Multi-epoch Doppler tomography and polarimetry of QQ Vul

Axel D. Schwope, Maria S. Catalán, Klaus Beuermann, André Metzner, Robert Connon Smith and Danny Steeghs

1 Astrophysikalisches Institut Potsdam, An der Sternwarte 16, 14482 Potsdam, Germany
2 Keele University, Department of Physics, Keele, Staffordshire ST5 5BG
3 Universitätsternwarte Göttingen, Geismarlandstrasse 11, D-37083 Göttingen, Germany
4 Max-Planck-Institut für Extraterrestrische Physik, Karl-Schwarzschild-Strasse 1, D-85748 Garching, Germany
5 Astronomy Centre, School of CPES, University of Sussex, Falmer, Brighton BN1 9QJ
6 University of St. Andrews, School of Physics and Astronomy, North Haugh, St Andrews, Fife KY16 9SS

Accepted 1999 November 11. Received 1999 September 6; in original form 1999 March 25

ABSTRACT

We present multi-epoch high-resolution spectroscopy and photoelectric polarimetry of the long-period polar (AM Herculis star) QQ Vul. The blue emission lines show several distinct components, the sharpest of which can unequivocally be assigned to the illuminated hemisphere of the secondary star and used to trace its orbital motion. This narrow emission line can be used in combination with NaI absorption lines from the photosphere of the companion to build a stable long-term ephemeris for the star: inferior conjunction of the companion occurs at HJD = 244 8446 ± 5

The polarization curves are dissimilar at different epochs, thus supporting the idea of fundamental changes of the accretion geometry, e.g., between one- and two-pole accretion modes. The linear polarization pulses display a random scatter by 0.2 phase units and are not suitable for the determination of the binary period. The polarization data suggest that the magnetic (dipolar) axis has a colatitude of 23°, an azimuth of −50°, and an orbital inclination between 50° and 70°.

Doppler images of blue emission and red absorption lines show a clear separation between the illuminated and non-illuminated hemispheres of the secondary star. The absorption lines on their own can be used to determine the mass ratio of the binary by Doppler tomography with an accuracy of 15–20 per cent. The narrow emission lines of different atomic species show remarkably different radial velocity amplitudes: $K = 85–130 \text{ km s}^{-1}$. Emission lines from the most highly ionized species, HeII, originate closest to the inner Lagrangian point $L_1$. We can discern two kinematic components within the accretion stream; one is associated with the ballistic part, and the other with the magnetically threaded part of the stream. The location of the emission component associated with the ballistic accretion stream appears displaced between different epochs. Whether this displacement indicates a dislocation of the ballistic stream, e.g. by a magnetic drag, or emission from the magnetically threaded part of the stream with near-ballistic velocities, remains unsolved.

Key words: accretion, accretion discs – line: profiles – polarization – stars: individual: QQ Vul – novae, cataclysmic variables.

1 INTRODUCTION

QQ Vul was discovered with the HEAO-1 low-energy detectors in the 0.15–0.5 keV band and catalogued by Nugent (1983).

* E-mail: aschwope@aip.de
† Visiting astronomer, German-Spanish Astronomical Center, Calar Alto, operated by the Max-Planck-Institut für Astronomie, Heidelberg, jointly with the Spanish National Commission for Astronomy.

Spectroscopic, photometric, and polarimetric observations by Nousek et al. (1984) immediately following its detection led to the classification of this object as an AM Her type cataclysmic variable (or ‘polar’) with an orbital period of 222.5 min. Nousek et al. found that the centroids of the prominent blue emission lines showed a huge systemic velocity, $\gamma \sim 500 \text{ km s}^{-1}$, when fitted with a circular orbit velocity equation, $v = K \sin 2\pi (\phi - \phi_0) + \gamma$.

An extensive observational study using X-ray (EXOSAT), UV (IUE), and optical spectroscopy and photometry was presented in...
Osborne et al. (1986) and Mukai et al. (1986). They found pronounced dips in the soft X-ray light curve caused by photoelectric absorption in the magnetically confined stream (out of the orbital plane). In addition, their spectroscopy revealed a systemic velocity $\gamma$ compatible with zero, indicating substantial changes in the line-emitting region with respect to the Nousek et al. (1984) results. They also identified a narrow emission-line component (`peak 2'), which they associated with the heated surface of the secondary star.

In the same year, McCarthy, Bowyer & Clarke (1986) presented their analysis of moderate-resolution, phase-resolved spectroscopy obtained in a state of reduced accretion. They identified a number of narrow emission lines, and tentatively assigned one of them to the illuminated part of the secondary. Surprisingly, they found a stationary emission-line component at redshift $z \simeq 0.05$, which remained largely unexplained.

In 1986, Mukai & Charles detected the secondary star in near-infrared spectra of QQ Vul and, in 1987, the same authors were able to trace the Na I $\lambda \lambda 8183/94$ doublet around the orbital cycle. Their data provided the first secure measurement of inferior conjunction of the companion star.

EXOSAT observations of QQ Vul showed substantial changes of the X-ray light curve, which were tentatively interpreted by Osborne et al. (1987) as changes between a simple one-pole geometry and a more complex two-pole geometry. This scenario has been supported by Beardmore et al. (1995) using more recent ROSAT X-ray observations.

The lack of an ephemeris with sufficient accuracy hampers the unique interpretation of all the data collected in the past. In this paper we will present an accurate spectroscopic ephemeris using both narrow emission lines from the illuminated hemisphere of the secondary star and photospheric absorption lines observed on several occasions between 1986 and 1993. We show that both features are equally well suited for tracing the secondary. Our new spectroscopic ephemeris replaces older ones which were built using the recorded times of linear polarization pulses or cross-correlations of optical light curves. We will show that the linear polarization pulses may occur at random phase (within a certain interval), and are therefore not suitable for the derivation of the binary period.

We also present the results of polarimetric observations obtained between 1985 and 1988. These data are discussed in conjunction with the spectroscopic observations in order to establish a consistent picture of the accretion geometry of QQ Vul. Previous polarimetry was presented by Nousek et al. (1984) and by Cropper (1998), who derived the orbital inclination to be $46^\circ < i < 74^\circ$ and $i = 40^\circ-50^\circ$, respectively.

This paper concentrates mainly on the analysis of the blue emission lines; in the companion paper (Mapping the secondary star in QQ Vul) by Catalán, Schwope & Smith (1999, hereafter Paper I) we present a detailed analysis of the absorption and emission lines in the red spectral regime. Preliminary results were presented in Catalán et al. (1996) and in Schwope et al. (1998, 1999).

2 OBSERVATIONS

2.1 High-resolution spectroscopy

QQ Vul was observed between 1986 and 1993 using the 2.2-m telescopes at La Silla and Calar Alto with Boller & Chivens Cassegrain spectrographs, with the Calar Alto 3.5-m telescope equipped with the Cassegrain double-beam spectrograph TWIN, and with the 4.2-m William Herschel telescope (WHT) at La Palma equipped with the double-beam spectrograph ISIS. All the blue spectra covered the approximate wavelength range 4200–5000 Å, where H-Balmer and helium emission lines are prominent. The red spectra were centred on the Na I doublet at $\lambda \lambda 8183/8194$ Å. Full phase-coverage was achieved on all occasions. Some details of the spectroscopic observations are given in Table 1. All observations were performed under good weather conditions, flat-field, bias, dark, and arc line spectra were taken frequently, and spectra of spectrophotometric standard stars were taken on each of the observing nights. We estimate the photometric accuracy of our spectra to be better than 30 per cent.

