusion coefficient, and \(P(x,t)\) is the concentration of NO produced per second at point \(x\). NO does not have a specific inactivating mechanism, and is lost through reaction with oxygen species and metals as well as with heme-containing proteins [33, 51]. This means that the movement of other molecules and receptors and their interactions need not be modeled and instead a more general loss function can be used. Hence \(S(x,t)\) is a depletion function to model NO sinks (such as blood vessels, with their very high concentrations of NO-binding hemes), and \(\lambda\) is a general inactivation rate for all points outside sinks, reflecting background oxidization and binding events. In this study \(P = Q \rho\) for points inside a source during synthesis, and \(P = 0\) elsewhere. \(Q\) is the amount of NO produced per second by a single NO-producing unit, and \(\rho\) is the density of such units. For full details of modeling methods, all parameter values used, and their biological justification, see [43, 44].

Figure 1 illustrates the evolution of NO concentration during and after a 100 ms burst of synthesis. Two very interesting observations are that the concentration remains high near the center of the cell.
body long after synthesis has finished and that there is a significant delay between the start of synthesis and a rise in concentration for points distant from the main cell body. These observations follow from a reservoir effect, where NO diffuses into the interior of the hollow structure and is then trapped there by a pressure gradient, resulting in a slow time-delayed release [43]. Such a phenomenon, with its possible functional implications, would not have been observed in a less accurate point-source-type model [54], or indeed by purely empirical methods, as they are as yet too crude.

Another very interesting NO signaling phenomenon amenable to computational modeling involves the study of the combined action of many small NO sources that individually cannot generate concentrations above the threshold level needed to have any effect. In particular, NO-producing plexus structures, or meshes, of axonal fibers with diameters of a few microns or less are found in various parts of the brain. A knowledge of the characteristics of the NO signal created by such a structure could be crucial in helping to understand NO’s neuromodulatory role. For instance, while NO-producing neurons account for only about 1% of cell bodies in the cerebral cortex, their processes spread so extensively that almost every neuron in the cortex is exposed to these small fibers, the vast majority of which have diameters of a micron or less [5, 20]. Such structures are common across a range of species; another example is found in the locust optic lobe, where there are highly ordered sets of NO-producing 2 μm diameter fibers [19]. Extending the techniques used for the study illustrated in Figure 1, Philippides et al. have modeled the diffusion of NO from multiple small sources, including plexus type structures [44].

An illustration of how cooperation can occur in a model of fibers in the locust optic lobe is provided by Figure 2, which shows the spatial extent of the NO signal generated by a single fiber of 2 μm diameter and by ordered arrays of 9, 16, 25, and 36 identical fiber sources separated by 10 μm. An ordered array of $N^2$ fibers is an evenly spaced-out 2D arrangement of $N \times N$ fibers. As the fibers are parallel, the solution is constant along the $z$-axis (out of the page), and so we give results only for cross-sectional slices in a plane perpendicular to the direction of the fibers. The single fiber does not achieve an above-threshold signal, principally because the great speed of NO diffusion means that NO will spread rapidly over a large volume. So while NO does not reach threshold anywhere, the volume...
occupied by NO at a significant fraction of threshold is large relative to the source size. Thus NO derived from small and well-separated individual sources can sum to produce an effective NO cloud.

But what are the characteristics of such a signal, and what do they imply for the way NO functions? The first thing to notice from Figure 2 is that while the reservoir effect is still present, with NO accumulating at the center of mass of the sources, the concentration profile appears to be flatter than for a single source. The effect of the spacing between the sources is further illustrated in Figure 3, where the area over threshold generated by 100 fibers is shown as a function of the total cross-sectional area of the source. What is immediately obvious from this figure is that if the goal is to reach the largest number of potential targets with a given volume of source fibers, then a dispersed source is better than a single source. Indeed, with multiple fine sources, it is possible to affect a volume over twice as large as for a solid source, simply by dispersing them correctly.

Figure 3b reveals that the extent of the interaction effect will depend on the spacing used. In particular, the delay before the start of interaction can vary from nothing to more than a second, increasing as the spacing is increased. This means that a system with optimal spacing, with respect to the extent of the affected region, will experience a considerable delay before the region begins to be affected, with the total area affected suddenly rising sharply at the end of the delay. This raises the intriguing functional possibility of a system that is completely unaffected by NO for a given length of time (which would be tunable by changing the spacing), but once past this point, behaves so that large regions are rapidly “turned on” by the cloud of NO.