2.2 Photoelectric polarimetry

Polarimetric observations of QQ Vul were carried out during several nights in 1985, 1987 and 1988 using the two-channel photometer/polarimeter of the DSAZ (Proetel 1978) mounted on the 2.2-m telescope at Calar Alto. In addition, a rather short (2-hr) observation covering just one linear polarization pulse was carried out in 1987 November at the 2.2-m telescope at La Silla using the ESO polarimeter PISCO (Stahl et al. 1986). Most observations were done in unfiltered (white) light; hence the spectral bandpass was limited by the atmospheric cut-off and the sensitivity of the photomultipliers to $\sim 3400–8500$ Å. An observation log is given in Table 2. The sky was monitored regularly, allowing

Table 1. Log of spectroscopic observations of QQ Vul.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>86/10/14-20</td>
<td>LS22</td>
<td>B&amp;C+RCA</td>
<td>3</td>
<td>4180–5050</td>
<td>600</td>
<td>31</td>
<td></td>
</tr>
<tr>
<td>86/10/18</td>
<td>LS22</td>
<td>B&amp;C+RCA</td>
<td>1.5</td>
<td>4540–4960</td>
<td>625</td>
<td>10</td>
<td></td>
</tr>
<tr>
<td>88/06/10-12</td>
<td>CA22</td>
<td>B&amp;C+RCA</td>
<td>3</td>
<td>4150–5050</td>
<td>720/500</td>
<td>22</td>
<td></td>
</tr>
<tr>
<td>91/07/08-10</td>
<td>CA35</td>
<td>CTS+RCA2</td>
<td>1.7</td>
<td>4400–4940</td>
<td>660–720</td>
<td>38</td>
<td></td>
</tr>
<tr>
<td>91/07/08-10</td>
<td>CA35</td>
<td>CTS+GEC</td>
<td>2.2</td>
<td>7550–8800</td>
<td>660–720</td>
<td>36</td>
<td></td>
</tr>
<tr>
<td>93/08/23-26</td>
<td>WHT42</td>
<td>ISIS+Tek1</td>
<td>1.5</td>
<td>4230–5010</td>
<td>300</td>
<td>64</td>
<td></td>
</tr>
<tr>
<td>93/08/23-26</td>
<td>WHT42</td>
<td>ISIS+EEV3</td>
<td>0.7</td>
<td>7940–8380</td>
<td>300</td>
<td>64</td>
<td></td>
</tr>
</tbody>
</table>

$^a$LS: La Silla, CA: Calar Alto, WHT: William Herschel Telescope La Palma; numbers following the observatory code denote the aperture diameter in units of 10 cm.

$^b$Instrument codes: B&C – Boller & Chivens spectrograph, CTS – Cassegrain Twin Spectrograph, ISIS – Intermediate-Dispersion Spectroscopic and Imaging System, the abbreviations following the instrument code denote the CCD chip used.

sky-subtraction from object measurements after fitting polynomials to the sky measurements.

Using the DSAZ polarimeter, the incoming signal is modulated by a rotating quarter-wave or half-wave plate, for the detection of circular (CP-mode) and linear polarization (LP-mode), respectively. In the CP-mode a linearly polarized signal can also be detected, but with reduced efficiency.

3 ANALYSIS

3.1 Spectroscopic ephemeris of the secondary star

The orbital mean spectrum of our 1993 observations (blue spectral range) is shown in Fig. 1. The mean spectra obtained on the other occasions look very similar to that shown in the figure, though at a somewhat different brightness level. QQ Vul displays the typical features of an AM Herculis star in a high accretion state: a strong line of ionized helium He\textsc{ii} λ4686, an inverted Balmer decrement, asymmetric variable lines with line wings extending to \( \sim 2000 \, \text{km s}^{-1} \), and a pronounced Bowen blend of C\textsc{iii}/N\textsc{iii}-lines between 4635 and 4650 Å.

Individual emission lines consist of several components with different radial velocity amplitudes and different brightness variations. To give an example, we show in Fig. 2 a grey-scale representation of the phase-folded, continuum-subtracted trailed spectrogram of the He\textsc{ii} λ4686-line (1991 observations). The ephemeris used for phase-binning is that given in equation (1). The trailed blue emission-line spectrogram is shown together with a trailed, continuum-subtracted spectrogram of the Na\textsc{i} absorption line doublet recorded simultaneously. These red spectra are fully analysed in the accompanying Paper I, and are shown here to facilitate the interpretation of the blue spectra.

The profile of the He line generally shows great similarity to those displayed in HU Aqr in its high accretion state (Schwope, Mantel & Horne 1997). The most pronounced feature is a narrow emission line (NEL) with rather low velocity amplitude. It moves parallel to the Na absorption lines, while its brightness is anticorrelated with those of the absorption lines. The latter are bright at inferior conjunction (blue-to-red zero crossing of the lines), and the NEL is bright at superior conjunction. The NEL clearly has a much lower radial velocity amplitude than the absorption lines. Both the different brightness variation and the different radial velocity amplitude suggest that the two spectral features originate mainly from opposite hemispheres of the secondary star. This is demonstrated clearly by a combined Doppler map of both lines shown in Fig. 3. The underlying broader features in the He\textsc{ii} emission line complex with higher radial velocity amplitudes must then have their origin somewhere in the accretion stream. They will be investigated in Section 3.3.4. Here we concentrate on the NEL, which obviously originates somewhere on the donor star.

We cannot confirm the finding by McCarthy et al. (1986) of a stationary narrow emission component at a velocity of \( \sim 500 \, \text{km s}^{-1} \).

The He\textsc{ii} λ4686 emission lines in all our spectra obtained during different years were fitted by two or three Gaussians in order to separate the NEL from the stream emission. This was unequivocally possible only in the phase interval 0.25–0.60; at other phases the NEL is too faint to be clearly detected, or strongly blended with another relatively sharp underlying component (around phases \( \sim 0.2 \) and \( \sim 0.7 \)). The centroid positions of the NEL were then fitted assuming a circular orbit velocity equation \( v = \gamma + K \sin 2\pi(t - t_0)/P \) with fixed period \( P \).

Similarly, the Na\textsc{i} absorption lines were fitted by a double Gaussian with a fixed peak separation and the same linewidths.

Table 2. Photoelectric polarimetry of QQ Vul.

<table>
<thead>
<tr>
<th>Date [Y/M/D]</th>
<th>Tel.</th>
<th>Instr.</th>
<th>Mode</th>
<th>Filter</th>
<th>( T_{\text{int}} ) [s]</th>
<th>( T_{\text{tot}} ) [hr]</th>
</tr>
</thead>
<tbody>
<tr>
<td>85/06/11</td>
<td>CA22</td>
<td>ZPP</td>
<td>CP</td>
<td>WL/RG630</td>
<td>60</td>
<td>3.9</td>
</tr>
<tr>
<td>85/06/12</td>
<td>CA22</td>
<td>ZPP</td>
<td>LP</td>
<td>WL</td>
<td>72</td>
<td>4.1</td>
</tr>
<tr>
<td>87/06/25-27</td>
<td>CA22</td>
<td>ZPP</td>
<td>CP</td>
<td>WL</td>
<td>100</td>
<td>8.2</td>
</tr>
<tr>
<td>87/09/04</td>
<td>LS22</td>
<td>PISCO</td>
<td>LP</td>
<td>WL</td>
<td>130</td>
<td>2.0</td>
</tr>
<tr>
<td>88/06/14+16</td>
<td>CA22</td>
<td>ZPP</td>
<td>LP</td>
<td>WL</td>
<td>60</td>
<td>5.0</td>
</tr>
<tr>
<td>88/06/15</td>
<td>CA22</td>
<td>ZPP</td>
<td>CP</td>
<td>WL</td>
<td>60</td>
<td>4.2</td>
</tr>
</tbody>
</table>

\( ^a \) For coding of telescopes see Table 1.
\( ^b \) ZPP: two-channel photometer/polarimeter, PISCO: Polarimeter for Instrumental and Sky polarization Compensation.
\( ^c \) CP: circular polarimetry, LP: linear polarimetry.

Figure 1. Orbital mean blue spectrum of QQ Vul in 1993 August.
Again the resulting radial velocities were fitted by a circular orbit velocity equation, and the values given in Paper I are quoted here. Ellipsoidal fits gave smaller residuals than the straight sine fits (Paper I); the influence on the times \( t_0 \) of zero crossing, however, is negligible. We compile the results for all fit parameters in Table 3, and include also those found in the literature (Mukai & Charles 1987, Na\( i \) measurement).

Linear regressions for the times of blue-to-red zero crossing were performed for the emission and the absorption features. They yielded identical results within the errors. The weighted linear regression for the combined Na\( i \) and He\( ii \) lines yields

\[
T_0(\text{HJD}) = 244\,844,471.05 + E \times 0.154,520,11 \quad (1)
\]

(the numbers in brackets are the uncertainties in the last digits). The epochs defined by integer numbers of \( E \) are regarded as epochs of inferior conjunction of the secondary star in QQ Vul. All phases in both papers refer to the ephemeris of equation (1). The residuals of several features recorded around the orbital cycle, such as radial velocity zero crossings, centres of linear polarization pulses, and X-ray absorption dips, are plotted in Fig. 4 with respect to equation (1). This diagram shows the good agreement of the NEL zero crossings with Na\( i \) absorption-line zero crossings. It shows furthermore that the ‘peak 2’ component of Mukai et al. (1986), which was suspected to originate from the secondary star, has nothing in common with the NEL from the companion investigated here. In addition, it shows the variability of the phase of the X-ray absorption dip (the bars in the diagram denote the duration of that feature, not the phase error), and it shows, finally, that the linear

![Figure 2](http://mnras.oxfordjournals.org/)  
**Figure 2.** Trailed spectrograms of the simultaneously recorded He\( ii \) \( \lambda \)4686 emission and Na\( i \) \( \lambda \lambda \)8183/94 absorption lines of QQ Vul (1991 observations). The original spectra were continuum-subtracted and phase-folded according to the final ephemeris of equation (1). All data are shown twice for clarity.

![Figure 3](http://mnras.oxfordjournals.org/)  
**Figure 3.** Doppler image (MEM-reconstruction) of the He\( ii \) emission and the Na\( i \) absorption lines recorded simultaneously in 1991. The Doppler image of Na\( i \) is shown as a contour plot with iso-intensity lines at 20, 40, 60, 80 and 98 per cent of the maximum intensity. The Doppler map of He\( ii \) is shown as a grey-scale image with dynamic range between 0 and 90 per cent of maximum intensity. The overlay gives the size of a Roche lobe for a mass ratio \( Q = 1.75 \), and the \( \times \) marks the adopted centre of mass of the secondary star.
Circular polarization pulse appears at random phase between phase 0.33 and 0.50, and cannot be used to derive the orbital period.

### 3.2 Analysis of polarimetric observations

#### 3.2.1 Overall characteristics of the light and polarization curves

In Fig. 5 we show phase-averaged light and polarization curves with full phase-coverage obtained in 1985 and 1988 in white light. All data were phase-folded and averaged using the ephemeris derived in Section 3.1, where phase zero indicates inferior conjunction of the secondary star. The data obtained in 1987 are very similar to those obtained one year later, but with poorer signal-to-noise ratios (S/N). These data are therefore not discussed separately.

The 1985 data are quite similar to those published recently by Cropper (1998), and to those by Nousek et al. (1984), but show some striking differences from the 1988 data with respect to the shape of the curves and the phasing of individual features.

The light curve at all three epochs is double-humped, with primary and secondary minima separated by a half orbital cycle and the primary minimum centred around \( \phi_{\text{spec}} = 0.9 \). In 1985 June, maximum light occurred at the phase of the second hump, whereas in all later data the first hump, was stronger (see Fig. 11). The phasing of the light curve does not show dramatic changes between 1985 and 1988, quite unlike the circular and linear polarization curves which do.

#### Circular polarization

Circular polarization is almost always negative, with short excursions at low level towards positive values somewhere in the phase interval \( \phi_{\text{spec}} = 0.30–0.55 \), and shows a pronounced depression at phase \( \phi_{\text{spec}} = 0.80 \) and 0.95 in 1985 and 1988, respectively.

Linear polarization is always low, i.e., below 2–3 per cent. The curves show one distinct linear polarization maximum (pulse) per orbital cycle. It is centred at phase \( \phi_{\text{spec}} = 0.42 \) in 1985, and marks the end of the phase interval of vanishing circular polarization in that year. In 1988, the pulse occurs at \( \phi_{\text{spec}} = 0.35 \), and marks the start of the interval of positive (or vanishing) circular polarization. Not so easily recognizable in the phase-averaged representation of Fig. 5 is a second fainter linear polarization pulse at \( \phi_{\text{spec}} = 0.57 \) observed in 1988 which coincides with a second circular polarization zero crossing. The linear polarization angle displays a large scatter in 1985, whereas the variation is much smaller in 1988. Meggitt & Wickramasinghe (1982) derived a simple relation for the derivative of the polarization angle at the time of the polarization pulse for the case of a point-like emission region, \( \psi_p = \cos \iota \). The observed data do not allow us to determine a unique value for \( \psi_p \) in 1985, contrary to 1988 where \( \iota = 60^\circ \). The fact that the value of \( \psi_p \) changes during the pulse in the 1985 observation means that the emission region must have had a more complicated shape on that occasion compared with the 1988 observation.

The optical light and polarization curves of AM Herculis binaries are modulated by cyclotron beaming, eclipses by the secondary star and the accretion stream, and self-eclipses of the accretion region by the white dwarf itself. X-ray observations on different occasions using the EXOSAT satellite have shown that there is no eclipse by the secondary star (Osborne et al. 1987). The polarimetric data in 1985 were taken simultaneously with an EXOSAT observation. The combined data show clearly that the depression in the circular polarization at phase \( \phi_{\text{spec}} = 0.8 \) is due to an obscuration of the accretion spot by the intervening accretion stream. It is that part of the stream which is magnetically coupled and lifted out of the orbital plane. As has been pointed out by Cropper (1998), this requires the orbital inclination \( \iota \) to be larger than the colatitude of the accretion spot \( \delta_s \) (measured with respect to the rotation axis).