Figure 2. Volume over threshold (0.25 \(\mu M\)) generated by NO-synthesizing fibers of 2 \(\mu m\) diameter organized in ordered arrays separated by 10 \(\mu m\) after 1 s of synthesis. The fiber dimensions and spacing have been chosen so as to approximate the arrangement of the nNOS-expressing fibers in the optic lobe of the locust [19]. The upper graph shows the volume over threshold per unit length of the fibers. The lower four graphs show the concentrations of NO (dark = low, light = high) in a two-dimensional slice through the fibers, which project out of the page. Here we see how NO from several sources can combine to produce above-threshold concentrations (areas inside the white boundaries), which extend away from the synthesizing region. Scale bar is 50 \(\mu m\).
Further computational studies have shown how a random mesh of fine fibers, as well as enabling similar signaling dynamics to the uniform meshes shown above, is an ideal structure to ensure a uniform concentration tightly targeted over the volume occupied by such a plexus \[42, 44\]. This is exactly the kind of structure found in the cortex; hence these models suggest a functional explanation for the extraordinary morphology of the plexus and point towards an important mechanism for allowing highly targeted NO “clouds” in the brain. In highlighting the functional importance of brain morphology, these phenomena take us increasingly further away from connectionist ideas and suggest that Pfeiffer’s notion of ecological balance, which requires a harmonious relationship between an agent’s morphology, materials, and control \[41\], can perhaps be taken inside the head.

The next section describes a set of ANNs whose properties draw on those of real NO volume signaling systems, including some discovered using the computational modeling approach outlined in this section.

5 GasNets

The GasNet incorporates a mechanism based on the neuron-modulating properties of a diffusing signaling gas into a more standard sigmoid-unit neural network \[28\]. In previous work the networks have been used in a variety of evolutionary robotics tasks, including the one used in this article, comparing the speeds of evolution for networks with and without the gas signaling mechanism active, and showing that GasNets are consistently faster to evolve than more standard networks \[28\]. More recent work has demonstrated advantages of GasNets over other dynamical networks in bipedal and quadrupedal locomotion \[38, 37\], a quite different task from the one used in the study highlighted in this article. A number of related studies have investigated the nature of the GasNet fitness landscapes \[48\] in order to elucidate the reasons for the faster evolutionary search. Other authors have used abstract notions of chemical modulation in neural networks used for controlling agents \[32, 25\], but on a more global level, which does not involve the detailed spatiotemporal aspect we incorporate into our systems. In this section we introduce the basic GasNet model and two further biologically motivated variants (plexus and receptor).

5.1 The Basic GasNet

The electrical network underlying the GasNet model is a discrete-time, recurrent neural network with a variable number of nodes. These nodes are connected by either excitatory (with a weight of +1) or inhibitory (with a weight of −1) links, with the output \(O_n^i\) of node \(i\) at time step \(n\)
determined by a continuous mapping from the sum of its inputs, as described by the following
equation:

\[ O_i^n = \tanh \left( k_{i0} \left( \sum_{j \in C_i} w_{ji} O_j^{n-1} + I_i^n \right) + b_i \right) \]  \hspace{1cm} (2)

where \( C_i \) is the set of nodes with connections to node \( i \), and \( w_{ji} = \pm 1 \) is a connection weight. \( I_i^n \) is the external (sensory) input to node \( i \) at time \( n \), and \( b_i \) is a genetically set bias. Each node has a genetically set default transfer function parameter \( k_{i0} \), which can be altered at each time step according to the concentration of the diffusing gas at node \( i \) to give \( k_i \) (as described later, in Section 5.3).

### 5.2 Gas Diffusion in the Networks

In addition to this underlying network in which positive and negative signals flow between units, an abstract process loosely analogous to the diffusion of gaseous modulators is at work. Some units can emit virtual gases, which diffuse and are capable of modulating the behavior of other units by changing their transfer functions. The networks occupy a 2D space; the diffusion processes mean that the relative positioning of nodes is crucial to the functioning of the network.

The original GasNet diffusion model is controlled by two genetically specified parameters, namely the radius of influence \( (r) \) and the rate of buildup and decay \( (s) \). Spatially, the gas concentration varies as an inverse exponential of the distance from the emitting node with a spread governed by \( r \); the concentration is set to zero for all distances greater than \( r \) (Figure 4):

\[
C(d, t) = \begin{cases} 
  e^{-2d/r} \times T(t), & d < r \\
  0, & \text{else}
\end{cases}
\]  \hspace{1cm} (3)

The maximum concentration at the emitting node is 1.0, and the concentration builds up and decays from this value linearly as dictated by the time course function \( T(t) \), defined by

\[
T(t) = \begin{cases} 
  H\left( \frac{t - t_s}{t_e} \right), & \text{emitting} \\
  H[H\left( \frac{t - t_s}{t_e} \right) - H\left( \frac{t - t_s}{t_e} \right)], & \text{not emitting}
\end{cases}
\]  \hspace{1cm} (4)

with

\[
H(x) = \begin{cases} 
  0, & x \leq 0 \\
  x, & 0 < x < 1 \\
  1, & \text{else}
\end{cases}
\]  \hspace{1cm} (5)

where \( C(d,t) \) is the concentration at a distance \( d \) from the emitting node at time \( t \); \( t_e \) is the time at which emission was last turned on, \( t_s \) is the time at which emission was last turned off, and \( s \) (controlling the slope of the function \( T(t) \) is genetically determined for each node. The total
concentration at a node is then determined by summing the contributions from all other emitting nodes (nodes are not affected by their own concentration, to avoid runaway positive feedback).