Around the phase of the X-ray and circular polarization dip the observer looks almost directly on to the accretion region (minimum angle between the line of sight and the surface normal at the accretion spot). At this viewing angle the optical flux and the circular polarization are reduced due to strong cyclotron beaming. The primary optical minimum (and circular polarization pulse) in 1988 was much shallower than in the 1985 observation. In 1988, the pulse occurs at \( \phi_{\text{spec}} = 0.42 \) in 1985, and marks the start of the interval of positive (or vanishing) circular polarization. Not so easily recognizable in the phase-averaged representation of Fig. 5 is a second fainter linear polarization pulse at \( \phi_{\text{spec}} = 0.57 \) observed in 1988 which coincides with a second circular polarization zero crossing. The linear polarization angle displays a large scatter in 1985, whereas the variation is much smaller in 1988. Meggitt & Wickramasinghe (1982) derived a simple relation for the derivative of the polarization angle at the time of the polarization pulse for the case of a point-like emission region, \( \psi_p = \cos \iota \). The observed data do not allow us to determine a unique value for \( \psi_p \) in 1985, contrary to 1988 where \( \iota = 60^\circ \). The fact that the value of \( \psi_p \) changes during the pulse in the 1985 observation means that the emission region must have had a more complicated shape on that occasion compared with the 1988 observation.

The optical light and polarization curves of AM Herculis binaries are modulated by cyclotron beaming, eclipses by the secondary star and the accretion stream, and self-eclipses of the accretion region by the white dwarf itself. X-ray observations on different occasions using the EXOSAT satellite have shown that there is no eclipse by the secondary star (Osborne et al. 1987). The polarimetric data in 1985 were taken simultaneously with an EXOSAT observation. The combined data show clearly that the depression in the circular polarization at phase \( \phi_{\text{spec}} = 0.8 \) is due to an obscuration of the accretion spot by the intervening accretion stream. It is that part of the stream which is magnetically coupled and lifted out of the orbital plane. As has been pointed out by Cropper (1998), this requires the orbital inclination \( \iota \) to be larger than the colatitude of the accretion spot \( \delta_s \) (measured with respect to the rotation axis).

#### 3.2.2 Modelling the 1988 polarimetry

To determine the accretion geometry of QQ Vul, we take the
simple view of a point-like accretion region in a dipolar geometry. A simplified sketch of the geometry is shown in Fig. 7. Three vectors play an important role, namely the magnetic axis $\mathbf{m}$, the surface normal in the accretion spot $\mathbf{s}$, and the field in the spot $\mathbf{f}$. All vectors are shown projected on to an $x_0{\pm}z$ plane centred on the white dwarf, with $z$ being parallel to the rotation axis. For an analogous representation of the geometry see, e.g., Cropper (1989). The stellar colatitudes of the dipolar axis, the spot and the field therein are measured with respect to the rotation axis and designated $\delta$ with the corresponding subscripts $\mu$, $s$ and $f$. Similarly, the azimuths, $\chi$, of these vectors are measured with respect to the line joining both stars. Conventionally, the accretion stream in our geometry is deflected towards negative azimuth. Below we will discuss also the azimuth of the threading region, $\chi_{th}$ (Fig. 8), which is defined in the same reference frame.

Previous determinations of the accretion geometry based on polarimetry were published by Nousek et al. (1984) and Cropper (1998). Nousek et al. used a point-like accretion spot, and derived a stellar latitude of the accreting magnetic pole in the range $27^\circ \pm 10^\circ$; and an orbital inclination of $i = 46^\circ \pm 8^\circ$. Cropper (1998) investigated extended accretion arcs with constant temperature, magnetic field and density, and derived $i = 40^\circ \pm 5^\circ$ and a colatitude of the magnetic dipolar axis $\delta_{\mu} = 10^\circ$.

The markedly different yet simpler behaviour seen in the 1988 data, relative to all previous observations, called for a redetermination of the accretion geometry. Furthermore, with our extended data set, it is possible to find a solution that can encompass the results from both polarimetry and Doppler tomography. Previous analyses also lacked an absolute reference in the binary frame. We do not attempt to perform a least-squares fit of the polarimetric data; instead, we try to optimize the model globally (including polarimetry, X-ray photometry and Doppler tomography). Cropper
Figure 7. Sketch of the dipolar geometry at the white dwarf surface. Shown are a cut through the white dwarf and a single dipolar field line projected on an appropriately rotated x'-z plane. Also shown are vectors indicating the orientation of the dipolar axis $\mathbf{\mu}$, of the surface normal in the accretion spot $s$, and of the magnetic field line in the accretion spot $f$, the last being the tangent to the field line at the footprint. In a dipolar geometry $s$ and $f$ are always different.

Figure 8. Model for the coupling of the accretion stream as seen by a hypothetical observer located at the white dwarf. The big circle represents the secondary star. The adopted orientation of the dipole $\mathbf{\mu}$ is given by its azimuth $\chi_\mu = -50^\circ$ and its colatitude $\delta_\mu = 23^\circ$.

(1998), although using a more sophisticated model which accounts for an extended accretion arc, found a full inversion of the data (as in Potter, Hakala & Cropper 1987) objectively inefficacious, and also only globally optimized his model.

The following observed features are used for an estimate of the geometry: the length of the self-eclipse $\Delta \phi_{self}$, the variation of the polarization angle, and the phase of the circular polarization dip. Variation of the dipolar axis $\mathbf{\mu}$, the inclination $i$, and the coupling radius then predicts a different run of the polarization angle. By integrating the equation of motion for one particle with given mass ratio $Q$, one can also predict its velocity pattern in the $(v_x,v_z)$ plane (a schematic Doppler map) when projected with the assumed orbital inclination. The resulting image can then be compared with the observed Doppler maps (Section 3.3.4), thus constraining the azimuth $\delta_\theta$ of the threading region. A solution is accepted if the predicted tomogram and the predicted curve of polarization angle are globally optimized, and the phase of the X-ray/circular polarization dip is reflected well.

The separation between the linear polarization pulses is 0.24 phase units. The sign reversals of the circular polarization are separated by 0.18 phase units. For our estimate we use the mean of both values, $\Delta \phi_{self} = 0.21$. Both features are, in principle, measures of the same event, namely when the line of sight is perpendicular to $f$. The length of the self-eclipse of the accretion spot is shorter than this phase interval. The inclination is approximately $60^\circ$, as suggested by the slope $\phi_p$ of the polarization angle during the pulse (Fig. 6). The values of $i$ and $\Delta \phi_{self}$ constrain the possible values of the colatitude $\delta_i$ of the field line to a certain range (see Brainerd & Lamb 1985 for technical details). The dip is centred at $\phi_{spec} = 0.95$, corresponding to an azimuth of about $-20^\circ$.

Model curves for the polarization angle for the acceptable range of inclination angles, $i = 50^\circ$–$70^\circ$, are shown in Fig. 6, together with the 1988 data. Deviations between model and observation in the phase interval 0.8–1.1 should not be taken seriously, since this is the phase of depolarization in the stream and low intensity due to cyclotron beaming. The adopted values of the magnetic colatitude for the three model curves are $\delta_i = 47^\circ$, $38^\circ$ and $27^\circ$ for $i = 50^\circ$, $60^\circ$ and $70^\circ$, respectively.

A globally optimized fit, taking into account the different observational quantities, was achieved with the following system parameters: mass ratio $Q = M_1/M_2 = 1.75$, inclination $i = 60^\circ$, orientation of the dipole axis $\delta_\mu = 23^\circ$ and $\chi_\mu = -50^\circ$, and azimuth of the threading region $\chi_\theta = -20^\circ$. With these parameters the accretion spot emerges at $\delta_s = 33^\circ$ and $\chi_s = -40^\circ$, and the field line within the spot has $\delta_f = 36^\circ$ and $\chi_f = -37^\circ$. In Fig. 8 a series of field lines around this particular one is shown as seen from the white dwarf. An observer viewing the binary at inclination $i$ would be rotating along a line of constant latitude $l = 90^\circ$–$i$. Hence the figure illustrates that the line of sight for a likely inclination of about $60^\circ$ crosses the stream between $\chi = -17^\circ$ and $-32^\circ$, which corresponds to orbital phase $\phi_{spec} = 0.91$–0.95. At that phase the X-ray absorption dip was observed in the 1985 September data. The model thus reproduces the observed motion of the polarization angle, and the observed phase of the X-ray/circular polarization dip, and it reflects the main features of the Doppler tomograms (see Section 3.3.4).

Based on the analysis of the 1988 polarimetry, we do not claim an accuracy of the orbital inclination $i$ and the colatitude $\delta_i$ better than $10^\circ$. One should bear in mind, however, that these two quantities cannot be varied independently, they communicate with each other via $\Delta \phi_{self}$. A higher inclination requires a lower colatitude of the field $\delta_i$ and of the spot $\delta_s$. We note in particular that our estimate of $i$ based on polarimetry is in full agreement with the result of Paper I, $i = 65^\circ$, using high-resolution spectroscopy of the infrared Na lines. It is also in agreement with the analysis in Nousek et al. (1984), which is worth mentioning since their data look quite different. The somewhat lower values favoured by Cropper (1998), $i = 40^\circ$–$50^\circ$, are likely to be caused by the large scatter of the polarization angle in his data, which indicates a more complicated accretion geometry in 1983–1985.

Our results imply certain values of the azimuth and colatitude of
the accretion spot, which are in good agreement with X-ray
photometry (not used for the determination of the geometry so far).
The value of $\chi = -40^\circ$ predicts a minimum in the X-ray flux
at phase 0.39 due to projection effects. Indeed, this is exactly the
phase where the broad X-ray minimum occurred in the EXOSAT
data taken in 1985 September (Osborne et al. 1987). Although the
X-ray observations and our polarimetric observations were not
carried out simultaneously, the simple shape of the X-ray light
curve in 1985 and the simple polarimetric behaviour of QQ Vul
seen in 1988 are suggestive of a similar accretion geometry. On the
other hand, our parameter combination of $i$ and $\delta_i$ predicts a
complete self-eclipse of the point-like accretion region at that
phase, $i + \delta_i = 93^\circ > 90^\circ$, which is not observed. However, this
does not necessarily imply that the model is incorrect. For one
thing, the uncertainties associated with our derived values are
larger than $5\%$. More importantly, the accretion region is likely to
be extended.

3.2.3 Changes of the accretion geometry

Up to this point, we have considered and modelled only the 1988
observations. The shift of the X-ray absorption dip towards earlier
phases in 1985 June and 1983 October, when the X-ray light curve
had a complex shape, suggests that threading of the stream occurs
further downstream, i.e., farther away from the $L_1$-point at an
azimuth of $\chi_{1b} \sim -70^\circ$. The X-ray light curve of 1985 June, on
the other hand, shows a completely different shape from the 1985
September data, which cannot be explained by a simple migration of
the accretion spot towards a different azimuth. The fact that
phasing of the X-ray maximum in 1985 June occurs exactly at the
phase of minimum flux in the light curve taken three months later
suggests the presence of a second active accretion region on the
opposite hemisphere (Osborne et al. 1987). The corresponding
cyclotron emission from the second region must affect the
polarization measurements and probably distorts the simple
variation of the polarization angle seen in 1988, which probably
represents a one-pole accretion mode. This was already pointed
out by Cropper (1998), who also detected a second polarization
variation of the polarization angle seen in 1988, which probably
in 1985 September (Osborne et al. 1987). Although this inconsistency results from the reduced phase interval in which the NEL
velocities can be derived with good accuracy. Thus we will use
radial velocity amplitudes derived from the Doppler maps, which
are based on all the data instead of a restricted data set. To
compute the Doppler maps, we mainly used the code of Spruit

The relatively sharp separation between emission and absorption
features in the Doppler map shown in Fig. 3 requires us to
address the following questions. (1) Is it possible to reconstruct the
shape of the Roche lobe and thus determine the mass ratio $Q$ using
Doppler maps of the Na I-lines alone? (2) Is it possible to measure
the size of the Roche lobe of the secondary directly using the
velocities of the illuminated and non-illuminated hemispheres of
the secondary star, provided these could be unequivocally deter-
mined observationally? Answering these questions, in particular
locating the $L_1$-point, is essential for the next section’s investiga-
tion of the accretion stream using Doppler tomography.

3.3 Analysis of the emission lines

3.3.1 Origin of the narrow emission lines

Our initial analysis of the simultaneously recorded spectrograms of the He II emission and the Na I absorption lines in Section 3.1
based on radial velocity fits suggests that the NEL and the absorption
lines originate on opposite hemispheres of the secondary
star. This impression is supported by a combined Doppler
tomogram of both lines (Fig. 3), which was constructed using
MEM-deconvolution of the trailed spectrograms. We had chosen the He II emission line for this initial analysis because it is
intrinsically the sharpest of the bright lines in the blue spectral
regime. With a full-width at half-maximum (FWHM) of 1.9 Å
(1991) and 2.0 Å (1993) at phase 0.5, the NEL of He II is just
resolved. The NEL components of the H-Balmer lines at the same
phase have a FWHM of 3.7 Å, those of He I have 2.5–4 Å. The
NEL of Mg II λ4481 is comparable in width to that in He II λ4686,
but has a much lower flux and thus reduced S/N.

A comparison of the results from the fit to the radial velocity
measurements and those from the Doppler map (Section 3.1) for
the same data set reveals an inconsistency between the radial
velocity amplitudes in the NEL. Maximum emission in the
Doppler map occurs at $v = |v_r| = 96 \text{ km s}^{-1}$, whereas the radial
velocity fit gives $v = 116 \pm 6 \text{ km s}^{-1}$. We think that this incon-
sistency results from the reduced phase interval in which the NEL
velocities can be derived with good accuracy. Thus we will use
radial velocity amplitudes derived from the Doppler maps, which
are based on all the data instead of a restricted data set. To
compute the Doppler maps, we mainly used the code of Spruit

In brief, the irradiating source is located at $M_1$, and it is
assumed that the secondary’s surface is illuminated by the accretion stream or an
accretion curtain occurs, and that a sharp separation of irradiated and non-irradiated parts of the secondary exists. We assume that
both emission and absorption lines originate from the photosphere, i.e., from the Roche lobe of the secondary. The shape of the Roche lobe is iterated for given $Q$. Line emission from a
surface element on the irradiated secondary is taken to be
proportional to the solid angle as seen from the source at $M_1$.
Radiation is assumed to be optically thick; hence foreshortening of surface elements has to be taken into account. For the non-
illuminated parts of the secondary star we assume that an
absorption line is formed whose strength is proportional to the size
of the surface element, and we also take foreshortening of the
individual element into account. Emission- and absorption-line
profiles are synthesized using the full Roche geometry. Since the
spread of the radial velocity over the secondary’s surface is of the
order of several hundred km s$^{-1}$, we regard velocity broadening as
the only broadening mechanism of spectral lines. In order to
transform velocities from dimensionless binary coordinates into
the observer’s frame, we adopt the mass–radius relation by Neece
(1984) for the secondary star. The often used empirical relation by
Caillault & Patterson (1990) gives slightly different results (see
below).