### 5.3 Modulation by the Gases

For mathematical convenience, in the basic GasNet there are two gases, one whose modulatory effect is to increase the transfer function gain parameter \( k_n^i \) from Equation 2 and one whose effect is to decrease it. It is genetically determined whether or not any given node will emit one of these two gases (gas 1 and gas 2), and under what circumstances emission will occur (either when the electrical activation of the node exceeds a threshold, or when the concentration of a genetically determined gas in the vicinity of the node exceeds a threshold; note these emission processes provide a coupling between the electrical and chemical mechanisms). The concentration-dependent modulation is described by the following equation, with transfer parameters updated on every time step as the network runs:

\[
    k_n^i = k_0^i + \alpha C_1^i - \beta C_2^i
\]

where \( k_0^i \) is the genetically set default value for \( k_i \), \( C_1^i \) and \( C_2^i \) are the concentrations of gas 1 and gas 2, respectively, at node \( i \) on time step \( n \), and \( \alpha \) and \( \beta \) are constants. Both gas concentrations lie in the range \([0, 1]\). Thus the gas does not alter the electrical activity in the network directly, but rather acts by continuously changing the mapping between input and output for individual nodes, either directly or by stimulating the production of further virtual gas. The concentration-dependent modulation can, for instance, change a node’s output from being positive to being zero or negative even though the input remains constant. Any node that is exposed to a nonzero gas concentration will be modulated. This set of interacting processes provides the potential for highly plastic systems with rich dynamics. Typically, many aspects of a functioning GasNet, such as the gas concentrations at any point or the gain parameter of a given node, are in continuous flux as it generates behavior in a mobile robot engaged in a sensorimotor task. The general form of the diffusion is based on the properties of a single source neuron as modeled in Section 4. The modulation chosen is motivated by what is known of NO modulatory effects at synapses [5].

Figure 4. (a) The spatial distributions of gas concentration for the different GasNet models. The solid line denotes the spatial distribution for the original GasNet model, while the dotted line shows the spatial distribution for the plexus model. Units are the (internally consistent) ones used in the implementation. See text for further details. (b) The spatial distributions of gas concentration outside the emitting (real) neuron for a single source (solid line) and dispersed sources (dotted line).
5.4 Extensions to the Basic GasNet I: The Plexus Model

In this section we introduce a GasNet variant, the plexus model, directly inspired by the type of signaling seen in the mammalian cerebral cortex as described earlier in Section 4. Recall that the NO signal is generated by the combined action of many fine NO-producing fibers, producing a targeted cloud, which is distant from the neurons from which the fiber plexus emanates. Figure 2 shows how NO derived from small and well-separated individual sources can sum to produce an effective NO cloud.

This method of signaling has several interesting implications for the spatiotemporal nature of the ensuing volume signal, making it very different from a signal generated by a single neuron of the same size (the inspiration for the basic GasNet). Section 4 showed that the summation of NO from several separated fibers gives a smoothed flat concentration distribution, with the above threshold concentration part extending over a wider area. Figure 3 illustrates the phenomenon whereby the whole volume affected by the cloud suddenly goes above threshold and is “turned on.”

What, though, if anything, do these features bring to evolved artificial nervous systems? In an attempt to answer this question, we developed the plexus GasNet, whose diffusion properties are modified so as to produce an abstraction of the type of signal produced by plexus structures. Firstly, we changed the spatial distribution of gas concentration. In the original GasNet this was modeled as an exponentially decaying function (Equation 3), which is loosely based on the type of spatial distribution of NO one would see outside a single neuron (Figure 4b). For the plexus model this has been modified to a uniform distribution over the affected volume

\[
C(d, t) = \begin{cases} 
0.5 \times T(t), & d < r \\
0, & \text{else} 
\end{cases} 
\]  

(Equation 7)

[T(t) refers to the function in Equation 4], with a peak concentration half that of the original (illustrated in Figure 4a).

The second change is to allow the center of this gas diffusion cloud to be distant from the controlling node (which, by analogy, is the source of the plexus). Note that this model requires two extra parameters for the gas diffusion center coordinates \((x, y)\). Thus the plexus model produces constant concentration within the area of effect, which can be centered anywhere in the space (Figure 5). All other details of the models are identical to the original GasNet model, as described earlier.