As mentioned above, our model does not take into account any
kind of shielding of the secondary star by, e.g., an accretion
curtain. This was present at some occasions in AM Her and HU
Aqr (Davey & Smith 1996; Schwwope et al. 1997), and became
obvious in these stars by a prominent left/right asymmetry of the
Doppler maps. Such an obvious asymmetry is not present in the
combined He/Na Doppler map of QQ Vul, and the centres of light
of both species lie at $v_r = 0 \text{ km s}^{-1}$ (Fig. 3), i.e., indicating far less
shielding (or none at all) in 1991 than in 1993. Shielding was present in 1993 (cf. Paper I), with the effect that the radial velocity curve of Na\textsubscript{i} had a higher ellipticity, yet smaller amplitude.

In order to answer question (1), we computed absorption-line profiles with the same spectral resolution, orbital phase sampling and noise level as our 1991 observations. In Fig. 9 we compare reconstructions of data with (a) infinite resolution and S/N, (b) resolution, sampling and noise as in 1991 ($\Delta v_{\text{FWHM}} = 80\,\text{km}\,\text{s}^{-1}$ measured using arc lines), (c) sampling and noise as before, but degraded resolution ($\Delta v_{\text{FWHM}} = 180\,\text{km}\,\text{s}^{-1}$), and (d) a reconstruction of the observed data. The Roche lobe used for generation of the data is shown in each panel.

From that exercise we learned (panel a) that it is possible to reconstruct the original shape of the non-irradiated hemisphere of the companion star using high-quality data (high resolution, low noise), not a big surprise. The reconstruction shown in panel (b), which uses data of same quality as the observed data appears somewhat smeared. This map has already lost the arc shape of the inner contours of the reconstruction in panel (a).

Due to the limited resolution of the data, the contours extend into the nominally dark, front-side hemisphere of the star. The whole map has a smaller FWHM than the reconstruction of the observed data (panel d). In order to match the FWHM of the map in panel (d), we had to degrade the resolution in our simulation to values as high as $\Delta v = 180\,\text{km}\,\text{s}^{-1}$. The resulting map (panel c) is almost rotationally symmetric, and no longer displays a half star as all other maps do. The high degree of similarity between maps (b) and (d) suggests that the Na\textsubscript{i} absorption almost entirely originates from the non-irradiated hemisphere of the companion star, and that the size of the Roche lobe chosen for the simulations is a fairly good representation of the true size. Variation of $Q$ increases the size, and shifts the lobe along the $v_\lambda$-axis, making the fit worse.

Our guess is that the observed map is disturbed by some effect, and is therefore not as sharply reconstructed as the simulated one. For example, emission from the nearby He\textsubscript{ii} 8236 line and the corresponding curved continuum could easily contaminate the absorption lines. The range of $Q$, which gave acceptable fits (by eye) to the location and curvature of the contours of the observed Doppler map, is $Q = 1.5$–$2.2$ (for $i$ between 50° and 71°), with a best agreement at about $Q = 1.8$.

Fig. 10 addresses question (2). We attempt to (further) constrain the mass ratio using the velocity ratio of the photocentres of the illuminated and non-illuminated hemispheres of the secondary star. Synthetic spectra computed for different mass ratio $Q$ and orbital inclination $i$ were used. The inclination only has a small effect on the velocity ratio. Theoretically, the velocity ratio $v_b/v_F$ is a steep function of $Q$. This – in principle – offers the opportunity to measure the size of the Roche lobe by determining the velocities of the photocentres. We assume that, observationally, the velocity of the non-irradiated side of the secondary star is $v_b = 271\,\text{km}\,\text{s}^{-1}$, the largest velocity amplitude of the Na\textsubscript{i} lines measured so far (1991 data). Above, we have argued that the Doppler map is consistent with a complete depletion of the irradiated front side of Na absorption. Incomplete Na depletion would mean that the true $v_b$ would be larger and the derived mass ratio smaller.

Using all NEL’s radial velocity amplitudes with estimated uncertainties better than $10\,\text{km}\,\text{s}^{-1}$ as potential tracers of $v_b$, observed ratios $v_b/v_F$ were computed. These ratios, shown as dotted lines in Fig. 10 are highly dispersed, from 85 km s$^{-1}$ for He\textsubscript{i} 4471 in 1993 to 135 km s$^{-1}$ for Ca\textsubscript{ii} in 1991, and do not allow

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure9.png}
\caption{Numerical experiments showing the effects of noise and sampling on the reconstructed Roche lobe. The input Roche lobe used for generation of synthetic spectra is shown in each panel. (a) Reconstruction without noise, infinite velocity resolution and velocity sampling 12 km s$^{-1}$, phase sampling 0.00556; (b) reconstruction with noise at observed level, velocity resolution 80 km s$^{-1}$, phase sampling 0.0556; (c) reconstruction with noise at observed level, velocity resolution 180 km s$^{-1}$, phase sampling 0.0556; (d) reconstruction of the observed (1991) spectra. In panels (b) – (d) the isocontours represent between 10 and 90 per cent of maximum intensity in steps of 20 per cent. The isocontours drawn in (a) are the 20–80 per cent, intensity levels in steps of 20 per cent, with an additional contour at 90 per cent.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure10.png}
\caption{Velocity ratio of the photocentres of the irradiated front- and the non-irradiated backside of the donor star due to our irradiation model compared with the observed velocity ratios of Na\textsubscript{i} absorption lines ($271\,\text{km}\,\text{s}^{-1}$) and narrow emission lines (NEL) of different species (data from 1991 and 1993). The solid line is a spline fit through the filled dots which were computed for $i = 90^\circ$, and the open circles were computed for $i = 60^\circ$ (fit indicated by dashed line).}
\end{figure}
us to constrain the mass ratio better than when using the Na i lines alone (see above and Paper I).

For \( Q = 1.85 \) and \( i = 65^\circ \) (Paper I), the predicted velocity \( v_1 \) is 115–125 km s\(^{-1}\), that of the \( L_1 \)-point is \( v_{1L1} = 75–80 \) km s\(^{-1}\), and \( v_b/v_1 = 2.36–2.17 \). For these parameters the H-Balmer lines are apparently the most suitable tracers of \( v_f \). The Ca and Paschen lines are compatible with this solution within the accuracy of our velocity determination, while the He ii lines display too low velocities, i.e., they originate closer to the \( L_1 \)-point. Obviously these lines are formed in an extended quasi-chromosphere located above the photosphere. The He ionizing radiation is not able to reach the whole geometrically allowed hemisphere of the secondary. The data presented here are thus able to resolve (although marginally) these different layers. A quantitative understanding of the formation of the emission lines requires detailed modelling of non-isotropically X-ray-irradiated photospheres of late-type stars, a project within reach of current models (e.g. Hauschildt, Baron & Allard 1997), but not yet undertaken.

### 3.3.3 Multi-epoch line flux variations

For the analysis of emission lines originating from the stream, we make use of emission-line light curves and Doppler maps, shown in Figs 11 and 12. The emission-line light curves are based on the integrated line profiles of the trailed spectrograms shown in Fig. 12. We approximately removed the contribution of the NEL, which does not originate from the stream, by measuring its flux at phase \( \phi_{\text{spec}} = 0.5 \), adapting a simulated emission-line light curve to that level and subtracting it from the total flux. These NEL-free light curves are also shown in Fig. 11. For comparison, continuum light curves extracted from a line-free region between the two emission lines H\( \beta \) and He ii \( \lambda 4686 \) are also shown.

The continuum light curves are all similar in shape, displaying a double-humped structure with the primary minimum centred on \( \phi_{\text{spec}} = 0.95 \) in 1991 and 1993, and probably somewhat earlier, and on \( \phi_{\text{spec}} = 0.92 \) in 1986. As discussed in Section 3.2, this minimum is caused by cyclotron beaming, and the small shift of minimum phase at the different epochs indicates a possible azimuthal shift of the emission region.

The emission-line light curves are also double-humped, with intensity maxima at phase 0.2 and 0.7. This behaviour is more pronounced in H\( \beta \) than in He ii, and more obvious after subtraction of the NEL, which peaks at \( \phi_{\text{spec}} = 0.5 \). Pronounced minima occur in the phase interval 0.92–1.00, and the minima in H\( \beta \) generally occur earlier by \( \sim 0.03–0.05 \) phase units at all epochs. The minima in both lines occurred earlier in 1986 than in 1993. The light curves in 1986 are highly asymmetric, with a pronounced first maximum which is more than double the height of the second one. All these observed properties are suggestive of
optically thick radiation in the accretion stream, with the stream having a higher thickness in 1986 than at the two other epochs.

3.3.4 Multi-epoch trailed spectrograms and Doppler maps of He\textsuperscript{ii} l\textsubscript{4686}

The trailed spectrograms and the Doppler maps are also markedly variable between the three epochs. We show in Fig. 12 the trails and maps of He\textsuperscript{ii} l\textsubscript{4686}. The data of the other emission lines look very similar as far as the velocity pattern (though not the brightness pattern) is concerned. Looking first at the trailed spectra, the NEL is the most obvious and the most pronounced feature in all three observations. The underlying emission from the stream is brighter close to the NEL emission in 1991 and 1993 than in 1986. Hence, during the two recent observations the stream was brighter in the vicinity of the inner Lagrangian point \( L_1 \) at rather lower velocities than in 1986, when stream emission was bright at higher velocities.

This is nicely illustrated too in the Doppler maps which are shown as contour plots below the trailed spectrograms in Fig. 12. Contour levels were chosen appropriately to emphasize stream emission (the inner contour corresponds to the maximum intensity level from the stream). In 1991 and 1993, there is some bright emission originating approximately at \( L_1 \) and extending down to velocities \( v_y \sim -500 \text{ km s}^{-1} \) at constant \( v_x \). From there, a tail stretches down to the lower left region of the maps, which can be recognized at velocities as high as \((v_x, v_y) = (-1200, -700) \text{ km s}^{-1}\). Within the resolution of our data, the orientation of these high-velocity tails is the same in all maps.

The initial ridge of emission between \( L_1 \) and \((v_x, v_y) \sim (-400, 50) \text{ km s}^{-1}\) can be tentatively identified with emission originating from the ballistic stream, as seen as prominent features in HU Aqr and UZ For (Schwope et al. 1997, 1999). There are, however, some problems with this interpretation, since this ridge shows a displacement by \( \Delta v_y = 45 \text{ km s}^{-1} \) between 1991 and 1993. If it were a purely ballistic stream, it would be fixed in the binary and always appear at the same \( v_y \)-velocity. In the following we will use the term ‘ballistic’ stream for the bright ridge of emission connected to the secondary star seen in the 1991 and 1993 tomograms, although it might not appear at a ballistic velocity at all.

We determined the location of the ballistic stream by fitting a Gaussian curve to the Doppler maps at \( v_x \sim -250 \text{ km s}^{-1} \). Maximum emission occurred at \( v_y = 45 \text{ km s}^{-1} \) in 1991, and at \( v_y = 0 \text{ km s}^{-1} \) in 1993. For a first-order estimate, we set the \( v_y \)-velocities at \( L_1 \) and at \( v_x = -250 \text{ km s}^{-1} \) to be the same. For our best guess of \( Q \) and \( i \), the projected velocity \( v_y \) at \( L_1 \) is 75–80\text{km s}^{-1} (see above). Only for the lower limit value \( Q = 1.5 \),
$i = 70^\circ$, is the projected $v_x = 51\text{ km s}^{-1}$ as low as observed in 1991. Hence, on both occasions (1991 likely, 1993 definitely), the observed ballistic stream appears at smaller velocities $v_x$ than predicted by a single-particle trajectory for the likely parameter combination of $i$ and $Q$.

Emission which could be apparently associated to the ballistic stream was almost completely absent in 1986. At that epoch a bright spot of emission centred on $(v_x, v_y) = (-380, -100)$ km s$^{-1}$ emerged instead.

As a first step to gain a quantitative understanding of the location and extent of the different parts of the stream in the magnetosphere, we have computed models for the accretion stream, representing it by a single-particle trajectory under gravitational and centrifugal influence. We accounted for the pull of the magnetic field on the partly ionized stream by a gravitational and centrifugal influence. We accounted for the

---

A model which accounts for most of the observed features of the 1991 and 1993 tomograms of He ii is shown in Fig. 13. We simulated several different trajectories coupling at different radii by varying the magnetic field strength, which appears as a dimensionless tuning parameter in our calculations. The trajectories shown in Fig. 13 in velocity space are the same as those shown in Fig. 8 in real space. The smaller the assumed value of the field strength, the longer the particle remains on the ballistic trajectory (coupling at larger azimuth) and the higher the velocity at the threading point becomes. Observationally, the ballistic part of the accretion stream can be followed down to $v_x = -500\text{ km s}^{-1}$. It is perhaps a bit more elongated in 1991 than in 1993, but this is difficult to state exactly, because the Doppler map of 1991 has a poorer velocity resolution. A velocity of $v_y = -500\text{ km s}^{-1}$ on the ballistic stream corresponds to an azimuth of the coupling region of about $-25^\circ$. Coupling may - in principle - occur all along the ballistic stream between the $L_1$-point and that azimuth. The orientation of the axis of the magnetic field was chosen in accord with polarimetry (Section 3.2). With the chosen field geometry the magnetically funnelled part of the trajectories stretches along a more or less straight line in the lower left quadrant of the velocity plane, almost exactly along the observed high-velocity ridge in the Doppler maps (indicated by a straight line in Fig. 13).

This simple model cannot account for the observed displacement towards smaller $v_y$-velocities of the ‘ballistic’ stream with respect to the single-particle trajectory. One possible explanation for this displacement is that a proper ballistic stream (not influenced by the magnetic field) exists, but that the observed emission is dominated by matter with slightly changed velocity (matter in the process of getting coupled). Another possibility has recently been worked out by Sohl & Wynn (1999), who treated the accretion flow as a number of diamagnetic blobs which independently interact with the magnetosphere of the primary. This model predicts blob trajectories differing from single-particle trajectories and might be applicable to QQ Vul.

The apparent absence of a ballistic stream in 1986 and the occurrence of the bright spot at $(v_x, v_y) = (-380, -100)$ km s$^{-1}$ remain unexplained so far. There might be two explanations for the missing ballistic stream: either matter couples on the field directly at $L_1$, or the stream was outshone by other emission components and therefore not recognizable at the phase and spectral resolution of our observations. We investigated the first possibility by tuning the magnetic field strength in our models to high values (which mimics low accretion rates), so that no ballistic stream was formed. We then used different orientations of the dipolar axis in order to check whether the trajectory runs through the observed bright spot down to the lower left quadrant in the $(v_x, v_y)$ plane. Azimuth and latitude of the magnetic axis were varied over large ranges, but no solution was found. We conclude that the resolution of the 1986 data and the brightness of the other components prevented us from detecting emission from the ballistic stream.