5.5 Extensions to the Basic GasNet II: The Receptor Model

An aspect of biological neuronal networks that has no analogue in the vast majority of ANNs is the role of receptor molecules. All neural signaling is mediated by a diverse group of proteins, which act as receptors to which neurotransmitters bind. The act of binding triggers chemical processes that result in functional changes to the neuron involved [12, 45]. In classical synaptic neurotransmission two basic classes of receptors have been identified: ionotropic and metabotropic. Ionotropic receptors are linked directly to ion channels in the postsynaptic membrane. These channels are opened or closed in response to transmitter binding, thus changing the postsynaptic membrane potential and hence mediating the postsynaptic electrical response. This type of receptor is generally involved in rapid-time-scale effects acting over milliseconds. Metabotropic receptors are not directly linked to ion channels, but affect them by the activation of intermediate G-proteins [45]. G-proteins can interact directly with ion channels or with effector enzymes that give rise to intracellular second messengers that lead to complex biochemical signaling cascades, most of which are as yet poorly understood. Hence they can give rise to a wide range of modulatory effects that act over time scales ranging from seconds to hours or even months and years. The picture is significantly complicated by the fact that a single transmitter can activate both classes of
receptors at a single site. As has already been stated, non-classical transmitters, such as NO, are not confined to act at localized synaptic sites, but diffuse freely. Accordingly, NO receptors are not membrane associated and can have a wide spatial distribution, so that they can be found anywhere in the nerve cell. NO triggers a variety of modulations through second messenger pathways that have the potential to interact in even more complex ways because of its spatially extended action.

Although neuroscience is a long way from a full understanding of receptor mechanisms, especially those involved in indirect modulation by second messenger intracellular pathways, there are a number of powerful systems-level ideas we can abstract and incorporate into our ANNs. This we have done with the second new GasNet variant: the receptor model, again taking inspiration directly from contemporary neuroscience.

Its details are similar to those of the basic GasNet, except there is now only one virtual gas, and each node in the network can have one of three discrete quantities (zero, medium, maximum) of each of $N$ possible receptors. Each diffusing neurotransmitter-receptor pairing gives rise to a separate modulation to the properties of the node. The strength of a modulation at node $i$ at time $n$, $\Delta M_i^n$, is proportional to the product of the gas concentration $C_i^n$ at the node, and the relevant receptor quantity $R_j$:

$$\Delta M_i^n = \rho_i C_i^n R_j$$  

(8)

Each modulation makes some change to one or more function parameters of the node. All the variables controlling the process are again set for each node by an evolutionary search algorithm.

Figure 5. An example plexus architecture network. The node plane is shown on the left, with the positions and connections of the network nodes, while the camera on the right shows the position of the visual inputs (see Section 6). Node 6 has a dispersed gas cloud centered in the top right of the network plane, with a uniform concentration over the area of effect, illustrating the effects of the plexus model. Thus node 6 can easily affect nodes that are far from its position in the node plane.
In the original GasNet, any node that was in the path of a diffusing transmitter would be modulated in a fixed way. The receptor model allows site-specific modulations, including no modulation (zero quantity of receptors) and multiple modulations at a single site. This provides a powerful context-switching mechanism that pulls the chemical and electrical processes further apart, allowing (but not forcing) looser coupling, while further increasing the potential for complex network dynamics. A number of different receptor linked modulations have been experimented with, including:

- **Action of receptor1**: Increase gain of node transfer function as in original GasNet.
- **Action of receptor2**: Decrease gain of node transfer function as in original GasNet.
- **Action of receptor3**: Increase proportion of retained node activation from last time step (i.e., treat node as a leaky integrator in which the time constant can be modulated upwards).
- **Action of receptor4**: If above a threshold, switch transfer function of node for sustained period (i.e., fundamentally change transfer function, for instance from a sigmoid to a constant output or a periodic function).

Note the first two modulations are immediate and short-lived, while the last two operate over a longer time scale. Each possible subset of these receptors proved to be at least as evolvable (in terms of speed to a very good solution) as the original GasNet, while some were significantly better. A variant that proved particularly successful used receptor1 only. This is the model that will be referred to as the *receptor GasNet* in the following sections on the comparative studies of the evolvability of different types of GasNet.

### 6 Comparative Experiments

Although most of the GasNet variants described in this article have been successfully used in a number of robotic tasks, their evolvability and other properties were thoroughly compared on a robotic visual discrimination task. Starting from an arbitrary position and orientation in a black-walled arena, a robot equipped with a forward-facing camera must navigate under extremely variable lighting conditions to one shape (a white triangle) while ignoring the second shape (a white square). The relative position of the shapes varied from trial to trial, as did their size, within ±10% in both dimensions. This task has been used before in detailed comparisons between the basic GasNet and other styles of ANN [28]; hence it is appropriate to use it in this comparison between GasNet variants. Because of the noise and variation and the robot’s limited sensory capabilities, this task is quite challenging in this setup. Both the robot control network (one or other form of GasNet) and the robot sensor input morphology (i.e., the number and position of the input pixels on the visual array) were under evolutionary control. This is illustrated in Figure 6. The fitness over a single trial was taken as the fraction of the starting distance moved towards the triangle by the end of the trial period, and the evaluated fitness was returned as the weighted sum of 16 trials of the controller from different initial conditions:

\[
F = \frac{2}{N(N+1)} \sum_{i=1}^{N} i \left(1 - \frac{D^F_i}{D^S_i}\right) 
\]

where \(D^F_i\) is the distance to the triangle at the end of the \(i\)th trial, and \(D^S_i\) the distance to the triangle at the start of the trial, and where the \(N\) trials are sorted in descending order of \(D^F_i\). Thus good trials, in which the controller moves some way towards the triangle, receive a smaller weighting than bad trials, encouraging robust behavior on all 16 trials. Success in the task was taken as an evaluated fitness of 1.0 over 30 successive generations of the evolutionary algorithm. Evaluations took place.
using a validated minimal simulation of the robot as described in [29]. Controllers developed in the simulation were successfully transferred to reality, generating behaviors in the actual physical robot at least as well as in the simulation. The noisy lighting conditions, varying positions and sizes of the shapes, and other properties of the simulation meant that highly robust solutions developed, generalized to the variations experienced during evolution. For further information on the task and robot see [28].

6.1 The Evolutionary Search Algorithm
A geographically distributed asynchronous updating evolutionary algorithm was used, with a population size of 100 arranged on a $10 \times 10$ grid. Parents were chosen through rank-based
roulette-wheel selection on the mating pool consisting of the eight nearest neighbors to a randomly chosen grid point. A mutated copy of the parent was placed back in the mating pool using inverse rank-based roulette-wheel selection. In what follows, a generation in such an algorithm occurs every 100 reproduction events. For full details see [28].

6.2 The Solution Representation and Mutation Operators
The robot controllers were encoded as a variable-length string of integers, with each integer allowed to lie in the range \([0, 99]\). Each node in the network was coded for by a number of parameters controlling such properties as node positions on the 2D grid in which GasNets operate, electrical connectivity, whether or not the node has sensor input, and all gas diffusion and modulation variables. Connections were formed as in Figure 8, with each node connecting to nodes lying within one of two connection segments. Hence each genotype consists of \(N\) blocks of \(P\) integers coding for the properties of the nodes, where \(N\) is the number of nodes in a particular network (this varies from genotype to genotype) and \(P\) is the number of parameters describing a node (19 for the original GasNet, 21 for the plexus and receptor versions).

Three mutation operators were applied to solutions during evolution. Each integer in the string had a probability (4%) of mutation in a Gaussian distribution around its current value. There was also an addition operator, with a 4% chance per genotype of adding one neuron to the network by inserting a block of random values describing each of new node’s properties. Finally there was a deletion operator, with a 4% chance per genotype of deleting one randomly chosen neuron from the network. In the next section, we describe the speed-of-evolution results for the three models.

7 Speed-of-Evolution Results
Table 1 shows the speed-of-evolution results for the three GasNet variants. Forty runs were carried out for each version, with runs being terminated once controllers were evolved that achieved 100%

![Figure 8](image-url)
fitness over 30 consecutive generations. In all cases successful networks have typically 8–15 nodes with 2–4 visual inputs. GasNet controllers are very lean, in terms of numbers of nodes and connections, in comparison with previously evolved solutions using other styles of ANN [28]. Here we see that the plexus and receptor models evolve good solutions significantly faster than the original GasNet model. The receptor model gives particularly dramatic improvements. During the course of a typical evolutionary run, the original and plexus GasNet fitnesses tended to rise in jumps following periods of stasis, whereas the receptor GasNet fitness tended to rise steadily to a perfect score of 1.0. The question is therefore, what is it about the new features of these two models that mediates this increase? In the remainder of the article we will explore this question through an analysis of the coupling between the chemical and electrical signaling mechanisms in the networks.

8 Why the Difference: Flexible Loose Coupling?

In earlier studies the original GasNet was compared with various styles of recurrent ANNs that did not possess complex intrinsic dynamics at the node level. The much greater evolvability of the GasNets might have been related to the richer internal dynamics of the networks with multiple time scales in operation. However, the significant variation in the evolvability of the three GasNet variants studied here, with highly comparable internal dynamics at the node level, suggests that the story is more complex. This is also backed up by recent detailed comparisons of many forms of recurrent networks with rich dynamics, including GasNets and CTRNNs [8], applied to bipedal and quadrupedal locomotion [38, 37], a task that would appear to be more dynamically demanding than the one studied in this article. The original GasNet variant was found to be either more evolvable, or at least more reliable in finding good solutions quickly, than the other forms of dynamical networks used. Hence the provision of rich internal dynamics is only part of the answer.