---

3.3.5 A simple model for the emission-line light curves

Support for the view that the bulk of matter does not couple at $L_1$ but somewhere downstream comes from some numerical experiments which were performed to reach a basic understanding of the emission-line light curves. A single-particle trajectory between the $L_1$ point, the coupling region and the white dwarf was divided into 100 parts of equal length, and each element was assigned an intensity value. We allowed for two different brightness values, depending on whether the irradiated or the non-irradiated side of the stream was seen. Emission from an element was assumed to be optically thick; hence the observed brightness of an element at a given phase was the intrinsic brightness times a foreshortening factor. The brightness $b$ of the vertical stream (along the dipolar
field line) was varied as a function of radius with $b \propto r^{1.5}$, starting with some initial value in the threading region. This radial dependence accounts for the shrinkage of the effectively emitting area due to the converging field lines. Light curves were computed by co-adding over all visible elements at a given phase, taking the full Roche geometry into account so that eclipses of parts of the stream are recognized if the inclination is high enough.

In Fig. 14 we show the resulting model light curves for the ballistic part of the stream and the magnetically funnelled part. The central trajectory of those shown in Figs 13 and 8 was used, and a contrast of 1:0.7 between the irradiated and non-irradiated sides of the stream was adopted. The light curves were computed for an assumed orbital inclination of 65°. Both light curves were normalized to maximum emission. Emission from the ballistic stream shows emission maxima at $\phi_{\text{spec}} = 0.3$ and 0.8, which is simply an expression of the deflection angle of $\sim 18^\circ$ of the ballistic stream with respect to the line connecting both stars. The primary minimum at $\phi_{\text{spec}} = 0.02$ is caused by the combined effect of foreshortening and a partial eclipse of the stream by the secondary star.

The model light curve from the magnetically funnelled part of the stream shown in Fig. 14(b) is affected only by foreshortening. This causes the maxima of emission to appear at spectroscopic phases 0.2 and 0.7, and the minima at phases 0.45 and 0.95. These phases are in good agreement with the observed maxima and minima of the emission lines of Fig. 11. These phasings and the absence of pronounced stream eclipses by the secondary star are suggestive of stream emission mainly originating from the magnetic part of the stream (in 1991 and 1993) or the threading region (1986). The visual impression of the Doppler maps (1991, 1993) is in apparent contradiction to this statement, since they show emission associated with the ballistic stream as a prominent feature. We regard the contradiction as apparent only for two reasons. First, as discussed above, at least part of the emission associated with the ballistic stream originates from matter which is coupled to the field, and thus is expected to produce a light curve resembling that in Fig. 14. Secondly, the surface brightness distribution of a Doppler map does not reflect the brightness distribution in real space. In particular, emission at high velocities is spread over a large region in a $(v_x, v_y)$ diagram. The summed flux of the high-surface-brightness pixels in the region defined by $(v_x, v_y) = (-500, -40) \text{ km s}^{-1}$ (lower left corner) and $(120, 200) \text{ km s}^{-1}$ (upper right corner), i.e., including the NEL from the secondary star, contributes only to about 40 per cent (1991) and 50 per cent (1993) of the total intensity in the maps. Hence, low-surface-brightness emission from higher velocities is dominating in the stream.

The Doppler maps indicate that we can best differentiate between emission from the ballistic and the magnetic stream at phases 0.25 and 0.75, i.e., in the direction of the $v_y$-axis. Projection in these directions produces a relatively sharp spectral feature of emission associated with the ballistic stream (though not as sharp as the NEL from the secondary), whereas emission from the magnetic stream will appear as a rather broad feature. Fitting the observed spectra (1991 and 1993) at these indicated phases with triple Gaussians (NEL plus medium-width and broad components) reveals that the medium-width and broad-base components carry almost the same flux at these phases on both occasions. If we then take into account the fact that even the medium-width component is fed by emission from matter which has already latched on to the field, it seems plausible that most of the observed line emission comes from the magnetically funnelled stream and/or matter which is in the process of becoming funnelled, and that emission from the ballistic stream plays a minor role in the formation of the emission-line light curves. Hence Doppler maps and emission-line light curves tell us the same story.

4 CONCLUSIONS AND OUTLOOK

Using medium- and high-spectral resolution observations with full phase-coverage of the long-period AM Herculis binary QQ Vul obtained on three occasions in 1986, 1991 and 1993, and complementary polarimetry obtained between 1985 and 1988, we studied the accretion geometry in the inner and outer magnetosphere. First of all, we derived a reliable spectroscopic ephemeris for inferior conjunction of the secondary star by combining Na I photospheric absorption lines with narrow emission lines of reprocessed emission from the X-ray-irradiated hemisphere. HJD$(T_0) = 2448446.4710(5) + E \times 0.15452011(1)$. The arrival times of linear polarization pulses show a large scatter in an $(O-C)$ diagram with respect to the new ephemeris, and thus are disqualified as useful tracers of the orbital motion for the case of QQ Vul.

Analysis of the linear and circular polarization curves favour an orientation of the (dipolar) magnetic axis of $\delta_m = 23^\circ$ and $\chi_m = -50^\circ$, and an orbital inclination between 50° and 70°. The variable shape of the polarization curves, in particular the phasing of circular polarization dips, suggests that the azimuth of the coupling (threading) region undergoes significant migrations in azimuth.

The suggested orientation of the magnetic dipole and of the coupling region is in good agreement with the results inferred from Doppler tomography of bright emission lines, in particular those of He II $\lambda 4686$. These show (in 1991 and 1993) three distinct emission features: (1) the irradiated hemisphere of the secondary star, (2) emission which can be associated with the ballistic stream, and (3) emission from the magnetically funnelled stream. Emission, which apparently arises from the ballistic stream, appears at different places in the Doppler tomograms of 1991 and 1993. This suggests that it is formed by matter which is in the process of becoming threaded, in complete agreement with the...
emission-line light curves, which show the major contribution from the magnetic part of the stream. On one occasion (1986) the Doppler maps do not reveal any emission that could be associated with the ballistic stream.

We explored whether it would be possible to use the narrow emission lines from the secondary star in combination with photospheric absorption lines to constrain the mass ratio and the orbital inclination. This was not possible in QQ Vul, because the radial velocity amplitudes of different atomic species were found to be widely different. Lines from high-ionization species such as $\text{He}^\text{II} \lambda 4686$ originate more closely to the $L_1$ than a reprocessing model predicts.

The Doppler tomograms presented in this paper suggest that threading of the accretion stream (or parts of it) starts very soon, or perhaps immediately, after leaving the secondary star. The stream seems to be completely disrupted at an azimuth of about $-30^\circ$. Future observations with higher spectral and temporal resolution of the Na $\text{I}$ lines (1) will allow the mass ratio to be determined with an accuracy of better than 10 per cent by the straightforward application of Doppler tomography, and (2) will reveal substructure in the Doppler maps due to, e.g., star spots.

ACKNOWLEDGMENTS

This paper was based in part on observations at the European Southern Observatory La Silla (Chile) with the 2.2-m telescope of the Max-Planck-Society. We thank Rick Hessman for carefully reading an early version of the manuscript, and the anonymous referee for helpful criticism. This work was supported by the DLR under grant 50 OR 9403 5, and by the Deutsche Forschungsgemeinschaft under grant Be 470/12-2.

REFERENCES


This paper has been typeset from a TEX/LATEX file prepared by the author.