As mentioned earlier, one of the most significant features of GasNets is the operation of two distinct, yet interacting, signaling mechanisms. An important aspect of the two new variants explored in this article is the fact that the nature of the coupling between the electrical and chemical processes is more controllable and flexible than in the original GasNet. We believe this has an important role to play in evolvability.

There is some evidence from evolutionary theory that the degree of coupling between interacting and yet distinct processes might lie at the heart of some important principles for the development of complex systems. To evolve successfully, an organism must satisfy the conflicting pressures of phenotypic stability and genetic instability, that is, the organism must be robust to phenotypic change (to not fall off the current adaptive peak) and amenable to genotypic change (to allow movement to a

Table 1. Number of generations before consistent success is achieved for the three models described earlier. Results for both plexus and receptor GasNets were significantly better than for the original GasNet. In particular, the receptor variant achieves success an order of magnitude faster. Runs not achieving consistent success by generation 10,000 were terminated.

<table>
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<tr>
<th></th>
<th>Original</th>
<th>Plexus</th>
<th>Receptor</th>
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<tbody>
<tr>
<td>No. of runs</td>
<td>40</td>
<td>40</td>
<td>40</td>
</tr>
<tr>
<td>No. of generations</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mean (s.d.)</td>
<td>3,042 (3,681)</td>
<td>1,579 (2,609)</td>
<td>82 (102)</td>
</tr>
<tr>
<td>Median</td>
<td>1201</td>
<td>512</td>
<td>47</td>
</tr>
<tr>
<td>Best</td>
<td>136</td>
<td>101</td>
<td>13</td>
</tr>
<tr>
<td>Worst</td>
<td>&gt;10,000</td>
<td>&gt;10,000</td>
<td>512</td>
</tr>
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</table>
new adaptive peak). Conrad [14] identifies genetic redundancy and multiple weak interaction as possible mechanisms by which these two conflicting pressures can be satisfied.

Such loosely coupled redundant systems contain the potential for genotypic change without phenotypic change; both multiple weak interactions and redundancy allow for gradual, or even neutral, transformation of function through genetic variation [14]. In such systems, phenotypic fitness is likely to be highly correlated across the genotype landscape, either through significant levels of neutrality or through low levels of ruggedness or through both. Such systems are also robust to phenotypic change; complex systems picked at random are more likely to be stable if the system is characterized by either multiply connected weakly interacting components or sparsely connected strongly interacting components [23, 35].

By contrast, strongly coupled non-redundant systems are far less amenable to variation; change in one component is more likely to affect the entire system, leading to phenotypic instability. We see this effect clearly in the theoretical NK fitness landscapes, where a higher degree of epistatic connection between the components leads to a less correlated fitness landscape [31]. In other words, even small changes in the genotype in a strongly coupled system lead to large changes in the phenotype. However, in tenably neutral versions of the NK landscapes, high degrees of redundancy compensate in some measure for the strong coupling, allowing genetic variation without massive phenotypic variation [6, 39].

We hypothesize that systems involving distinct yet coupled processes are highly evolvable when the coupling is flexible (i.e., when it is easy for evolution to change the degree of coupling in the system) with a bias towards loose coupling; this allows the possibility of tuning one process against the other without destructive interference. Some evidence that GasNets are this kind of system can be found in [49], where it is shown that GasNets can re-evolve to deal with a changed time scale much faster than more standard electrical-connection-only networks. Here we present further evidence of a different kind.

As described earlier, the plexus model allows network nodes to emit gas from anywhere in the grid. This partly separates the gas diffusion and the electrical synaptic activity mechanisms; synaptic connections are formed from the current node position, while gas diffusion connections are formed from the gas emission position. Thus gas connections in the grid can be changed through modifying the gas emission position, while synaptic connections can be altered through moving the node itself.

Similarly, the addition of receptors to mediate the modulatory effects of the virtual gas potentially allows even more independence between electrical and chemical signaling. This is because, as explained in Section 5.5, the receptor GasNet used in the comparative experiments had only one type of receptor; its presence or absence at a node in the network essentially acts as a switching mechanism turning on and off modulation at the node.

There is no simple way of calculating the degree of coupling in the three forms of network. In principle one can measure the degree of ruggedness through correlation lengths or similar methods. However, Smith et al. [48] show that these types of measures do not discriminate well between such highly heterogenous problem spaces as those found here. In this section, we introduce a number of simple, and admittedly incomplete, measures of the degree of coupling between the gas diffusion and electrical synapse mechanisms.

The first of these involves calculating the two connectivity matrices (electrical and chemical) for a given successful GasNet, and computing the coupling as the number of overlapping connections, that is, of elements that are nonzero in both connectivity matrices. Table 2 shows this coupling between the electrical and gas diffusion processes for the three models. The numbers of electrical synaptic connections and gas diffusion connections (averaged per neuron), and the percentage of overlapping connections, are shown for each GasNet variant. The values shown were calculated by averaging over the best evolved controllers from each of the successful runs. Three points can be made. First, there are no significant differences between the numbers of electrical synaptic connections across the three models. Second, the percentages of overlapping connections in the GasNet are significantly higher.

1 Note that the two mechanisms are not entirely separated: Both act on the actual position of the destination nodes.
than those in the receptor and plexus models; thus indicating that coupling between the electrical and diffusion processes is far stronger in the GasNet model than in the receptor and plexus models and may provide part of the reason for the faster evolutionary search. Third, the number of diffusion connections is significantly lower in the receptor GasNets. This last fact suggests that the receptor mechanism is being used to shape leaner networks with fewer, more specific gas connections.

However, this method of measuring the coupling of the two signaling systems does not take account of the actual action of the network. For instance, a gas or electrical connection is registered regardless of whether the neuron emitted gas or was electrically active, respectively. To remedy this, we examined the online coupling by measuring the overlap between the electrical and gaseous activity matrices (denoted by \( E \) and \( G \), respectively) at each time step during a run of the robot. These matrices are generated by setting \( G_{ij} \) (or \( E_{ij} \)) = 1 if the amount of gas or total electrical activity (i.e., excitatory activity minus inhibitory activity, including self-recurrency) at node \( i \) due to node \( j \) at a given time step \( t \) is nonzero. \( G_{ij} \) (or \( E_{ij} \)) = 0 otherwise. In addition, for the gas matrix only, \( G_{ij} \) is set to zero if there is no electrical activity at node \( j \) at that time step, since in its absence the gas would be ineffectual in influencing electrical activity at the node. For the receptor GasNet there must also be a nonzero number of receptors associated with node \( j \) for \( G_{ij} \) to be set to one. The amount of overlap between the two matrices at each time step (i.e., the number of corresponding nonzero elements) is a measure of the online coupling between the electrical and chemical mechanisms. This value is averaged over all time steps during 16 runs of the robot with random starting conditions to give the online coupling value for a given network.

As can be seen from Table 3, where the measure is compared for the three GasNet variants, the online coupling gives a lower value than that generated from the static connectivity matrices (Table 2). This measure is lower for the plexus GasNet than for the original model, but higher for the receptor model. This may indicate that the receptor GasNets, with fewer gas connections, have more highly tuned architectures where the connections are used more frequently, giving rise to the higher value. The best that can be said is that this measure is rather inconclusive.

While the online connectivity coupling measure described above gives an indication of the functional coupling of a network, we have hypothesized that flexible loose coupling is useful in an evolutionary context. To investigate this further we must, therefore, look at the mutants of evolved networks rather than just the networks themselves. In particular, if we are to suppose that a loose coupling between the two systems is beneficial, then we might expect that the distribution of fitnesses of mutations that affected either chemical or electrical signaling systems independently would be different. This is indeed the case, as can be seen in Figures 9 and 10, where we have compared, for 10 successful GasNets of each type, the fitnesses of all possible one-point mutants in which either the gas connectivity or the electrical connectivity matrix has been changed independently, or both matrices have been changed. Mutants were created by generating each possible single-point mutation of the genomes of the successful GasNets. What is clear is that for each style of network, mutations

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<tr>
<td>No. of successful runs</td>
<td>33</td>
<td>37</td>
<td>40</td>
</tr>
<tr>
<td>Synaptic connections (s.d.)</td>
<td>1.89 (0.52)</td>
<td>1.72 (0.41)</td>
<td>1.85 (0.42)</td>
</tr>
<tr>
<td>Diffusion connections (s.d.)</td>
<td>2.27 (0.93)</td>
<td>2.78 (0.84)</td>
<td>1.02 (0.56)</td>
</tr>
<tr>
<td>Overlapping connection coupling (s.d.)</td>
<td>40.5% (13.2%)</td>
<td>10.8% (8.1%)</td>
<td>12.32% (5.26%)</td>
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that change the gaseous connections only have superior average fitness (Figure 9) and a distribution most biased towards high fitnesses (Figure 10), while those mutants that change both types of connectivity are most detrimental, indicating destructive interference between the two mechanisms.

Given that the properties of mutants that affect the signaling systems independently differ among the three network search spaces, in light of the difference in evolutionary speeds, the natural question to ask next is whether the distribution of these independent mutations is different for the spaces. Examining the average number of mutations as a fraction of the total number of mutations for all the one-point mutants that changed either one or other or both connectivity matrices, we do see differences, as shown in Figure 11. While both the total proportion of mutants that affect connectivity matrices at all, and the proportion affecting electrical connections only, are very similar for all three spaces, the proportion affecting the gaseous signaling system only (which have higher average fitness) is significantly greater for the plexus and receptor GasNet spaces relative to the proportion of destructive mutations that affect both systems. In the original GasNet the proportion of these two types of mutants is the same. This means that the receptor and plexus variants are less likely to suffer deleterious mutations. When we add to this the fact that receptor GasNet gas-only mutants have a higher average fitness than their plexus GasNet counterparts (Figure 9) and have

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<td>2.78 (0.84)</td>
<td>1.02 (0.56)</td>
</tr>
<tr>
<td>Online connection coupling (s.d.)</td>
<td>5% (7.5%)</td>
<td>1.3% (3.1%)</td>
<td>6.12% (5.39%)</td>
</tr>
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Table 3. A measure of online coupling in the original GasNet and plexus models. For each of the successfully evolved controllers, the number of electrical synaptic connections and number of gas diffusion connections are shown (averaged per neuron). The percentage of online connections that overlap is also shown. Standard deviations in parentheses. See text for further details.

Figure 9. Mean fitnesses of one-point mutants of 10 evolved original, plexus, and receptor GasNets. For all styles of network, all possible one-point mutants of the original successful evolved genotypes were exhaustively generated. The mutants were then divided into three groups: those whose electrical connectivity matrices are altered by the mutation, relative to the original genotype, but whose gaseous connectivity matrices are unchanged (labeled “Elec”), those whose gaseous connectivity matrices are altered but whose electrical connectivity matrices are unchanged (labeled “Gas”), and those in which both electrical and gaseous connectivity matrices are altered (labeled “Both”). Mutants where there is no change in either connectivity matrix are ignored for the purposes of this analysis. Electrical connectivity matrices are generated in the standard way; elements $G_{ij}$ of the gaseous connectivity matrices are generated by calculating the maximum concentration that could be experienced at node $j$ due to node $i$. Each mutant network was then evaluated five times to allow for noise, and the mean mutant fitnesses for the subgroups of each evolved network calculated. The figure shows the means over the 10 networks, with error bars showing standard deviations. Note the repeated pattern across all network variants: high mean fitness of “Gas” mutants and the low mean fitness of mutants where both connectivity matrices are changed.
their distribution of fitnesses biased more heavily towards high scores (Figure 10), we can start to see why, under the guidance of a selection mechanism that favors fitter individuals, the receptor GasNets are the most evolvable. Selection is able to exploit the greater proportion of fitter (or at least less deleterious) mutants.

These measures all point towards the benefit of systems with loosely coupled distinct processes that can be (flexibly) tuned against each other. Here the picture emerging is of tuning the gas mechanisms against the electrical networks, which can be done more easily in a nondestructive, beneficial way in the less coupled plexus and receptor GasNets.

9 Conclusions

The results on degree of coupling and speed of evolution presented in this article support our view that systems involving distinct yet flexibly coupled processes are highly evolvable when there is a bias

Figure 10. Distributions of fitnesses of one-point mutants of 10 evolved original, plexus, and receptor GasNets. Each row compares distributions for different mutant subclasses of the three styles of network: (a) mutants in which the mutation altered both gaseous and electrical connectivity matrices; (b) mutants in which the mutation altered electrical connectivity matrices only; (c) mutants in which the mutation altered gaseous connectivity matrices only. See the caption of Figure 9 for more details. Distributions shown as proportions of total number of one-point mutants. For all styles of network, mutations that affect gas connectivity only have a distribution that has a lighter tail (fewer low fitnesses) than the other groups. This is particularly marked in the receptor case, where there are practically no mutants with a fitness less than 0.6.
towards loose coupling between the processes; this allows the possibility of evolution tuning one
against the other without destructive interference. The receptor model, in which the search process
arguably has the most direct control over the degree of coupling, is seen to be far the most
evolvable in terms of consistent speed to very good solutions. Indeed, preliminary experiments on
extended versions of the shape discrimination task, involving more shapes and two-stage discrimi-
nations, have proved highly successful with the receptor model. The one-point mutant studies only
really address evolvability at high fitnesses, since the mutants were generated from already successful
individuals. A fuller (and very time consuming) study will repeat this kind of analysis at intervals
throughout the entire evolutionary history.

This article marks a first step in our attempts to gain deeper insights into the importance, or
otherwise, of the coupling issue. As well as exploring the use of our artificial nervous systems for
generating more complex behaviors, we are trying to build a formal framework to extend our
theoretical understanding. In this we have some considerable distance to go. Although we have
concentrated on changes (to plastic systems) over an evolutionary time scale, very similar issues are
likely to be important at the time scale of the plastic changes themselves.

Of course, there are many other forms of plasticity in real neuronal networks and many other
potential principles to be abstracted [17, 34], but we believe that explicitly dealing with the electro-
chemical nature of nervous systems is likely to be an increasingly fruitful area of research that will
force us to broaden our notions of what behavior-generating mechanisms might look like [53].

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